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December 7, 1983 BRANCH

John H. Frye, III, Chairman  
Administrative Judge  
Atomic Safety and Licensing Bd.  
U.S. Nuclear Regulatory Comm.  
Washington, D.C. 20555

Dr. Emmeth A. Luebke  
Administrative Judge  
Atomic Safety and Licensing Bd.  
U.S. Nuclear Regulatory Comm.  
Washington, D.C. 20555

Glenn O. Bright  
Administrative Judge  
Atomic Safety and Licensing Board  
U.S. Nuclear Regulatory Commission  
Washington, D.C. 20555

In the Matter of  
THE REGENTS OF THE UNIVERSITY OF CALIFORNIA  
(UCLA Research Reactor)  
Docket No. 50-142  
(Proposed Renewal of Facility License)

Re: Neutron Transport Calculations Requested by CBG

Dear Administrative Judges:

Enclosed are the raw data underlying the neutron transport calculations of Mr. Ostrander which were described in connection with the Wigner energy calculation in University's rebuttal testimony. This material was requested by CBG in Mr. Hirsch's letter of November 18, 1983.

Also enclosed is Mr. Ostrander's "Correction" to those calculations. The relevant effect of the correction is to change the reported result of the "Monte Carlo" calculation of the percentage of fission neutron energy deposited in the graphite (and fuel region) from 15% (and 85%) to 19% (and 81%). A separate correction is made to the uncollided flux calculation which changes the reported result from 85% to 71%; however, this calculation does not directly enter any of the analyses nor is it relied upon by any of University's witnesses. (In this regard, I note that I inadvertently over-stated the significance of these corrections on page 18 of "University's Response to CBG's Objections to Rebuttal Testimony", dated December 2, 1983: the only significant changes are the change in the reported percentage of fission neutron energy absorbed in the water, which is noted at several places in University's rebuttal testimony, from 85% to 81%; and the change from 15% to 19% for the percentage of fission neutron energy deposited in the graphite which enters into the last step of the Wigner energy calculation.)

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PDR ADDCK 05000142  
PDR

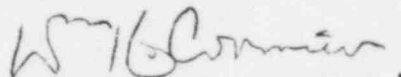
D503

Administrative Judges  
December 7, 1983

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We had intended to respond to CBG's request by reproducing the computer code listing and data for the Monte Carlo calculation with further explanations in a more presentable form, but because of CBG's insistence that the calculations be presented now, we have abandoned that time-consuming effort.

Very truly yours,

A handwritten signature in dark ink, appearing to read "W H Cormier", followed by a period.

William H. Cormier

Enclosures

cc: Service List

## C O R R E C T I O N T O

THE DISTRIBUTION OF FISSION NEUTRON ENERGY DEPOSITION BETWEEN FUEL REGIONS  
AND GRAPHITE IN AN ARGONAUT RESEARCH REACTOR

BY

N.C. OSTRANDER

Two calculations were performed to determine the percentage of fission neutron energy deposited in the fuel region and graphite of an Argonaut research reactor. The first calculation was based on a model of the "uncollided flux" which reached the graphite. The second calculation utilized a detailed "Monte Carlo" method which traced the paths and energy deposition of individual neutrons. As previously reported, the Monte Carlo calculation yielded the result that approximately 85% of the fission neutron energy was deposited in the fuel region and only 15% was deposited in the graphite. This result was stated to be consistent with the result obtained based on the "uncollided flux" model calculation. Two corrections are to be noted.

### The Uncollided Flux Calculation

The model of the uncollided flux used and previously reported yields the fraction of the fission neutrons which reach the center graphite

island at high energy. That fraction is approximately 15%. However, an approximately equal fraction reaches the graphite reflector opposite the center island. As a result, the total fraction of fission neutrons which reach the graphite at high energy is approximately 29%. As previously reported, the result failed to properly account for the "mirror image" symmetry of the calculational model.

#### The Monte Carlo Calculation

The Monte Carlo calculation is not affected by the correction made in the uncollided flux calculation. However, verification of the calculation disclosed that of the population of 45 neutrons whose paths were traced, only 19 of the neutrons initially started in the direction of the graphite while 24 of the neutrons moved toward the interior of the fuel box. The initial directions of two of the neutrons could not be ascertained. Although the initial directions were determined by means of a random number sub-routine in the program, the selection produced an obvious bias in the procedure which could have affected the results.

In order to remove the bias, eliminate the two neutrons of uncertain initial direction, and to improve the statistics by providing a more uniform sampling of the initial directions, thirteen neutrons of the initial population have been discarded and eighteen new neutron samples were run to provide a population of 50 neutrons. Of the discarded



neutrons, only three had reached the graphite and that sub-population deposited only 5.7% of its total energy in the graphite.

For the new population of 50 neutrons, the estimate of energy deposition in the graphite is 19%, instead of approximately 15% as previously reported, and, accordingly, 81% of the energy is deposited in the fuel region.

#### Comparison of the Two Calculations

The Monte Carlo calculation indicates that about 34% of the fast neutrons enter the graphite above 0.8 mev. The corrected uncollided flux model suggests 29%. The 34% of the fast neutrons that enter the graphite transport an average energy of 1.88 mev per neutron to the graphite. However, these neutrons rarely stay in the graphite and much of their energy is ultimately deposited in the fuel box. The Monte Carlo calculation demonstrates that an average net deposition of 0.94 mev per fast neutron (greater than 0.8 mev) occurs in the graphite. In other words, the uncollided flux does not deposit the entirety of its energy in the graphite, but more nearly 50% of its energy. The other source of energy deposited in the graphite is due to a small fraction (approximately 10%) of the population that occasionally migrate into the graphite but at much lower average energy levels.

Thus, there is a relationship between the uncollided flux and the energy deposition in graphite, but it cannot be interpreted without more

precise information concerning the energy deposition due to the flux and the lower energy neutrons which are responsible for a small contribution to the total energy deposited in the graphite. These factors cannot be accounted for the calculation based on the uncollided flux model, but they are accounted for in the Monte Carlo calculation.

I. Uncollided Flux Integral

II. Monte Carlo: Program and Results

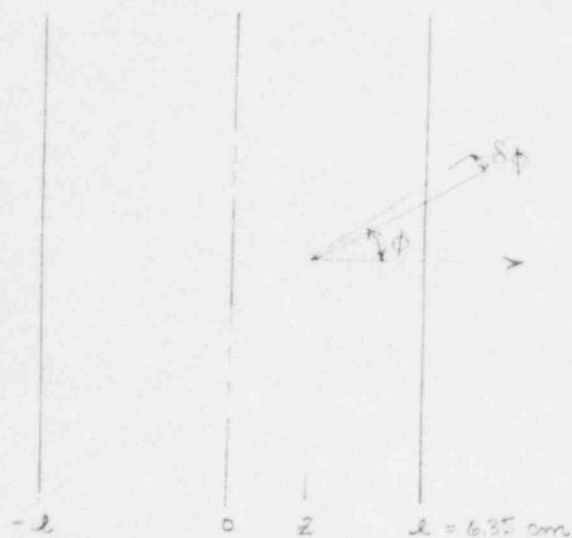
## The Uncollided Flux Integral

Fuel Box Composition (by volume) al:  $H_2O = 0.34 : 0.66$

component	atoms/cm <sup>3</sup>	<sup>235</sup> U $\Sigma_a$ (karns)	$\Sigma_a$ (cm <sup>-1</sup> )	$\Sigma_a$	%
H	$4.37 \times 10^{22}$	2.90	0.127	0.127	59
O	$2.19 \times 10^{23}$	1.40	0.030	0.088	41
al	$2.05 \times 10^{26}$	2.82	0.058		
			0.215	0.215	100

(Source: BNL-325, see Monte Carlo calculations, p. 5)

Fission neutrons are born at an average density of  $N$  per cm<sup>3</sup>. The geometry is that of a solid bounded by two planes ( $x-y$ ) that are of infinite extent.



In the region  $\delta z$  at  $z$ , the fission neutron density is  $N \cdot \delta z$  per square cm.

The neutrons are emitted isotropically and the fission neutron density is

$$\delta n = \frac{N}{4\pi} \delta z \cdot d\Omega \cdot \sin \phi \, d\phi$$

The integration over the azimuthal angle  $\theta$  is just a multiplication by  $2\pi$  and

$n$  = the number of neutrons per square cm which transit the plane  $z = l$  without having a collision in the fuel box.

$$n = \frac{N}{2} \int_{\phi=0}^{\pi/2} \int_{z=-l}^l e^{-(l-z)\Sigma_a/\cos \phi} dz \sin \phi \, d\phi$$

Note that if  $\Sigma_a = 0$ ,  $n = Nl$ , and half of the fission neutrons cross the plane  $z = l$ , the other half cross the plane  $z = -l$ .

uncollided flux (cont)

Let  $\cos \phi = \mu$  and  $x = l - z$ . The integral becomes

$$\begin{aligned} n &= \frac{N}{2} \int_{\mu=0}^1 \int_{x=0}^{2l} e^{-x \Sigma_s / \mu} dx d\mu \\ &= \frac{N}{2 \Sigma_s} \int_{\mu=0}^1 (1 - e^{-2l \Sigma_s / \mu}) \mu d\mu \\ &= \frac{N}{2 \Sigma_s} \left[ \frac{1}{2} - \int_{\mu=0}^1 e^{-2l \Sigma_s / \mu} \mu d\mu \right] \end{aligned}$$

with the substitution  $y = 1/\mu$ , the remaining integral is found to be the exponential integral,  $E_3$ .

$$E_3(2l \Sigma_s) = \int_1^{\infty} e^{-2l \Sigma_s y} \frac{dy}{y^3}$$

$$n = \frac{N}{2 \Sigma_s} \left[ \frac{1}{2} - E_3(2l \Sigma_s) \right]$$

with  $l = 6.35$  and  $\Sigma_s = 0.215$ ,  $2l \Sigma_s = 2.73$  (see Handbook of Mathematical Functions (Abramowitz and Stegun, editors), U.S. Dept. Commerce, AMS 55, June 1964, p. 228 eq. 5.1.4 and p. 248 for tables).

$E_3(2.73) \approx 0.0123$ . neglecting  $E_3$  relative to 0.5

$$n = \frac{N}{4 \Sigma_s}$$

The total fission neutrons generated per square cm of fuel box surface is  $2Nl$  and hence the fraction which has first collisions with graphite in the region  $z > l$  is

$$f = \frac{n}{2Nl} = \frac{1}{2l \Sigma_s} = 0.0916$$

correction - see next page.

