

# Application of Point Precipitation Frequency Estimates to Watersheds

Presented at

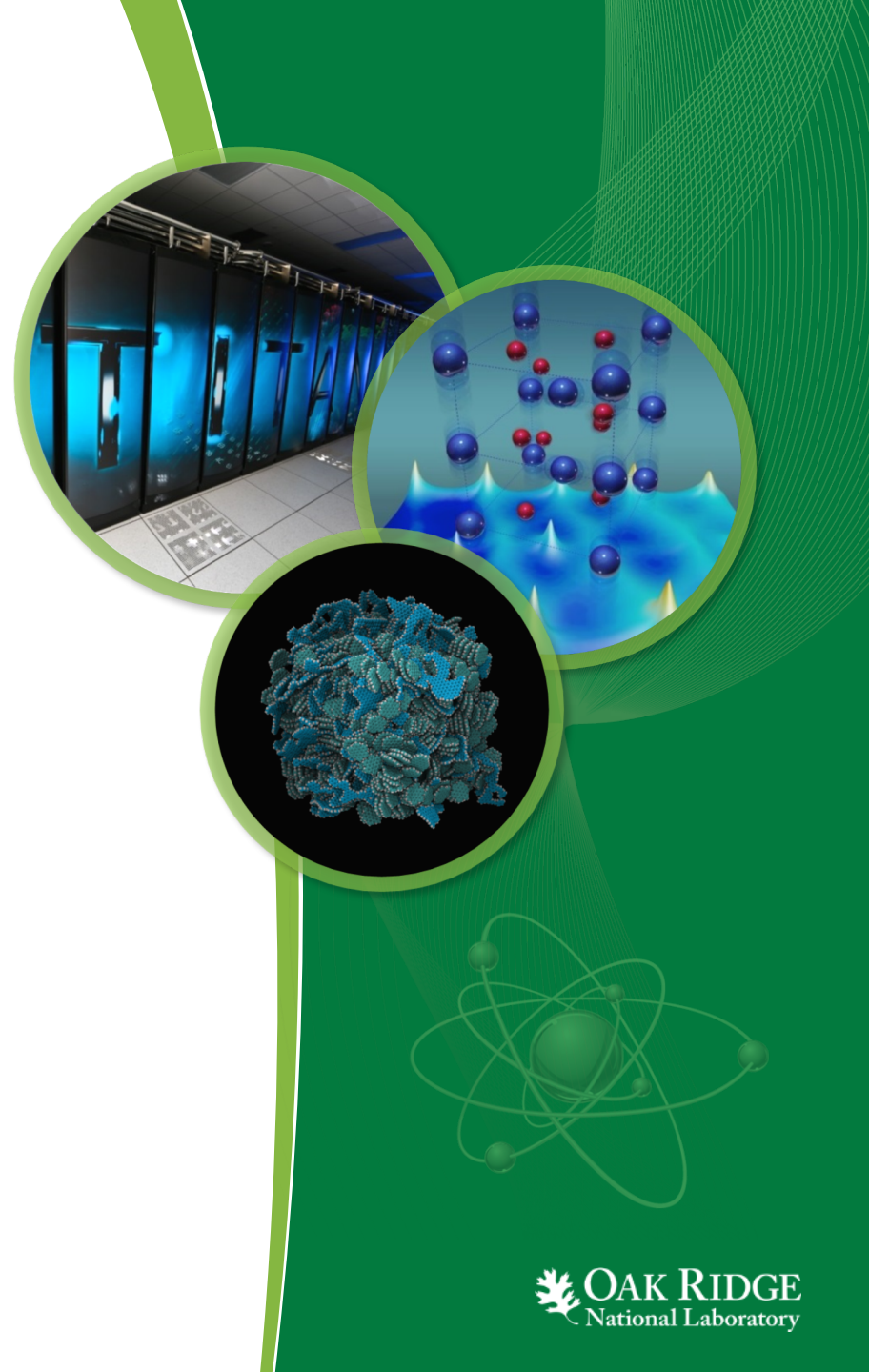
## **The 5<sup>th</sup> Annual Probabilistic Flood Hazard Assessment (PFHA) Research Workshop**