The number  $f$  should be doubled to include the uncollected flux in the reflector.

$$f_1 = \frac{1}{4.2 \Sigma_0} = 0.183$$

The probability of a collision with a heavy atom is the probability of non-escape ( $1 - 0.183 = 0.817$ ) times the probability that the collision is with O or Al instead of H.

$$f_3 = 0.817 \left( \frac{\Sigma_0 + \Sigma_{al}}{\Sigma_0} \right) = 0.817 \left( \frac{0.088}{0.215} \right) \\ = 0.334$$

The probability of  $n$  such events followed by escape is  $f_3^n$  and the probability that the neutron escapes after 1, 2, 3, ...  $N$  such events is

$$F = f_1 (1 + f_3 + f_3^2 + \dots + f_3^N) \\ = \frac{f_1 (1 - f_3^{N+1})}{1 - f_3} \rightarrow \frac{f_1}{1 - f_3} \\ = \frac{0.183}{1 - 0.334} = 0.28$$

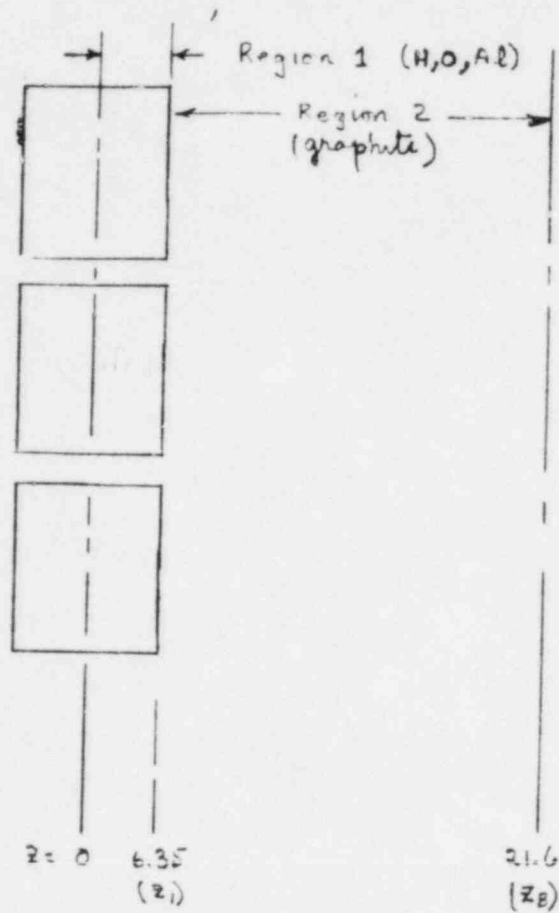
# A Monte Carlo Calculation of Energy Deposition in graphite by Fast Neutrons

The computer program is written for a Hewlett-Parkard, HP-41CV, with an extended Function/memory module. The latter is an unessential convenience for register manipulation and data storage. The idealized one dimensional geometry of the UCLA reactor is shown in Figure 1. The attached program, notes, and results are indexed here for convenience.

	<u>page</u>	<u>Lab. Note, pg</u>
Fig. 1 Geometry	2	2
Program "MC"	3	59
Program "Σ"	4	60
Cross Section Data	5	4
Program "REF"	6	34, 35
REF/SIJ Logic	7	5
Program "SCN"	8	61
Program "SCAT"	9	45
Direction Cosines	10, 11	31, 32
Program "SHOW"	12	62
Program "UZ"	12	62
Register Assignments	13	58
Results (1st 45 neutrons)	14-28	39-44, 47-51
Summary of results (45 neutrons)	28	55
Results (next 18 neutrons)	29-34	63-68
Statistical Summary	35	69
Statistics (neutrons that enter graphite)	36	70
Initial values ( $z$ , $\cos \psi$ )	37	71



## Geometry



Planes  $z = 0$  and  $z = z_B$  are assumed to be planes of symmetry and treated as reflecting boundaries.

FIGURE 1

Main (master) Program

01	LBL "MC"	31	XEQ "U2"	(p. 62)
02	"MCE D"	32	RCL 08	
03	000.000	33	LN	
04	SEEKPTA	34	CHS	
05	037.077	35	34	
06	GETRX	36	RCL 02	
07	072.005002	37	+	
08	REGMOVE	38	X < y	
09	LBL 01	39	RCL INC y	
10	069.002002	40	÷	
11	REGMOVE	41	RCL 09	
12	074.016004	42	*	
13	REGMOVE	43	RCL 13	
14	0	44	+	
15	STO 01	45	STO 14	
16	"20 = "	46	XEQ "REF"	(p. 5, 35)
17	PROMPT	47	XEQ "SCN"	(p. 61)
18	STO 13	48	XEQ "SCAT"	(p. 31, 32, 45)
19	XEQ "U2" (p. 62)	49	XEQ "SHOW"	(p. 62)
20	STO 09	50	0.1	
21	X <sup>2</sup>	51	RCL 16	
22	1	52	X > y ?	
23	-	53	GTO 02	
24	CHS	54	GTO 01	
25	SQRT	55	END	
26	STO 10			
27	LBL "NEXT"			
28	LBL 02			
29	XEQ "Σ" (p. 60)			
30	LBL "Z"			

These steps  
are wasted,  
R<sub>10</sub> is never  
recalled in  
this context

Steps 19 - 26 replaced with:

19	"DC"
20	PROMPT
21	STO 09
22	1
23	+
24	2
25	÷
26	STO 02
27	STOP

12-5-83

Note RN

01	<u>LBL "Σ"</u>			36	ISG	30
02	30			37	GTO	08
03	STO 29			38	GTO	09
04	0.1			39	<u>LBL</u>	<u>08</u>
05	RCL 16	E(n)		40	1	
06	X > Y ?			41	ST+	29
07	GTO 03	E(n) is > 0.10		42	RCL	16
08	0			43	RCL	30
09	GTO 06	E(n) is < 0.10		44	Y <sup>X</sup>	
10	<u>LBL 03</u>			45	RCL	30
11	0.3			46	1	
12	RCL 16	E(n)		47	+	
13	X > Y ?			48	X < Y	
14	GTO 04	E(n) > 0.3		49	RCL	Y
15	8			50	*	
16	GTO 06	0.1 < E(n) < 0.3		51	STO	29
17	<u>LBL 04</u>			52	GTO	07
18	1			53	<u>LBL</u>	<u>09</u>
19	RCL 16	E(n)		54	RCL	34
20	X > Y ?			55	STO	36
21	GTO 05	E(n) > 1.0		56	RCL	31
22	16			57	RCL	32
23	GTO 06	1.0 < E(n)		58	+	
24	<u>LBL 05</u>			59	STO	34
25	24			60	RCL	33
26	<u>LBL 06</u>			61	+	
27	35.00002			62	STO	35
28	+			63	END	
29	STO 30					
30	8					
31	+					
32	1000					
33	÷					
34	ST+ 30					
35	<u>LBL 07</u>					

$\Sigma_i$

$\Sigma_c = \Sigma_2$

$\Sigma_H$

$\Sigma_0$

$\Sigma_H + \Sigma_0$

$\Sigma_1$

at step 26, the x register contains one of the following numbers: 0, 8, 16, 24.

Macroscopic Cross Sections From the "Burn Bank"  
BNL - 325 (1958)

E (mev)	cross sections, barns			
	H	O	Al	C
0.03	17	3.5	1.2	4.60
0.1	12.6	3.5	3.6	4.50
0.3	7.93	3.5	3.6	3.60
1.0	4.25	3.5	3.4	2.60
3.0	2.77	2.8	2.55	1.45

macroscopic cross sections ( $\text{cm}^{-1}$ )

E (mev)	H	O	Al	C
0.03	0.7526	0.0775	0.0244	0.3692
0.1	0.5578	"	0.0733	0.3612
0.3	0.3511	"	0.0733	0.2290
1.0	0.1981	"	0.0692	0.2087
3.0	0.1002	0.0117	0.0519	0.1164

These are fitted with an equation  $\Sigma = aE^b$ .

E	H		O		Al		C		
	b	a	b	a	b	a	b	a	
0.03 - 0.10	-0.249	0.3144	0	0.0775	0.914	0.6014	-0.018	0.3465	14
0.10 - 0.30	-0.421	0.2115	0	0.0775	0	0.0733	-0.203	0.2265	20
0.30 - 1.00	-0.518	0.1881	0	0.0775	-0.042	0.0692	-0.270	0.2087	21
1.0 - 3.0	-0.571	0.1881	-1.344	0.0775	-0.262	0.0692	-0.531	0.2087	17

The values are stored in registers 37 thru 68 by row.

E	Register Allocation					
0.03 - 0.10	R37	R38	R39	...	R44	in sequence b, a, b, a
0.10 - 0.30	R45	R46				"
0.30 - 1.00	R53					"
1.00 - 3.0	R61	R62	R63	...	R68	"

For a given E, a block of eight registers is treated sequentially, calculating  $\Sigma_H$ ,  $\Sigma_O$ ,  $\Sigma_{Al}$ ,  $\Sigma_C$ ,  $\Sigma_H + \Sigma_O$ ,  $\Sigma_1 = \Sigma_H + \Sigma_O + \Sigma_{Al}$ , and  $\Sigma_2 = \Sigma_1$ .

REF/SIJ (Reflect - convert)

This is the same scheme  
illustrated on page 5.

01	<u>LBL</u>	<u>REF</u>
02	<u>LBL</u>	6
03	RCL	14
04	RCL	05
05	-	
06	SIGN	
07	3	
08	+	
09	2	
10	÷	

11	STO	03	Region of Scat.
12	RCL	02	Region of Orig.
13	-		
14	$x = 0 ?$		
15	GTO	05	same region
16	<u>LBL</u>	<u>SIJ</u>	
17	RCL	35	$Z_1$
18	RCL	36	$Z_2$
19	÷		$Z_1/Z_2$
20	$x < 0 ?$		$n, Z_1/Z_2$

21	$\frac{y}{x}$		$(Z_1/Z_2)^n$
22	RCL	14	$z'$
23	RCL	05	$z_1$
24	-		$z' - z_1$
25	*		$(z' - z_1)(Z_1/Z_2)^n$
26	RCL	05	
27	+		
28	STO	14	corrected $z'$
29	<u>LBL</u>	<u>05</u>	
30	RCL	14	

31	$x > 0 ?$	
32	GTO	06
33	CHS	
34	STO	14
35	GTO	08
36	<u>LBL</u>	<u>06</u>
37	RCL	06
38	RCL	14
39	-	
40	$x > 0 ?$	

41	GTO	09
42	<u>LBL</u>	<u>07</u>
43	RCL	06
44	+	
45	STO	14
46	<u>LBL</u>	<u>08</u>
47	-1	
48	ST*	09
49	$\alpha R \alpha$	
50	AVIEW	