February 19<sup>th</sup> – February 21<sup>st</sup>, 2020

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Oak Ridge National Laboratory

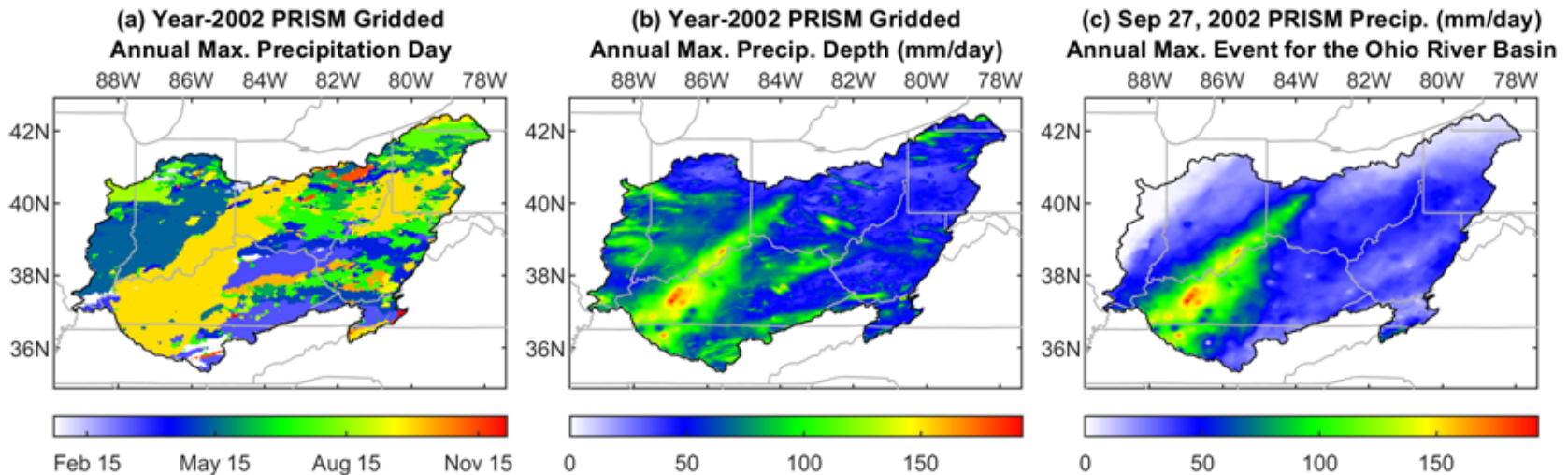
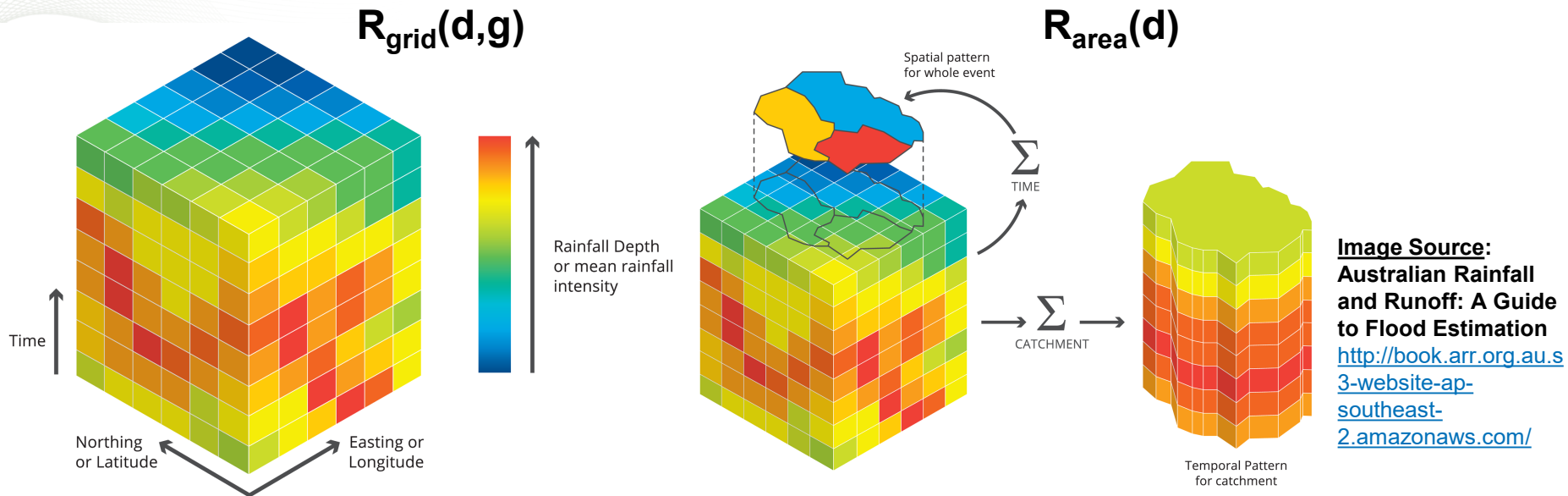
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# Leverage Existing PFA Products