51	STOP	
52	GTO	6
53	<u>LBL</u>	<u>09</u>
54	RCL	03
55	STO	02
56	RCL	14
57	STO	13
58	RTN	
59	END	

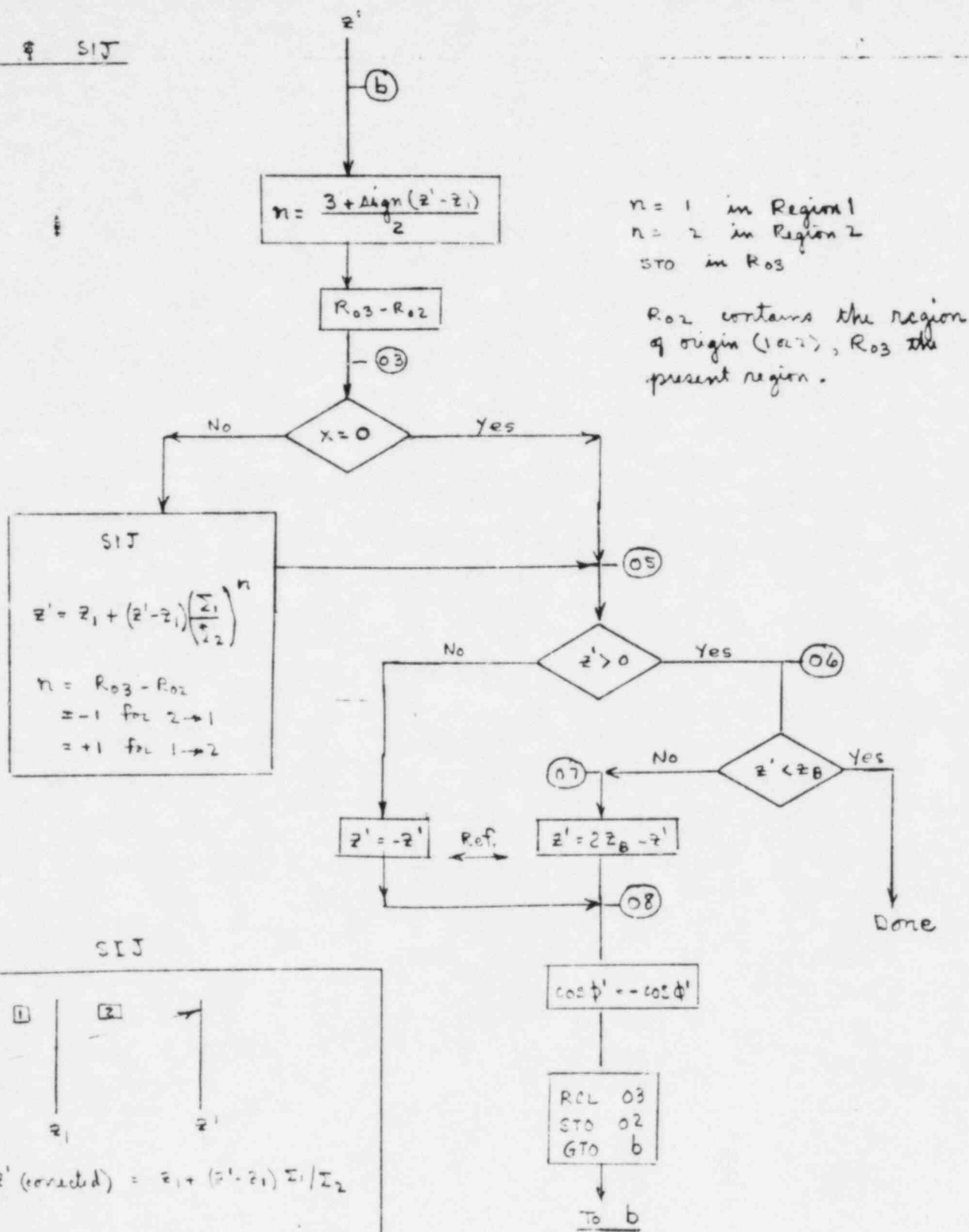
 $z_B$  $z'$  $z_B - z'$  $2z_B - z'$ 

reverse dir.

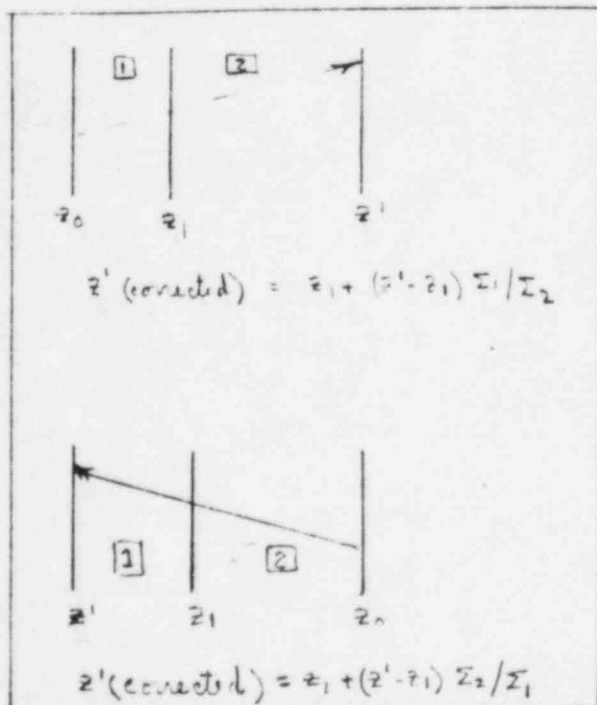
note reflect (R).

Done

REF &amp; SIJ



SIJ



~~Page~~

SCN (identify scatterer; H, O, Al, or C. If the neutron is in Region 2, the scatterer is C, otherwise a decision is required).

01	<u>LBL</u>	"SCN"		31	27	
02	RCL	02		32	GTO	04
03	2			33	<u>LBL</u>	03
04	$x = y?$			34	"C = 12"	
05	GTO	03	(graphite)	35	ASTO	00
06	XEQ	UZ		36	12	
07	RCL	31		37	<u>LBL</u>	04
08	RCL	35		38	STO	04
09	$\div$			39	END	
10	RCL	08	$0 < N_i < 1$			A = 1 or 12 or 16 or 27
11	$x > y?$		$N_i > Z_H/Z_1?$			
12	GTO	01	yes, not H			
13	"H = 1"		no, it is H			
14	ASTO	00				
15	1					
16	GTO	04				
17	<u>LBL</u>	01				
18	RCL	34	$Z_H + Z_0$			
19	RCL	35	$Z_1$			
20	$\div$					
21	RCL	08				
22	$x > y?$		$N > (Z_H + Z_0)/Z_1$			
23	GTO	02	yes, Not O			
24	"O = 16"					
25	ASTO	00				
26	16					
27	GTO	04				
28	<u>LBL</u>	02				
29	"Al = 27"					
30	ASTO	00				



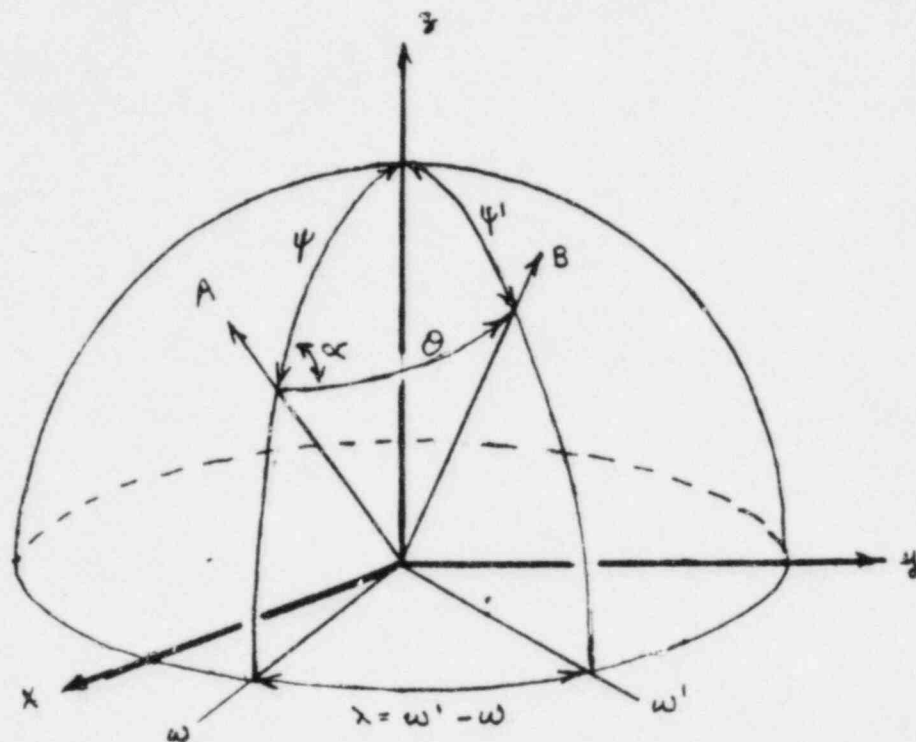
# SCAT (Scatter, Energy and New $\cos \psi$ )

01	LBL	SCAT	
02	XEQ	U2	$\cos \phi$
03	RCL	07	
04	RCL	04	A
05	*		$A \cos \phi$
06	2		
07	*		$2 A \cos \phi$
08	1		
09	+		$1 + 2 A \cos \phi$
10	RCL	04	A
11	X <sup>2</sup>		$A^2$
12	+		
13	STO	15	$1 + A^2 + 2 A \cos \phi$
14	1		
15	RCL	04	A
16	+		$1 + A$
17	X <sup>2</sup>		$(1 + A)^2$
18	÷		$E/E_0$ (p.32)
19	RCL	16	$E_0$
20	*		E
21	STO	17	E
22	RCL	16	$E_0$
23	-		
24	RCL	02	Region (1 or 2)
25	17		
26	+		
27	X $\Delta \psi$		
28	ST+ .4		Accumulate $\Delta E$
29	RCL	17	
30	STO	16	New E
31	LBL	THETA	
32	RCL	07	$\cos \phi$
33	RCL	04	A
34	*		$A \cos \phi$
35	1		

36	+		
37	RCL	15	
38	SQRT		
39	÷		$\cos \theta$
40	STO	10	$\cos \theta$ (p.31)
41	XEQ	U2	(for azimuths)
42	180		
43	*		( $\alpha$ = azim. deg)
44	cos		$\cos \alpha$ (p.32)
45	1		
46	RCL	10	$\cos \theta$
47	X <sup>2</sup>		
48	-		
49	1		
50	RCL	09	$\cos \psi$
51	X <sup>2</sup>		
52	-		
53	*		
54	SQRT		$\sin \theta \sin \psi$
55	*		$\sin \theta \sin \psi \cos \alpha$
56	RCL	10	$\cos \theta$
57	RCL	09	$\cos \psi$
58	*		
59	+		$\cos \psi'$ (new)
60	STO	09	
61	END		

Calculated new  $\cos \psi$  in the stack.

# THREE DIMENSIONAL SCATTERING



The neutron, initially moving in direction A, is scattered through polar angle  $\Theta$  at azimuth  $\alpha$  into direction B. The direction cosines:

Before scattering

$$\begin{aligned} u_x &= \sin \psi \cos \omega \\ u_y &= \sin \psi \sin \omega \\ u_z &= \cos \psi \end{aligned}$$

After scattering

$$\begin{aligned} u'_x &= \sin \psi' \cos \omega' \\ u'_y &= \sin \psi' \sin \omega' \\ u'_z &= \cos \psi' \end{aligned}$$

For isotropic scattering in a center-of-mass coordinate system, let  $\cos \phi$  be the polar angle uniformly distributed,  $-1 < \cos \phi < 1$ , and  $\alpha$  will be uniformly distributed  $-\pi < \alpha < \pi$ . With A representing the mass of the scattering nucleus, the polar scattering angle in the laboratory coordinate system is

$$\cos \Theta = \frac{1 + A \cos \phi}{\sqrt{A^2 + 1 + 2A \cos \phi}}$$

The post scattering direction cosines, in terms of the scattering angles  $\theta$  and  $\alpha$  are calculated by:

$$u_z = \cos \psi' = \cos \psi \cos \theta + \sin \psi \sin \theta \cos \alpha$$

$$\sin \lambda = \sin \theta \cdot \sin \alpha / \sin \psi'$$

$$\cos \lambda = (\cos \theta - \cos \psi \cos \psi') / \sin \psi \sin \psi'$$

$$\sin \omega' = \sin(\omega + \lambda) = \sin \omega \cos \lambda + \cos \omega \sin \lambda$$

$$\cos \omega' = \cos(\omega + \lambda) = \cos \omega \cos \lambda - \sin \omega \sin \lambda$$

The  $u_x$  and  $u_y$  direction cosines can be calculated from these components. However, we shall track only the motion in  $z$  and need only  $u_z$ . Note that  $0 < \psi' < \pi$ ,  $\sin \psi' \geq 0$ , and hence

$$\sin \psi' = \sqrt{1 - \cos^2 \psi'}$$

The procedure is to choose a random number  $N$  from a uniformly distributed population,  $-1 < N < 1$  and

$$\cos \phi = N$$

$$\cos \theta = \frac{1 + A \cdot N}{\sqrt{1 + A^2 + 2AN}}$$

$$\sin \theta = \frac{A \sqrt{1 - N^2}}{\sqrt{1 + A^2 + 2AN}} = \sqrt{1 - \cos^2 \theta} \geq 0$$

$$\cos \psi' = \cos \psi \cos \theta + \sin \psi \sin \theta \cos \alpha$$

where  $\alpha$  is a random number uniformly distributed over  $-\pi, \pi$  ( $\alpha = 180, 180$  deg).