- **To avoid going through the entire chain of precipitation frequency analysis (PFA), we have often opted to look up pre-calculated  $T$ -year rainfall depths from existing PFA products**
  - TP-40 (Hershfield, 1961)
  - National Oceanic and Atmospheric Administration (NOAA) Atlas 14 (Bonnin et al., 2004 and other volumes)
- **However, most of the PFA products (including NOAA Atlas 14) provide frequency estimates of “point” precipitation**
  - This happens because the **annual (or partial duration) maxima are usually identified independently in time.**
  - Representative only for a small domain – not directly appropriate for large-scale watershed modeling applications.
  - Appropriate conversion factor is hence needed to derive areal-based extreme precipitation estimate.

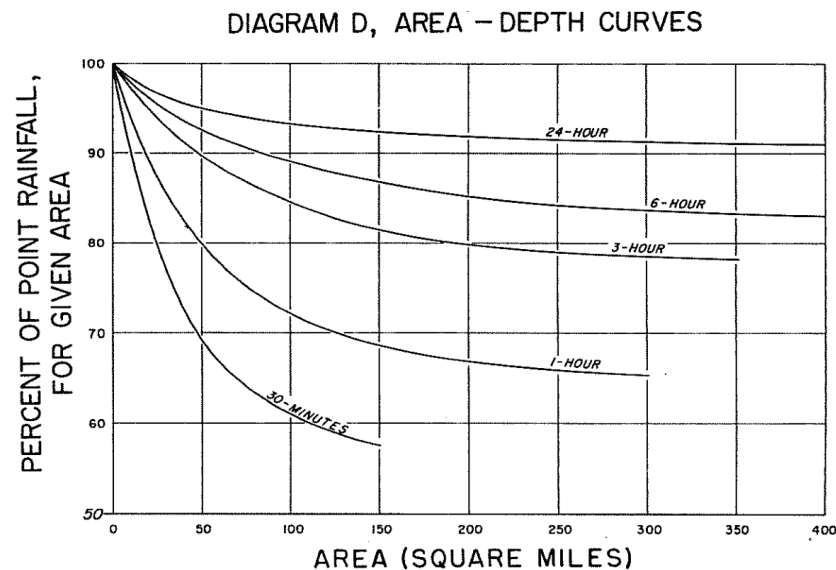
# Differences between Grid vs. Areal Maximum



# Precipitation Areal Reduction Factor (ARF)

- Existing PFA products (e.g., NOAA Atlas 14) are mostly developed for point rainfall
- Areal reduction factor (ARF) is defined as the ratio of areal extreme rainfall depth ( $P_{\text{area}}$ ) to point-based extreme rainfall depth ( $P_{\text{point}}$ )
  - $P_{\text{area}} = P_{\text{point}} * \text{ARF}$
- ARFs in common use suffer from several key limitations:
  - Limited / outdated data
  - Small area sizes (up to 400 mi<sup>2</sup>)
  - Do not vary with location, return period, or season

## Example ARF curves (from TP-29)



Source: Technical Paper No. 29; noaa.gov



# Objectives of this Project

- **Understand and demonstrate how ARFs may vary when using different precipitation data products and ARF methods across different geographical locations, durations, areas, return periods, seasons, and etc.**
  - Task 1: Provide a summary of available precipitation products that can be used to develop ARFs.
  - Task 2: Provide a critical review of available ARF methods with a view to addressing the deficiencies in the commonly used empirical methods.
  - Task 3: Demonstrate use of the most promising method/dataset combinations through selected test cases.
- **Support Nuclear Regulatory Commission (NRC) on the development of future Probabilistic Flood Hazard Assessment (PFHA) guidance on ARFs used by NRC licensees**

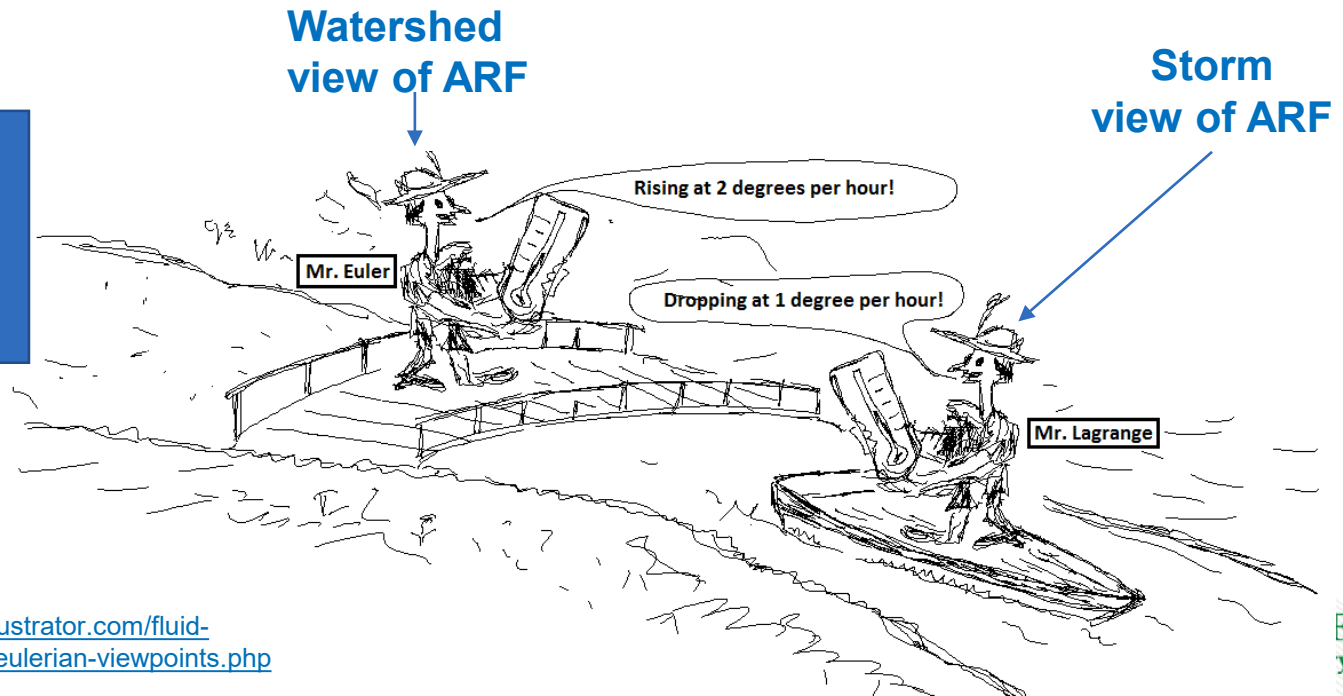
# Fixed-area ARF

- **Following a watershed**
  - Find the maximum rainfall depth for a watershed
  - Maximum rainfall may capture one or multiple storms
  - More suitable for PHFA applications

# Storm-centered ARF

- **Following a storm**
  - Describe the maximum rainfall depth of a moving storm
  - Storm may move across multiple watersheds
  - More suitable for deterministic storm analysis (e.g., PMP)

Given our specific focus of PFHA, this study only examined fixed-area ARF.