The post-collision Energy (Soodak & Campbell, Pg. 6, Eq 3-2)

$$\frac{E}{E_0} = \frac{1 + A^2 + 2A \cos \phi}{(1 + A)^2}$$

$$A = m/m$$

SHOW (Display Output)

01	LBL	"SHOW"	
02	BEEP		
03	I		
04	ST+	01	
05	VIEW	01	collision No.
06	STOP		
07	VIEW	00	A = A
08	STOP		
09	VIEW	18	E <sub>1</sub>
10	STOP		
11	VIEW	19	E <sub>2</sub>
12	STOP		
13	VIEW	13	z
14	STOP		
15	RCL	09	cos $\psi'$
16	ACOS		$\psi'$
17	STOP		
18	VIEW	16	E(n)
19	STOP		
20	VIEW	08	N
21	STOP		
22	EXEQ	"U2"	
23	END		

U2 (generates Random Numbers)

01	LBL	"U2"	
02	RCL	08	N <sub>i</sub>
03	Z3		
04	*		
05	↑		
06	INT		
07	10 <sup>8</sup>		
08	÷		
09	-		
10	FRC		$0 < N_{i+1} < 1$
11	STO	08	
12	Z		
13	*		
14	I		
15	-		
16	STO	07	
17	END		

Monte Carlo Program (11-20-83)Register Assignments

R 00		R 70	Region (initially)
R 01	n : collision no	R 71	0 (initially)
R 02	Region of origin, 1 or 2	R 72	6.35 boundary
R 03	Region of event, 1 or 2	R 73	21.6 boundary
R 04	A = Scat. Mass (1, 12, 16, 27)	R 74	2 E(n=0) Reg. 1
R 05	$z_1 = 6.35$ cm	R 75	2 E(n=0) Reg. 2
R 06	$z_B = 21.6$ cm	R 76	0 0 $\Delta E_1$
R 07	$\cos \phi$	R 77	0 0 $\Delta E_2$
R 08	N		
R 09	$\cos \psi$		
R 10	$\cos \theta$		
R 11	Not used		
R 12	Not used		
R 13	Z		
R 14	Z'		
R 15	$1 + A^2 + 2A \cos \phi$		
R 16	$E_0$		
R 17	E		
R 18	$\Delta E_1$		
R 19	$\Delta E_2$		
R 20 - R 28	Not used		
R 29	Index Address (in "Z")		
R 30	ISG (in "Z")		
R 31	$\Sigma_H$		
R 32	$\Sigma_0$		
R 33	$\Sigma_{AL}$		
R 34	$\Sigma_C, \Sigma_H + \Sigma_0$		
R 35	$\Sigma_1 = \Sigma_H + \Sigma_0 + \Sigma_{AL}$		
R 36	$\Sigma_2 = \Sigma_C$		
R 37 - R 48	constants for $\Sigma(E)$		
R 49	1 Region (initially)		

	$z_0$	Ni	n	A	$\Delta E_1$	$\Delta E_2$	z	y	E
1	5.715	0.490	1	27	-0.251	0.000	2.37	98	1.749
		0.621	2	16	-0.559		1.67	67	1.441
		0.521	3	16	-0.599		1.69	86	1.401
		0.297	4	1	-1.529		1.74	82	0.471
		0.383	5	1	-1.740		1.81	74	0.260
		0.073	6	1	-1.807		2.01	101	0.193
		0.418	7	1	-1.890		1.84	128	0.110
		0.636	8	1	-1.982		1.44	110	0.018
					<u>-2.000</u>	<u>0.000</u>			
2	4.445	0.617	1	1	-0.168	0.000	2.90	142	1.832
		0.684	2	16	-0.380		1.80	126	1.620
		0.177	3 R	16	-0.610		4.48	91	1.390
		0.007	4	27	-0.618		4.37	111	1.382
		0.235	5	1	-1.562		3.15	93	0.438
		0.732	6	1	-1.587		3.13	91	0.413
		0.923	7	1	-1.750		3.08	121	0.250
		0.917	8	1	-1.875		0.79	76	0.125
		0.067	9	1	-1.948		1.02	56	0.052
		0.894	10	1	-1.987		1.43	21	0.033
		0.952	11	1	-1.990		1.55	51	0.010
					<u>-2.000</u>	<u>0.000</u>			
3	3.175	0.803	1	27	-0.167		3.10	149	1.833
		0.918	2 R	1	-1.837		5.26	102	0.163
		0.389	3	1	-1.856		5.24	99	0.144
		0.157	4	1	-1.931		5.11	133	0.069
		0.532	5	1	-1.977		3.79	77	0.023
					<u>-2.000</u>	<u>0.000</u>			
4	1.905	0.407	1	27	-0.197		0.36	26	1.803
		0.575	2	1	-0.844		6.29	44	1.156
		0.750	3	12	"	-0.127	11.49	109	1.029
		0.101	4	12		-0.355	9.70	130	0.801
		0.031	5	12		-0.540	8.68	36	0.617
		0.374	6	12		-0.549	10.38	51	0.608
		0.827	7	12		-0.650	20.90	44	0.507
		0.520	8	12		-0.665	21.04	11	0.491
		0.531	9 R	12		-0.671	16.21	167	0.486
		0.081	10	12		-0.691	15.65	128	0.465
		0.614	11	12		-0.692	10.75	130	0.464
		0.787	12	1	-1.053	-0.692	5.49	98	0.255
		0.635	13	16	-1.055	-0.692	5.36	110	0.253

$z_0$	$N_i$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$y$	$E$
1.905	0.138	14	1	-1.208	-0.692	4.23	127	0.090
	0.163	15	1	-1.262	"	4.00	102	0.046
	0.685	16	1	<u>-1.301</u>	<u>"</u>	3.93	60	0.007
				-1.308	-0.692			

5	0.635	0.369	1R	27	-0.232	0.000	1.63	83	1.768
		0.640	2	1	-1.523		1.82	100	0.477
		0.204	3	16	-1.577		1.66	62	0.423
		0.329	4	1	-1.641		2.23	40	0.359
		0.481	5	12	-1.641	-0.060	7.13	65	0.298
		0.393	6	12	"	-0.080	12.04	62	0.279
		0.702	7	12	"	-0.151	15.23	124	0.207
		0.195	8	12	"	-0.155	13.91	96	0.203
		0.465	9	12		-0.205	13.79	71	0.154
		0.304	10	12		-0.246	19.84	133	0.112
		0.061	11	12		-0.268	18.08	56	0.090
		0.338	12	12		-0.292	18.46	119	0.066
		0.255	13	12		-0.293	18.27	111	0.065
		0.716	14	12		-0.296	17.54	114	0.062
		0.214	15	12		-0.311	17.45	37	0.048
		0.387	16	12		-0.311	17.66	59	0.047
		0.015	17	12		-0.324	19.14	155	0.035
		0.958	18	12		-0.328	9.78	121	0.030
		0.976	19	12	<u>-1.641</u>	<u>-0.333</u>	8.66	126	0.025
					-1.641	-0.359			

6	5.715	0.878	1	1	-0.742	0.000	3.13	91	1.258
		0.464	2	1	-1.086	"	3.09	84	0.914
		0.710	3	1	-1.239	"	3.46	96	0.761
		0.164	4	1	-1.683	"	3.38	53	0.317
		0.575	5	1	-1.885	"	5.25	42	0.115
		0.353	6	12	"	-0.016	8.94	95	0.099
		0.792	7	12	"	-0.022	8.55	119	0.093
		0.157	8	12	"	-0.025	7.87	85	0.090
		0.441	9	12	"	-0.043	8.35	81	0.072
		0.717	10	12	"	-0.056	8.66		0.059
		0.563	11	12	"	-0.057	8.78	48	0.058
		0.853	12	12	"	-0.073	9.69	138	0.042
		0.066	13	12	"	-0.076	8.32	146	0.039
		0.890	14	12	"	-0.078	6.62	107	0.037
		0.589	15	1	<u>-1.919</u>	<u>-0.078</u>	6.25	134	0.003
					-1.919	-0.081			



	<u>Z<sub>0</sub></u>	<u>N<sub>i</sub></u>	<u>n</u>	<u>A</u>	<u>ΔE<sub>1</sub></u>	<u>ΔE<sub>2</sub></u>	<u>z</u>	<u>Y</u>	<u>E</u>
7	4.445	0.866	1	12	0.000	-0.073	13.89	71	1.927
		0.040	2	12	0.000	-0.403	14.05	130	1.597
		0.138	3	12	"	-0.434	7.01	104	1.566
		0.439	4	1	-0.222	"	4.58	102	1.344
		0.743	5	1	-0.477	"	2.80	85	1.090
		0.641	6	27	-0.483	"	2.88	108	1.023
		0.011	7	16	-0.714	"	1.48	91	0.853
		0.893	8	1	-0.721	"	1.45	93	0.846
		0.814	9	16	-0.747	"	1.40	86	0.819
		0.725	10	16	-0.802	"	1.47	145	0.764
		0.048	11 R	16	-0.937	"	3.45	110	0.630
		0.714	12	27	-0.957	"	2.70	59	0.609
		0.567	13	12	"	-0.581	6.92	79	0.462
		0.405	14	12	"	-0.656	7.75	128	0.387
		0.855	15	12	"	-0.729	6.83	65	0.314
		0.693	16	12	"	-0.763	6.92	89	0.280
		0.228	17	12	"	-0.797	6.99	66	0.246
		0.317	18	12	"	-0.814	8.62	46	0.229
		0.356	19	12	"	-0.852	12.37		0.191
		0.564	20	12	"	-0.890	12.43		0.153
		0.026	21	12	"	-0.892	11.01	134	0.151
		0.575	22	12	"	-0.936	7.85	62	0.113
		0.761	23	12	"	-0.947	8.78	46	0.095
		0.395	24	12	"	-0.948	13.46	51	0.095
		0.943	25	12	"	-0.956	14.12	70	0.087
		0.734	26	12	"	-0.971	14.24	96	0.072
		0.760	27	12	"	-0.973	14.01	90	0.070
		0.715	28	12	"	-0.986	13.99	149	0.056
		0.932	29	12	"	-0.988	12.01	118	0.055
		0.600	30	12	"	-0.997	11.73	148	0.046
		0.030	31	12	"	-1.009	10.89	57	0.033
		0.961	32	12	-0.957	-1.015	14.20	107	0.028
					-0.957	-1.043			

8	3.175	0.800	1	27	-0.135	0.000	0.04	73	1.865
		0.700	2	1	-0.143		3.10	76	1.857
		0.908	3	1	-1.285		3.22	108	0.715
		0.853	4	1	-1.703		2.82	61	0.297
		0.553	5	16	-1.758		3.15	81	0.242
		0.626	6	27	-1.782		3.40	72	0.218
		0.685	7	1	-1.813		3.55	76	0.187

	<u>Z</u>	<u>N<sub>2</sub></u>	<u>n</u>	<u>A</u>	<u>ΔE<sub>1</sub></u>	<u>ΔE<sub>2</sub></u>	<u>Z</u>	<u>P</u>	<u>E</u>
	cont	0.770	8	1	-1.821	0.000	3.70	87	0.179
		0.921	9	1	-1.927	"	3.83	41	0.073
		0.447	10	1	<u>-1.984</u>	<u>0.000</u>	5.15	97	0.016
					-2.000	0.000			
9	1.905	0.902	1	1	-1.079	0.000	2.05	30	0.921
		0.590	2	27	-1.096	"	3.56	67	0.904
		0.842	3	16	-1.280	"	4.26	138	0.720
		0.895	4	1	-1.891	"	3.18	71	0.109
		0.475	5	1	-1.941	"	3.21	29	0.059
		0.506	6	1	-1.958	"	3.75	10	0.042
		0.447	7	1	<u>-1.979</u>	<u>0.000</u>	5.33	43	0.021
					-2.000				
10	0.635	0.301	1	1	-0.280	0.000	3.87	40	1.728
		0.780	2	16	-0.594	"	4.06	167	1.406
		0.014	3R	1	-1.397	"	0.18	59	0.603
		0.875	4	27	-1.478	"	2.97	109	0.522
		0.385	5	1	-1.565	"	2.83	117	0.435
		0.186	6	1	-1.632	"	1.49	95	0.368
		0.441	7	1	-1.755	"	1.12	76	0.245
		0.342	8	27	-1.759	"	1.19	102	0.241
		0.142	9	27	-1.787	"	0.65	47	0.213
		0.386	10	1	-1.900	"	0.81	68	0.100
		0.779	11	1	-1.935	"	0.86	103	0.065
		0.043	12	1	-1.958	"	0.85	80	0.042
		0.646	13	1	-1.962	"	0.89	95	0.038
		0.073	14	1	<u>-1.986</u>	"	0.85	44	0.014
					-2.000				

Summary 1st 10 neutrons, 20 meV

$\Sigma \Delta E_1 =$	17.716 meV	88.6%
$\Sigma \Delta E_2 =$	2.118 meV	10.6%
Remaining K.E.	<u>0.165</u> meV	0.8%
	19.999	

number of collisions = 137  
 lethargy =  $\ln(2/0.00835) = 2.495$   
 $\bar{n} = 137/10 = 13.7$   
 $\bar{\xi} = 0.57$

For the next set, add XEA UZ prior to RTN1 in  
 "SHOW" format - to further isolate successive cycles.  
 The first N is 0.53391624

p.18

$\Sigma$	N	A	$\Delta E_1$	$\Delta E_2$	$\Sigma$	4	E
5.715	0.534	1	-0.694	0.000	4.04	152	1.306
0.020	2	27	-0.753	"	0.65	85	1.247
0.442	3	1	-0.814	"	0.72	94	1.186
0.870	4	1	-1.179	"	0.18	123	0.821
0.919	5 R	1	-1.262	"	1.39	52	0.738
0.693	6	1	-1.803	"	2.77	99	0.197
0.129	7	1	-1.942	"	2.13	102	0.058
0.773	8	1	-1.968	"	1.67	60	0.032
0.512	9	1	-1.975	0.000	1.76	39	0.025
0.405	1	1	-1.618	0.000	4.47	45	0.382
0.394	2	1	-1.845	"	6.18	37	0.155
0.358	3	12	-1.845	-0.015	7.89	101	0.140
0.077	4	12	"	-0.043	7.85	128	0.113
0.123	5	12	"	-0.045	7.60	100	0.111
0.467	6	12	"	-0.063	7.59	32	0.092
0.411	7	12	"	-0.081	9.25	97	0.074
0.287	8	12	"	-0.082	8.38	96	0.074
0.262	9	12	"	-0.091	8.34	158	0.064
0.940	10	16	-1.851	-0.091	5.99	106	0.058
0.796	11	16	-1.861	"	5.45		0.048
0.602	12	12	-1.861	-0.100	7.58	68	0.039
0.511	13	12	"	-0.107	8.49	34	0.032
-	14	12	-1.861	-0.110	14.35	26	0.029
0.503	1	27	-0.158	0.000	2.96	117	1.842
0.838	2	1	-0.613	"	0.55	103	1.387
0.313	3	27	-0.776	"	0.29	52	1.224
0.363	4	1	-1.952	"	0.34	121	0.048
0.908	5 R	1	-1.998	"	0.93	135	0.002
0.033	1	1	-0.342	0.000	1.55	131	1.658
0.062	2	1	-1.360	"	0.76	148	0.690
0.883	3 R	16	-1.395	"	2.33	58	0.605
0.272	4	27	-1.424	"	2.33	124	0.576
0.936	5	1	-1.615	"	2.23	98	0.385

(c)

$z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$y$	$E$
cont.	0.365	6	1	-1.642	0.060	1.33	85	0.358
	0.431	7	1	-1.935	"	2.29	106	0.065
	0.193	8	1	-1.993	0.000	1.77	73	0.007
				-2.000	0.000			
0.635	0.319	1	1	-1.116	0.000	4.54	85	0.884
	0.168	2	27	-1.124	"	4.54	57	0.876
	0.451	3	1	-1.169	"	6.30	63	0.831
	0.813	4	12	-1.169	-0.049	9.12	86	0.782
	0.199	5	12	"	-0.229	10.02	53	0.602
	0.392	6	12	"	-0.310	11.56	123	0.521
	0.104	7	12	"	-0.312	7.09	117	0.519
	0.677	8	1	-1.525	-0.312	4.95	106	0.163
	0.245	9	1	-1.636	"	4.58	83	0.052
	0.308	10	1	-1.680	-0.312	4.64	21	0.008
				-1.688	-0.312			

Summary, 1st 15 neutrons, 30 meV

	<u>1st 5</u>	<u>2nd 5</u>	<u>3rd 5</u>	<u>Total</u>	
$\Delta E_1$	8.891	8.825	9.507	27.223	90.7%
$\Delta E_2$	1.025	1.093	0.422	2.540	8.5%
Residual	0.083	0.082	0.071	0.236	0.8%
	9.999	10.000	10.000	29.999	100.0%

Total no of collisions: 183

$$\begin{aligned} \text{ave lethargy from 2 meV} &= \ln(30/0.236) = 4.845 \\ \bar{\xi} &= \text{lthargy per collision } (183/15 = 12.2 \text{ coll/neut}) \\ &= 0.397 \end{aligned}$$

we had  $\bar{\xi} = 0.408$  for the isotropic case with 40 neutrons.

Programs ENER & SLC combined into one program named SCAT. minor modifications required in MC and SCN. 7-8-83

	$z_0$	$N$	$n$	$A$	$AE_1$	$AE_2$	$z$	$y$	$E$	$p.20$
16	5.715	0.950	1	H	-1.103	0.000	1.53	84	0.297	
		0.321	2	H	-1.854	"	1.59	88	0.146	
		0.751	3	H	-1.956	"	1.63	144	0.044	
					-2.000	0.000			-	
17	5.715	0.550	1	AL	-0.124	0.000	5.79	41	1.876	
		0.615	2	C	-0.124	-0.085	16.02	45	1.790	
		0.310	3 <sup>R</sup>	C	"	-0.401	20.44	76	1.474	
		0.721	4	C	"	-0.557	21.08	28	1.318	
		0.419	5 <sup>R</sup>	C	"	-0.563	20.64	143	1.313	
		0.658	6	C	"	-0.916	7.00	48	0.960	
		0.232	7	C	"	-1.021	7.50	100	0.855	
		-	8	C	"	-1.082	7.35	118	0.794	
		0.182	9	AL	-0.128	"	3.12	115	0.790	
		0.240	10	H	-0.529	"	0.40	90	0.389	
		0.328	11	O	-0.611	"	0.41	113	0.307	
		0.086	12 <sup>R</sup>	AL	-0.627	"	0.42	21	0.291	
		0.442	13	AL	-0.652	"	0.99	84	0.266	
		0.566	14	O	-0.710	"	1.24	82	0.208	
		0.410	15	H	-0.804	"	1.35	44	0.114	
		0.558	16	H	-0.908	"	1.42	111	0.010	
					-0.918	-1.082			-	
18	5.715	0.300	1	C	0.000	-0.511	7.38	120	1.489	
		0.299	2	AL	-0.130	"	4.40	25	1.359	
		0.442	3	O	-0.367	"	4.92	137	1.122	
		0.869	4	I	-1.361	"	3.78	134	0.188	
		0.857	5	I	-1.484	"	3.04	58	0.005	
					-1.489	-0.511			-	
19	5.715	0.700	1	AL	-0.083	0.000	1.23	148	1.917	
		0.055	2 <sup>R</sup>	C	"	-0.260	10.69	114	1.657	
		0.031	3	C	"	-0.632	9.66	99	1.285	
		0.827	4	C	"	-0.838	9.26	167	1.079	
		0.928	5	C	"	-1.039	7.29	88	0.878	
		0.928	6	C	"	-1.203	7.76	122	0.714	
		0.841	7	C	"	-1.247	7.53	171	0.670	
		0.025	8 <sup>R</sup>	AL	-0.104	-1.247	3.36	61	0.649	
		0.860	9	O	-0.138		3.43	7	0.615	
		0.488	10	C	-0.138	-1.392	13.99	133	0.470	

(cont)

$z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$y$	$E$
5.715	0.963	11	C	-0.138	-1.396	9.87	142	0.465
(cont)	0.151	12	C	"	-1.518	9.45	57	0.393
	0.798	13	C		-1.587	9.60	130	0.275
	0.848	14	C		-1.651	8.97	103	0.210
	0.016	15	C		-1.677	8.63	157	0.125
	0.067	16	O	-0.162	"	5.42	79	0.161
	0.710	17	O	-0.184	"	5.72	153	0.139
	-	18	H	-0.309		3.76	93	0.014
				-0.323	-1.677			

20	5.715	0.150	1	H	-1.701	0.000	5.23	35	0.299
		0.440	2	H	-1.784	"	5.32	17	0.216
		0.584	3	H	-1.906	"	5.64	66	0.094
					-2.000	0.000			-

21	5.715	0.850	1	AL	-0.042	0.000	5.92	40	1.958
		0.495	2 <sup>R</sup>	C		-0.441	15.84	67	1.517
		0.753	3	C		-0.855	21.59	136	1.103
		0.933	4	C		-1.092	19.85	25	0.866
		0.557?	5 <sup>R</sup>	C		-1.165	21.19	123	0.793
		0.199	6	C		-1.249	14.65	55	0.709
		0.450	7	C		-1.258	14.77	74	0.700
		-	8	C		-1.264	16.37	63	0.694
		0.371	9	C		-1.278	17.68	41	0.680
		0.403	10	C		-1.405	20.28	107	0.553
		0.776	11	C		-1.446	19.67	158	0.512
		0.048	12	C		-1.466	14.61	138	0.492
		0.774	13	C		-1.598	13.17	22	0.360
		0.410	14	C		-1.695	13.31	141	0.263
		0.121	15	H	-0.178	-1.695	3.19	146	0.127
		0.118	16	O	-0.201	"	2.63	52	0.104
		0.298	17	O	-0.203		2.81	47	0.102
		0.685	18	AL	-0.207		3.37	68	0.098
					-0.305	-1.695			