# Study Approach

- **Factors affecting ARFs**

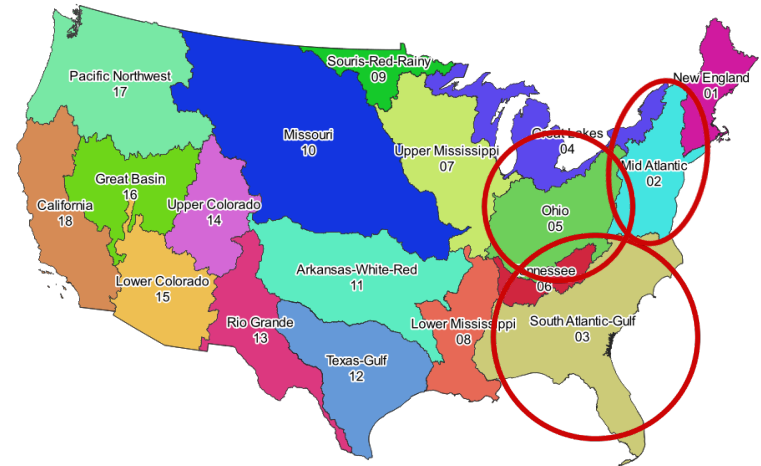
- Area, duration, and return period
- Different ARF methods
- Precipitation products to use
- Geographical locations
- Seasonality

- **Case study application**

- Regional comparison
  - 3 hydrologic regions (HUC02), 5 precipitation products, and 6 ARF methods
- National comparison
  - 18 hydrologic regions (HUC02), 1 precipitation product, and 1 ARF method

- **Evaluation through fitting statistics (e.g., NSE, RMSE,  $R^2$ )**

- **Only consider “geographically-fixed-area” ARF**



# Key Metrics for Data Consideration

- **Accuracy/precision**
  - How reliable are the precipitation estimates available from the product, and what sources of error and uncertainty exist?
- **Temporal coverage**
  - For what time period are the precipitation estimates available, and are there any gaps in temporal coverage?
- **Data latency**
  - How regularly are the precipitation estimates uploaded online?
- **Spatial coverage**
  - For what regions are the precipitation estimates available?
- **Temporal resolution**
  - How frequently are precipitation estimates provided?
- **Spatial resolution**
  - For what horizontal spacing or area size are individual precipitation estimates available?



# Selected Precipitation Products in Case Study

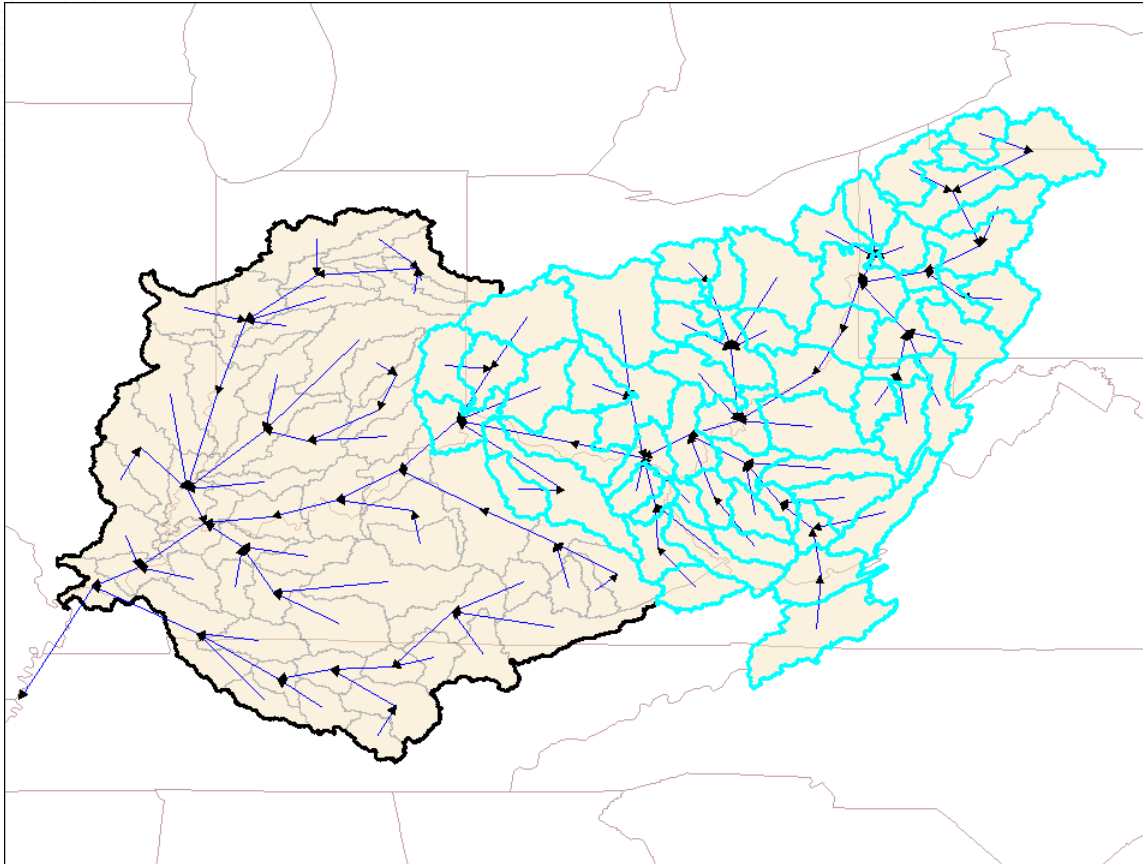
Precipitation Products	Provider	Dataset Type	Coverage Start	Coverage End	Data Latency	Spatial Coverage	Temporal Resolution	Spatial Resolution
<b>Gauge-only Datasets</b>								
Hourly Precipitation Data (DSI3240)	NOAA National Centers for Environmental Information (NCEI)	Gauge observation	1940	2013	Data since 2014 have not been released (checked 10/17/2017)	U.S. (including AK, HI, PR)	Hourly	Gauge
<b>Gauge-driven Products</b>								
Daymet version 3 (Daymet)	Oak Ridge National Laboratory (ORNL)	Gridded from gauge observation	1980	2017	Annual update	North America	Daily	1 km * 1 km
Daily PRISM Dataset (PRISM)	Oregon State University	Gridded from gauge observation (and partially with radar)	1981	present	Operational (updated automatically)	U.S. (48 states)	Daily	1/24 deg * 1/24 deg (~ 4 km * 4 km)
Livneh CONUS Near-surface Meteorological Data (Livneh)	University of Colorado, Boulder	Gridded from gauge observation	1950	2013	No scheduled update (checked 10/17/2017)	U.S. (48 states), Mexico, & Canada (south of 53N)	Daily	1/16 deg * 1/16 deg (~ 6 km * 6 km)
<b>Radar-driven Products</b>								
NCEP National Stage IV Analyses (ST4)	NOAA National Centers for Environmental Prediction (NCEP)	Merged radar and gauges (with QC)	2002	present	Operational (updated automatically)	U.S. (48 states), excluding California-Nevada & Northwest RFCs	Hourly	4 km * 4 km

- These precipitation products exhibit long temporal coverage, broad spatial coverage, and sufficient temporal/spatial resolution.
- DSI3240 is only analyzed for Region 05 (Ohio).

# Case Study Assessment Procedures

- **Annual maximum series (AMS) searching**
  - *Data*
    - PRISM (1981–2017), Daymet (1980–2017), ST4 (2002–2017), Livneh (1950–2013), DSI3240 (1950–2013)
  - *Duration*
    - All: 1-day, 2-day, 3-day
    - Additionally for ST4 & DSI3240: 1-hr, 2-hr, 3-hr, 6-hr, 12-hr, 18-hr
  - *Season*
    - All season, Warm season (May–Oct), Cool season (Jan–Apr, Nov–Dec)
  - *Grid AMS* ( $P_{\text{grid}}$ ): annually at each grid
  - *Areal AMS* ( $P_{\text{area}}$ ): annually at each HUC08, HUC06, HUC04, HUCac
- **Sample ARF at each areal units (HUCs)**
  - Average AMS
    - (Temporal average of  $P_{\text{area}}$ ) / (Temporal and spatial average of  $P_{\text{grid}}$ )
  - T-year estimate
    - Fitting AMS by GEV, and getting T-year estimates (e.g.,  $P_{\text{area},10\text{yr}}$ )
    - $P_{\text{area},\text{Tyr}}$  / (Spatial average of  $P_{\text{g11},\text{Tyr}}$ )
- **Regional fitting by different ARF models**