$\Sigma \Delta E's$ , 6 samples  
at  $z_0 = 5.715$

$\Delta E_1$	$\Delta E_2$
7.035	4.965

	<u>z<sub>0</sub></u>	<u>N</u>	<u>n</u>	<u>A</u>	<u>ΔE<sub>1</sub></u>	<u>ΔE<sub>2</sub></u>	<u>z</u>	<u>ψ</u>	<u>E</u>
22	4.445	0.430	1	C	0.000	-0.108	7.59	33	1.893
		0.629	2	C	"	-0.339	10.18	105	1.661
		0.093	3	O	-0.031	-0.339	6.12	136	1.629
		0.037	4	H	-1.393	-0.339	3.72	113	0.267
		0.774	5	O	-1.431	"	2.82	90	0.229
		0.236	6	H	-1.612	"	2.82	130	0.049
					-1.661	-0.339			
23	4.445	0.570	1	H	-1.263	0.000	2.14	89	0.737
		0.473	2	O	-1.370		2.18	114	0.629
		0.818	3	H	-1.968	0.000	2.14	122	0.032
					2.000	0.000			
24	4.445	0.290	1	H	-0.222	0.000	5.86	52	1.778
		0.451	2	C	-0.222	-0.309	6.74	142	1.469
		0.927	3	AL	-0.410	-0.309	4.85	29	1.281
		0.640	4	C	"	-0.540	7.39	75	1.051
		0.429	5	C	"	-0.821	7.64	97	0.769
		0.288	6	C	"	-1.001	7.10	131	0.589
		0.071	7	H	-0.675	-1.001	5.74	98	0.324
		0.630	8	H	-0.839		5.22	66	0.160
		0.376	9	C	-0.839	-1.017	7.53	106	0.145
		0.162	10	C	"	-1.057	7.45	60	0.105
		0.629	11	C	"	-1.076	7.56	77	0.085
					-0.924	-1.076			
25	4.445	0.710	1	H	-1.784	0.000	3.61	39	0.216
		0.484	2	H	-1.882		5.89	15	0.118
		0.563	3	AL	-1.894		5.89	129	0.106
		0.894	4	H	-1.930		5.65	123	0.070
					-2.000	0.000			
26	4.445	0.160	1	O	-0.195	0.000	5.19	124	1.805
		0.870	2 <sup>R</sup>	O	-0.501		1.27	68	1.499
		0.423	3	H	-1.005		1.96	71	0.995
		0.258	4	AL	-1.016		3.02	74	0.984
		0.250	5	H	-1.501		3.86	53	0.499
		0.649	6	AL	-1.534		4.79	136	0.466
		0.958	7	H	-1.722		4.53	119	0.278
		0.721	8	H	-1.937		3.87	120	0.063
					-2.000	0.000			



$z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$\psi$	$E$
4.445	0.840	1	H	-1.125	0.000	2.73	151	0.875
	0.066	2	H	-1.792		2.41	91	0.208
	0.469	3	O	-1.827		2.36	58	0.173
	0.353	4	H	-1.896		2.58	78	0.104
	0.814	5	H	-1.958		2.84	40	0.042
				-2.000	0.000			

$\Sigma \Delta E$ 's, 6 samples

@  $z_0 = 4.445$

10.585 1.415

Initial  $N$ 's

$z_0 = 5.715$	0.15	0.30	0.45	0.55	0.70	0.85
4.445	0.16	0.29	0.43	0.57	0.71	0.84
3.175	0.14	0.28	0.42	0.58	0.72	0.86
1.905	0.11	0.27	0.41	0.59	0.73	0.89
0.635	0.08	0.25	0.417	0.583	0.75	0.92

$z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$\psi$	$E$
3.175	0.140	1 <sup>R</sup>	H	-0.521	0.000	4.16	87	1.479
	0.011	2	O	-0.781		4.21	90	1.219
	0.745	3	AL	-0.914		4.15	83	1.086
	0.726	4	H	-0.987		4.24	68	1.013
	0.469	5	C		-0.112	7.80	134	0.902
	0.068	6	O	-1.115		1.89	92	0.773
	0.205	7	H	-1.459		1.80	97	0.429
	0.772	8	AL	-1.485		1.54	72	0.403
	0.698	9	H	-1.730		4.60	123	0.158
	0.028	10	H	-1.842	-0.112	4.39	114	0.047
				-1.888	-0.112			
3.175	0.280	1	H	-0.430		3.98	77	1.570
	0.060	2	H	-1.003		4.61	50	0.997
	0.603	3	C		-0.024	9.96	81	0.973
	0.013	4	C		-0.256	12.14	78	0.741
	0.684	5	C		-0.367	14.69	160	0.631
	0.960	6	C		-0.537	13.73	46	0.460
	0.050	7	C		-0.659	17.78	103	0.338
	0.568	8	C		-0.670	17.26	71	0.327
	0.414	9	C		-0.697	20.19	103	0.300

$z_0$	$N$	$n$	$r$	$\Delta E_1$	$\Delta E_2$	$z$	$y$	$E$
3.175	0.177	10	C	-1.003	-0.715	19.95	64	0.283
(cont)	0.392	11	C		-0.735	21.39	120	0.262
	0.032	12	C		-0.768	20.93	127	0.229
	0.851	13	C		-0.769	20.80	112	0.228
	0.545	14	C		-0.819	19.95	74	0.178
	0.264	15	C		-0.850	20.73	158	0.147
	0.941	16	C		-0.892	19.73	30	0.105
	0.051	17	C	-1.003	-0.921	20.07	147	0.076
				-1.003	-0.997			

30	3.175	0.420	1	H	-1.562	0.000	5.73	132	0.438
		0.033	2	H	-1.729		4.47	125	0.271
		0.235	3	AL	-1.743		2.18	120	0.257
		0.177	4	H	-1.795		1.28	97	0.205
		0.407	5	O	-1.831		0.91	72	0.169
		0.705	6	H	-1.896		1.07	98	0.104
		-	7	H	-1.967		0.69	89	0.033
					-2.000	0.000			

31	3.175	0.580	1	AL	-0.061	0.000	2.88	145	1.939
		0.903	2	AL	-0.100		0.38	112	1.900
		0.657	3 <sup>R</sup>	H	-1.468		0.12	23	0.532
		0.434	4	AL	-1.489		0.82	51	0.511
		0.657	5	H	-1.636		1.65	38	0.364
		0.354	6	H	-1.951		3.89	100	0.049
					-2.000	0.000			

32	3.175	0.720	1	H	-0.964	0.000	3.25	120	1.036
		0.914	2	H	-1.937		1.52	56	0.063
					-2.000	0.000			

33	3.175	0.860	1	O	-0.329	0.000	3.34	155	1.671
		0.925	2 <sup>R</sup>	H	-1.553		4.15	75	0.447
		0.147	3	H	-1.692		4.26	101	0.308
		0.885	4	H	-1.818		3.82	68	0.182
		0.595	5	H	-1.845		4.03	45	0.155
		0.490	6	O	-1.861		5.02	37	0.137
		0.525	7	H	-1.937		5.44	11	0.063
					-2.000	0.000			

$\Sigma \Delta E$ 's = Sample  
at  $z_0 = 3.175$

10.891 1.109

	$z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$z$	$y$	$E$
4	1.905	0.110	1	H	-0.991	0.000	2.37	81	1.019
		0.723	2	O	-1.057		2.79	94	0.943
		0.228	3	H	-1.511		2.71	132	0.489
		0.927	4	H	-1.537		1.56	134	0.463
		0.797	5	H	-1.810		0.80	86	0.190
		0.446	6	Al	-1.830		1.02	63	0.170
		0.396	7	H	-1.994		2.47	103	0.006
					-2.000	0.000			
5	1.905	0.270	1	H	-1.862	0.000	1.40	60	0.138
		0.593	2	H	-1.876		1.96	50	0.124
		0.651	3	O	-1.898		3.14	129	0.102
		0.185	4	Al	-1.900		2.97	164	0.100
		0.047	5	O	-1.902		2.96	160	0.098
					-2.000	0.000			
6	1.905	0.410	1	H	-0.382		1.83	77	1.618
		0.604	2	H	-1.831		2.88	37	0.169
		0.396	3	O	-1.854		4.34	129	0.146
		0.910	4	H	-1.883		3.86	103	0.117
		0.516	5	H	-1.884		2.93	99	0.116
		0.664	6	H	-1.889		2.62	111	0.111
		0.018	7	H	-1.955		2.10	94	0.045
					-2.000	0.000			
7	1.905	0.590	1	H	-1.623	0.000	3.34	60	0.377
		0.332	2	O	-1.676		3.82	42	0.324
		0.496	3	H	-1.835		4.79	47	0.165
		0.700	4	H	-1.881		5.56	19	0.119
		0.548	5	H	-1.890		6.01	11	0.110
		0.395	6	C	-1.890	-0.004	6.56	45	0.106
		0.792	7	C		-0.013	11.71	48	0.097
					-1.890	0.110			
8	1.905	0.730	1	C	0.000	-0.051	6.85	84	1.949
		0.928	2	C		-0.353	6.93	16	1.697
		0.460	3	C		-0.565	15.49	66	1.935
		0.576	4	C		-0.799	16.28	107	1.201
		0.796	5	C		-0.917	16.18	172	1.083
		0.017	6	C		-1.145	15.04	74	0.855
		0.998	7	C		-1.311	17.53	106	0.689
		0.217	8	C		-1.413	17.45	148	0.587
		0.082	9	C		-1.458	15.63	114	0.542

$Z_0$	$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$Z$	$\psi$	$E(n)$
1.905	0.740	10	C	0.000	-1.569	14.95	19	0.431
(cont)	0.443	11	C		-1.607	17.39	76	0.393
	0.860	12	C		-1.632	17.40	82	0.368
	0.750	13	C		-1.637	17.50	100	0.363
	0.088	14	C		-1.733	17.09	57	0.267
		15	C		-1.792	21.39	176	0.208
	0.991	16	C		-1.792	19.03	179	0.208
	0.956	17	C		-1.792	16.67	176	0.208
	0.940	18	C		-1.838	12.47	64	0.162
	0.047	19	C		-1.876	15.63	91	0.124
	0.302	20	C		-1.895	15.60	47	0.105
		21	C		-1.916	21.11	151	0.084
				0.000	-2.000			

39	1.905	0.890	1	O	-0.227	0.000	1.85	104	1.773
		0.213	2	H	-0.561		1.20	90	1.439
		0.664	3	H	-1.457		1.24	71	0.543
		0.684	4	O	-1.508		1.59	80	0.492
		0.267	5	O	-1.562		2.32	40	0.438
		0.612	6	H	-1.773		2.64	79	0.227
		0.892	7	H	-1.956		2.66	23	0.044
					-2.000	0.000			

$\Sigma \Delta E$ 's, 6 samples  
at  $Z_0 = 1.905$

9.890 2.110

40	0.635	0.080	1	H	-1.440	0.000	4.24	21	0.560
		0.435	2	C		-0.027	15.53	62	0.533
		0.118	3	C		-0.131	17.44	138	0.428
		0.123	4	C		-0.136	11.62	144	0.424
		0.170	5	C		-0.241	11.50	74	0.319
		0.878	6	C		-0.263	13.05	59	0.296
		0.325	7	C		-0.306	13.53	85	0.253
		0.260	8	C		-0.312	13.72	74	0.248
		0.317	9	C		-0.326	13.86	80	0.233
		0.250	10	C		-0.353	15.10	77	0.207
		0.720	11	C		-0.377	15.15	4	0.182
		0.510	12	C		-0.391	15.18	61	0.169
		0.014	13	C		-0.391	16.41	50	0.168
		0.592	14	C		-0.425	16.57	69	0.134
		0.600	15	C		-0.439	18.21	94	0.120
		0.787	16	C		-0.458	17.81	36	0.102

	<u>z<sub>0</sub></u>	<u>N</u>	<u>h</u>	<u>A</u>	<u>ΔE<sub>1</sub></u>	<u>ΔE<sub>2</sub></u>	<u>z</u>	<u>ψ</u>	<u>E</u>
	0.635	0.600	17	C	-1.440	-0.478	19.22	76	0.081
	(cont)				-1.440	-0.560			
41	0.635	0.250	1	AL	-0.207	0.000	3.86	99	1.793
		0.734	2	H	-0.443		2.86	120	1.557
		0.973	3	H	-0.873		2.20	96	1.127
		0.653	4	H	-1.007		1.52	97	0.993
		0.266	5	H	-1.529		1.39	143	0.476
		0.015	6	H	-1.792		0.85	162	0.208
		0.060	7 <sup>R</sup>	AL	-1.797		0.26	34	0.203
		0.564	8	H	-1.878		1.19	67	0.122
		0.864	9	H	-1.959		2.44	68	0.041
					-2.000	0.000			
42	0.635	0.417	1	O	-0.135	0.000	1.08	143	1.865
		0.004	2 <sup>R</sup>	O	-0.439		4.66	144	1.561
		0.083	3	H	-1.301		4.28	114	0.699
		0.297	4	H	-1.577		4.24	129	0.421
			5	O	-1.604		1.70	172	0.396
		0.992	6 <sup>R</sup>	C	-1.604	-0.110	17.70	153	0.287
		0.618	7	C		-0.143	16.51	90	0.254
		0.654	8	C		-0.187	16.51	135	0.209
		0.877	9	C		-0.204	16.04	95	0.192
		0.316	10	C		-0.220	15.58	56	0.176
		0.373	11	C		-0.257	18.14	143	0.139
		0.886	12	C		-0.260	16.78	116	0.136
		0.446	13	C		-0.283	16.62	131	0.113
		0.101	14	C	-1.604	-0.304	13.51	53	0.093
					-1.604	-0.396			
43	0.635	0.583	1 <sup>R</sup>	H	-1.397	0.000	0.13	130	0.603
		0.931	2 <sup>R</sup>	H	-1.874		0.35	87	0.126
		0.809	3	H	-1.943		0.35	71	0.057
					-2.000	0.000			
44	0.635	0.750	1 <sup>R</sup>	H	-0.504		0.03	72	1.496
		0.202	2	H	-1.095		0.43	107	0.905
		0.919	3 <sup>R</sup>	H	-1.844		1.13	136	0.156
		0.958	4	H	-1.900		0.93	135	0.100
		0.798	5 <sup>R</sup>	H	-1.956		1.47	93	0.044
					-2.000	0.000			

	$z_0$	N	n	A	$\Delta E_1$	$\Delta E_2$	z	$\psi$	E
45	0.635	0.820	1 <sup>R</sup>	H	-1.257	0.000	0.81	18	0.743
		0.550	2	O	-1.333		0.83	75	0.667
		0.318	3	Al	-1.378		1.74	54	0.622
		0.1648	4	H	-1.530		1.90	34	0.470
		0.394	5	H	-1.710		3.88	61	0.290
		0.173	6	H	-1.928		4.19	69	0.072
					<u>-2.000</u>	<u>0.000</u>			

$\Sigma \Delta E$ 's, 6 samples

from  $z_0 = 0.635$

11.044 0.953

Summary 45 neutrons:

	$z_0$	$\Delta E_f$	$\Delta E_c$
9 from	0.635	16.373	1.627
9 from	1.905	15.198	2.802
9 from	3.175	16.891	1.109
9 from	4.445	15.403	2.597
9 from	5.715	<u>12.954</u>	<u>5.046</u>
TOTAL		76.819	13.181

OF the  $2 \times 45 = 90$  max of the 45 neutrons,  
 85.4% is deposited in the fuel or water,  
 14.6% is deposited in the graphite.

of the 45 neutrons, 36 passed the lower  
 energy cut-off in the H-O-Al, and 9 in the  
 graphite.  $36/45 = 0.800$

$$46 \quad z_0 = 5.715 \quad DC_0 = 0.460$$

	N	n	A	$\Delta E_1$	$DE_2$	$z$	$\frac{\cos \phi}{4}$	E
46	0.730	1	H	-0.180		6.22	0.199	1.820
	0.928	2	H	-1.163		6.32	0.775	0.837
	0.576	3	C	-1.163	-0.101	8.44	0.174	0.736
	0.248	4	C		-0.143	9.10	0.353	0.693
	0.302	5	C		-0.337	9.75	-0.147	0.500
	0.382	6	C		-0.337	9.66	-0.218	0.499
	0.963	7	C		-0.448	7.96	-0.733	0.382
	0.997	8	H	-1.204		6.13	-0.513	0.348
	0.597	9	H	-1.321		5.81	-0.324	0.231
	0.280	10	H	-1.392		4.85	-0.605	0.159
	0.860	11	O	-1.401		4.84	-0.316	0.151
	0.253	12	H	-1.548		4.82	0.879	0.003
				1.552	-0.448			

$$47 \quad z_0 = 5.715 \quad DC_0 = 0.604$$

0.202	1	C	0.000	-0.421	8.78	-0.914	1.579
0.934	2	AL	-0.177		5.10	-0.436	1.402
0.308	3	H	-1.221		4.90	-0.712	0.357
0.859	4	H	-1.345		3.97	-0.958	0.234
0.062	5	H	-1.378		3.16	-0.886	0.201
0.747	6 <sup>R</sup>	H	-1.559		1.31	+0.299	0.020
			-1.579	-0.421			

$$48 \quad z_0 = 4.445 \quad DC_0 = 0.170$$

0.585	1	H	-0.610	0.000	5.07	-0.400	1.390
0.983	2	H	-1.631		2.67	-0.805	0.369
0.112	3	H	-1.721		0.39	-0.786	0.079
			-2.000				

49 is missing See pg 68

$$50 \quad z_0 = 4.445 \quad DC_0 = 0.534$$

0.767	1	AL	-0.251	0.000	5.55	-0.910	1.749
0.045	2	O	-0.297		4.31	-0.668	1.703
0.280	3	H	-1.373		0.27	+0.170	0.627
0.461	4	AL	-1.376		1.66	+0.432	0.624
0.435	5	H	-1.473		3.10	+0.697	0.527
0.409	6	H	-1.779		4.28	0.826	0.221
0.630							

$RN$	$N$	$A$	$\Delta E_1$	$\Delta E_2$	$Z$	$\cos \psi$	$E_n$
0.630	7	C	-1.779	-0.030	6.96	-0.433	0.191
0.042	8	H	-1.928	-0.030	5.93	-0.966	0.042
			-1.970	-0.030			

51  $Z_0 = 4.445$   $DC_0 = -0.534$

0.233	1	H	-0.178	0.000	1.90	0.751	1.822
0.952	2	H	-1.985	0.000	1.13	-0.278	0.015
			-2.000	0.000			

52  $Z_0 = 4.445$   $DC_0 = -0.840$

0.080	1	H	-1.280	0.000	3.76	-0.423	0.720
0.280	2 <sup>R</sup>	H	-1.402		3.61	+0.111	0.598
0.118	3	H	-1.926		3.89	-0.418	0.074
			-2.000	0.000			

53  $Z_0 = 3.175$   $DC_0 = -0.120$

0.440	1	AL	-0.143		1.99	-0.763	1.257
0.039	2 <sup>R</sup>	O	-0.525		0.91	-0.720	1.475
0.648	3	O	-0.794		0.87	-0.055	1.206
0.079	4	AL	-0.875		0.65	-0.256	1.125
0.791	5 <sup>R</sup>	H	-1.234		0.28	0.568	0.716
0.643	6	O	-1.332		4.28	-0.422	0.668
0.930	7	H	-1.502		4.10	-0.655	0.498
0.141	8	H	-1.705		2.52	-0.154	0.295
0.621	9	H	-1.805		2.29	-0.195	0.195
0.231	10	H	-1.987		1.36	-0.786	0.013
			-2.000				

54  $Z_0 = 3.175$   $DC_0 = 0.218$

0.609	1	C	0.000	-0.477	9.12	0.084	1.523
0.703	2	C		-0.693	9.20	0.997	1.307
0.488	3	C		-0.771	9.50	0.603	1.229
0.175	4	C		-1.035	10.43	0.292	0.965
0.606	5	C		-1.282	11.20	0.005	0.718
0.310	6	C		-1.485	11.24	-0.120	0.515
0.111							

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$N$	$n$	$A$	$\Delta E_1$	$\Delta E_2$	$Z$	$\cos \psi$	$E$
0.111	7	C	0.000	-1.609	10.97	0.749	0.391
0.426	8	C		-1.703	13.24	0.016	0.297
0.523	9	C		-1.740	13.29	-0.515	0.260
0.839	10	C		-1.774	12.61	0.243	0.226
0.684	11	C		-1.837	15.08	0.053	0.163
0.457	12	C		-1.839	15.08	-0.083	0.161
0.801	13	C		-1.878	15.06	0.672	0.122
	14	C		-1.902	15.85	-0.755	0.098
			0.000	-2.000			

55  $Z_0 = 3.175$   $DC_0 = \overline{0.840}$  should have been 0.734  
see pg 68

0.920	1	C	0.000	-0.182	12.29	0.673	1.818
	5	C	0.000	-1.121	11.96		0.879
0.397	10	C	0.000	-1.573	11.10	0.521	0.427
0.143	15	C	0.000	-1.753	10.24	-0.389	0.247
	19	H	-0.094	-1.822	6.29	-0.498	0.083
			-0.178	-1.822			

56  $Z_0 = 3.175$   $DC_0 = -0.840$  should have been 0.734  
see pg 68

0.080	1	H	-1.280	0.000	2.49	-0.423	0.720
0.220	2 <sup>R</sup>	H	-1.402		4.82	0.111	0.598
0.118	3	H	-1.926		5.16	-0.418	0.074
			-2.000	0.000			

57  $Z_0 = 1.905$   $DC_0 = +0.278$

0.639	1	H	-0.574	0.000	2.37	0.646	1.426
0.397	2	C	-0.574	-0.050	8.02	0.234	1.376
	5			-0.755	11.10	-0.435	0.671
0.088	10	H	-0.591	-0.947	6.20	-0.787	0.462
0.189	11	H	-0.792		3.11	-0.993	0.261
0.975	12	H	-0.820		2.46	-0.905	0.233
0.567	13	H	-0.976		2.01	-0.229	0.077
			-1.053	-0.947			

N	n	A	$\Delta E_1$	$\Delta E_2$	Z	$\cos \theta$	E
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52  $z_0 = 1.905$   $DC_0 = +0.886$

0.943	1	al	-0.143	0.000	3.44	-0.432	1.857
0.060	2	H	-1.052		3.30	-0.267	0.948
0.740	3	H	-1.395		2.16	-0.004	0.605
0.691	4	al	-1.446		2.16	-0.009	0.554
0.752	5	al	-1.469		2.15	-0.830	0.531
0.066	6 <sup>R</sup>	al	-1.521		2.03	-0.478	0.477
0.802	7 <sup>R</sup>	H	-1.645		0.20	-0.029	0.355
0.029	8	H	-1.829		0.06	-0.586	0.171
0.106	9 <sup>R</sup>	H	-1.871		0.01	0.569	0.129
0.274	10	H	-1.959		0.03	0.731	0.041
			-2.000	0.000			

59  $z_0 = 1.905$   $DC_0 = -0.886$

0.057	1 <sup>R</sup>	H	-0.962	0.000	2.91	0.342	1.038
0.937	2	H	-1.606		3.47	0.285	0.394
0.734	3	H	-1.842		4.26	-0.027	0.158
0.205	4	H	-1.919		4.23	-0.119	0.081
			-2.000	0.000			

60  $z_0 = 0.635$   $DC_0 = -0.326$

0.337	1	H	-1.442	0.000	0.20	0.521	0.558
0.416	2	H	-1.560		3.26	0.226	0.440
0.147	3	H	-1.854		3.57	0.724	0.146
0.616	4	O	-1.880		3.74	-0.350	0.120
0.640	5	Al	-1.886		3.70	-0.972	0.114
-	6	H	-1.939		2.25	-0.613	0.061
			-2.000	0.000			

61  $z_0 = 0.635$   $DC_0 = -0.680$

0.160	1 <sup>R</sup>	O	-0.124	0.000	0.59	0.928	1.876
0.560	2 <sup>R</sup>	C	-0.124	-0.494	11.34	0.879	1.382
0.928	3	C	-0.893		16.52	-0.742	0.983

N	n	A	$\Delta E_1$	$\Delta E_2$	Z	$\cos \psi$	$E_n$
0.175	12	C	-0.124	-1.522	7.96	-0.455	0.354
0.479	13	C		-1.535	7.24	-0.904	0.341
0.964	14	al	-0.144	-1.535	5.10	-0.298	0.321
0.199	15	H	-0.281	-1.535	4.54	-0.466	0.184
0.187	16	H	-0.352	-1.535	4.48	-0.866	0.113
0.068	17	H	-0.438	-1.535	4.39	0.009	0.027
			-0.465	-1.535			

62  $z_0 = 0.635$   $DC_0 = 0.822$

0.911	1	al	-0.238	0.000	0.82	-0.822	1.762
0.148	2 <sup>R</sup>	H	-0.982		1.43	0.722	1.018
0.292	3	al	-1.039		2.24	0.786	0.961
0.558	4	O	-1.206		4.50	-0.927	0.794
0.967	5	H	-1.352		2.47	-0.853	0.648
0.765	6	H	-1.676		1.81	-0.233	0.324
0.498	7	H	-1.801		1.28	-0.650	0.199
0.109	8	H	-1.884		1.00	-0.023	0.116
-	9	H	-1.956		0.99	0.493	0.044
			-2.000	0.000			

63  $z_0 = 0.635$   $DC_0 = -0.822$

0.089	1 <sup>R</sup>	C	0.000	-0.522	13.36	-0.884	1.478
0.863	2	C		-0.527	9.97	-0.869	1.473
0.753	3	H	-0.255	-0.527	2.99	-0.995	1.218
0.020	4 <sup>R</sup>	O	-0.343	-0.527	0.69	0.489	1.130
0.464	5	al	-0.497	-0.527	1.62	-0.390	0.977
0.316	6 <sup>R</sup>	H	-0.880	-0.527	0.58	-0.269	0.594
0.983	7 <sup>R</sup>	O	-0.771	-0.527	0.37	0.543	0.482
0.494	8	O	-1.084	-0.527	3.09	-0.946	0.390
0.053	9	al	-1.091	-0.527	2.99	-0.845	0.382
0.863	10	H	-1.417	-0.527	2.34	0.025	0.056
			-1.473	-0.527			

1 N 1 n 1 A 1  $\Delta E_1$  1  $\Delta E_2$  1 z 1  $\cos \phi$  1 E

49  $z_0 = 4.475$   $DC_0 = -0.170$

0.415	1	H	-1.390	0.000	3.97	-0.912	0.610
0.014	2	H	-1.619	0.000	1.31	-0.559	0.321
0.362	3 <sup>R</sup>	O	-1.634	0.	0.38	-0.219	0.366
0.002	4 <sup>R</sup>	H	-1.939		3.42	-0.200	0.061
			-2.000	0.000			

55  $z_0 = 3.175$   $DC_0 = 0.734$

0.867	1	O	-0.094	0.000	3.38	0.124	1.906
0.145	2	H	-0.721		3.80	0.613	1.279
0.428	3	C	-0.721	-0.225	7.94	-0.202	1.054
0.772	4	C		-0.450	6.84	0.522	0.829
0.668	5	C		-0.470	8.90	-0.136	0.809
0.819	7	H	-1.292	-0.561	6.15	0.040	0.147
0.711	8	H	-1.425	-0.561	6.16	-0.342	0.014
			-1.439	-0.561			

56  $z_0 = 3.175$   $DC_0 = -0.734$

0.133	1 <sup>R</sup>	C	0.000	-0.365	6.56	-0.313	1.435
0.211	2	H	-0.127	-0.365	5.86	-0.351	1.508
0.219	3	H	-0.896		1.93	-0.174	0.739
0.267	4	O	-0.985		1.42	0.974	0.650
0.528	5	H	-1.006		6.32	0.952	0.628
0.231	6	C	-1.006	-0.459	12.04	-0.073	0.542
0.137	8	C		-0.640	10.23	-0.046	0.354
0.123	11	H	-1.043	-0.790	4.20	-0.778	0.166
0.830	12	H	-1.094		4.16	-0.995	0.116
0.996	13	H	-1.178	-0.790	3.93	-0.517	0.031
			-1.210	-0.790			

Statistical SummaryCase 1 All 63 neutrons

		$\Delta E_1$	$\Delta E_2$
First	45	76.819	13.181
Nept	18	<u>28.741</u>	<u>7.259</u>
		105.560	20.440

Fraction in Graphite 0.162

Case 2

50 neutrons. This case was constructed by deleting 13 neutrons and adding the 18 neutrons number 46-63. The 13 that were discarded were rejected because of one of the following:

- The early results were somewhat biased in initial direction, 24 started moving into the fuel box, only 19 outward, 2 unknown.
- The two unknown (in direction) were discarded.
- Others were paired using complementary initial direction cosines. Two that had been paired (26 and 27) fell close to another pair (24 and 25). The 50 neutrons are unbiased and more uniformly sample the  $2\pi, \cos \phi_0$  initial coordinates.

The 13 discards are Nos 2, 3, 5, 9, 10, 11, 12, 13, 14, 26, 27, 29, 45. These neutrons had deposited 94.3% of their energy in the fuel box. The 50 neutron summary.

$$\left. \begin{array}{ll} \Delta E_1 = 81.021 & 81\% \\ \Delta E_2 = 18.979 & 19\% \end{array} \right\}$$

## NEUTRONS THAT ENTER GRAPHITE

	$z_0$	$(\cos \phi)_0$	$t_1$	$\Delta E$	$n_e$	$n_c$
4	1.905	-0.278	1.156	0.692	1	9
6	5.715	-0.603	0.115	0.115	1	1
7	4.445	+0.840	2.000	1.043	2	3, 10
15	0.635	-0.326	0.831	0.312	1	4
17	5.715	+0.300	1.876	1.082	1	7
18	5.715	+0.800	2.000	0.511	1	1
19	5.715	-0.800	1.917	1.677	2	6, 6
21	5.715	-0.100	1.958	1.695	1	13
22	4.445	+0.780	1.892	0.339	1	2
24	4.445	+0.340	1.778	1.076	3	1, 3, 3
28	3.175	-0.560	1.013	0.112	1	1
37	1.905	0.140	0.110	0.110	1	2
38	1.905	0.580	2.000	2.000	1	21
40	0.635	0.680	0.560	0.560	1	16
42	0.635	0.182	0.396	0.396	1	9
46	5.715	0.460	0.837	0.448	1	5
47	5.715	0.604	2.000	0.421	1	1
50	4.445	0.534	0.221	0.030	1	1
54	3.175	0.218	2.000	2.000	1	14
55	3.175	0.734	1.279	0.561	1	3
56	3.175	-0.734	2.000	0.790	2	1, 3
57	1.905	0.278	1.426	0.947	1	9
61	0.635	-0.680	1.876	1.535	1	12
63	0.635	-0.822	2.000	0.527	1	2
			33.241	18.979		

	neutrons	reached	graphite	(48%)	$\bar{E}_1$
24	neutrons	reached	graphite	from $z_0 = 5.715$	1.53
7	"	"	"	" " = 4.445	1.47
4	"	"	"	" " = 3.175	1.57
4	"	"	"	" " = 1.905	1.17
4	"	"	"	" " = 0.635	1.12
5	"	"	"	" " = 0.635	1.12

Number Entering in	$\Delta E = E_1 - E_2$
$\Delta E = 2.0 - 1.0$	8
1.0 - 0.5	7
0.5 - 0.25	5
< 0.25	4

$$\bar{E}_1 = 1.385 \text{ mev/neutron}$$

$$\overline{\Delta E} = 0.783 \text{ mev/neutron}$$

1. The average neutron which reaches graphite, deposits  $0.783/2 = 0.392$  of its birth energy in the graphite.
2. As 48% of the neutrons reach the graphite one way or another, the fraction of the total birth energy that is deposited in graphite is:

$$0.392 \times 0.48 = 0.188$$

INITIAL CONDITIONS - Direction Cosines at  $Z_0$  in  $\Delta(\cos \psi) = 0.10$

	5.715	4.445	3.175	1.905	0.635
DESCRIPTION		1	2	3	4
0.0 - 0.1			<del>3</del> - 0.067	34/39 $\pm$ 0.060	
0.1 - 0.2	20 - 0.100 21 + 0.100	48 + 0.170 47 - 0.170	<del>13</del> + 0.156 32 + 0.120 53 - 0.120	36/37 $\pm$ 0.140	42/43 $\pm$ 0.170
0.2 - 0.3			8 - 0.218 54 + 0.218	4 - 0.278 57 + 0.278	
0.3 - 0.4	16 - 0.300 17 + 0.300	<del>12</del> - 0.350 24/25 + 0.340 <del>26/27</del> $\pm$ 0.360	30/31 $\pm$ 0.320		15 - 0.326 60 - 0.326
0.4 - 0.5	1 - 0.460 <del>1</del> - 0.436 46 + 0.460				<del>5</del> - 0.426
0.5 - 0.6		50 + 0.534 51 - 0.534	22/23 $\pm$ 0.560	<del>9</del> + 0.506 <del>14</del> - 0.520 35/38 $\pm$ 0.580	41/45 $\pm$ 0.500
0.6 - 0.7	6 - 0.603 47 + 0.604	<del>2</del> - 0.618			40 + 0.620 61 - 0.620
0.7 - 0.8		22 + 0.780 23 - 0.780	55 + 0.734 56 - 0.734		
0.8 - 0.9	18 - 0.860 19 - 0.900	7 + 0.840 52 - 0.840		58 + 0.826 59 - 0.886	<del>10</del> + 0.860 62 + 0.822 63 - 0.822
0.9 - 1.0					
			<del>29</del> - ?		<del>45</del> - ?