# Watershed-based AMS Searching Approach



- Increase AMS samples to cover a wider range of watershed sizes
- Define additional spatial unit HUCac based on watershed connectivity
  - For each HUC08, using its connectivity with other HUC08s to identify the entire upstream contributing watershed as HUCac
  - Use HUCac to search AMS
- Use HUC08, HUC06, HUC04, and HUCac AMS to fit different ARF models
  - 120 HUC08: 290 – 840 km<sup>2</sup>
  - 21 HUC06: 4,400 – 54,000 km<sup>2</sup>
  - 7 HUC04: 15,000 – 85,000 km<sup>2</sup>
  - 46 HUCac: 4,600 – 420,000 km<sup>2</sup>

# Selected ARF Models

## • Empirical Methods

- M1: Leclerc & Schaake (1972) – fitted formula of US Weather Bureau TP-29
- M2: Koutsoyiannis and Xanthopoulos (1999) – fitted UK-NERC ARF relationship (NERC, 1975)
- M3: Hydrological Atlas of Switzerland Model (Grebner et al., 1998)
- M4: Australian Rainfall & Runoff (ARR) Guideline (Nathan and Weinmann, 2016)

$$ARF(A, D) = 1 - e^{aD^b} + e^{(aD^b - cA)}$$

$$ARF(A, D) = 1 - \frac{aA^{(b-c \ln A)}}{D^d}$$

$$ARF(A) = \frac{a_0}{(A + a_2)^{a_1}} + a_3 e^{-a_4 A}$$

$$\begin{aligned} ARF(A, D, AEP) &= 1 - a(A^b - c \log_{10} D)D^{-d} \\ &+ eA^f D^g (0.3 + \log_{10} AEP) \\ &+ h10^{iAD} (0.3 + \log_{10} AEP) \end{aligned}$$

## • Dynamic Scaling Model

- M5: De Michele et al. (2001)

$$ARF(A, D) = \left[ 1 + w \left( \frac{A^z}{D} \right)^b \right]^{-v/b}$$

## • Extreme Value Theory

- M6: Overeem et al. (2010)

$$\begin{aligned} ARF(A, D, AEP) &= P(A, D, AEP) / P(A^*, D, AEP) \\ P(A, D, AEP) &= GEV^{-1}(1 - AEP | \mu, \gamma, \kappa) \\ \mu(A, D) &= aD^b + (c + d \ln D)A^e \\ \gamma(A, D) &= f \ln A + g \ln D + h \\ \kappa(A) &= i \ln A + j \end{aligned}$$



# M5: De Michele Dynamic Scaling Model

- **De Michele et al. (2001) and (2011)**

- Uses the concepts of dynamic scaling and statistical self-affinity to find a general expression for the mean annual maxima precipitation as a function of the rainfall duration and area

- $$ARF(A, D) = \left[ 1 + w \left( \frac{A^z}{D} \right)^b \right]^{-v/b}$$

- $A$ , area (km<sup>2</sup>)
- $D$ , duration (hr)
- Four parameters:  $v$ ,  $b$ ,  $w$ ,  $z$

- **ORNL Fitting**

- Minimize the root mean square error (RMSE) between ARF samples and ARF model using Matlab *fminsearch* function (Nelder-Mead simplex algorithm; Lagarias et al., 1998)
- Performance evaluated by Nash–Sutcliffe efficiency (NSE)
- (4 fitted parameters) \* (# of frequency levels)

# Summary of Overall Findings

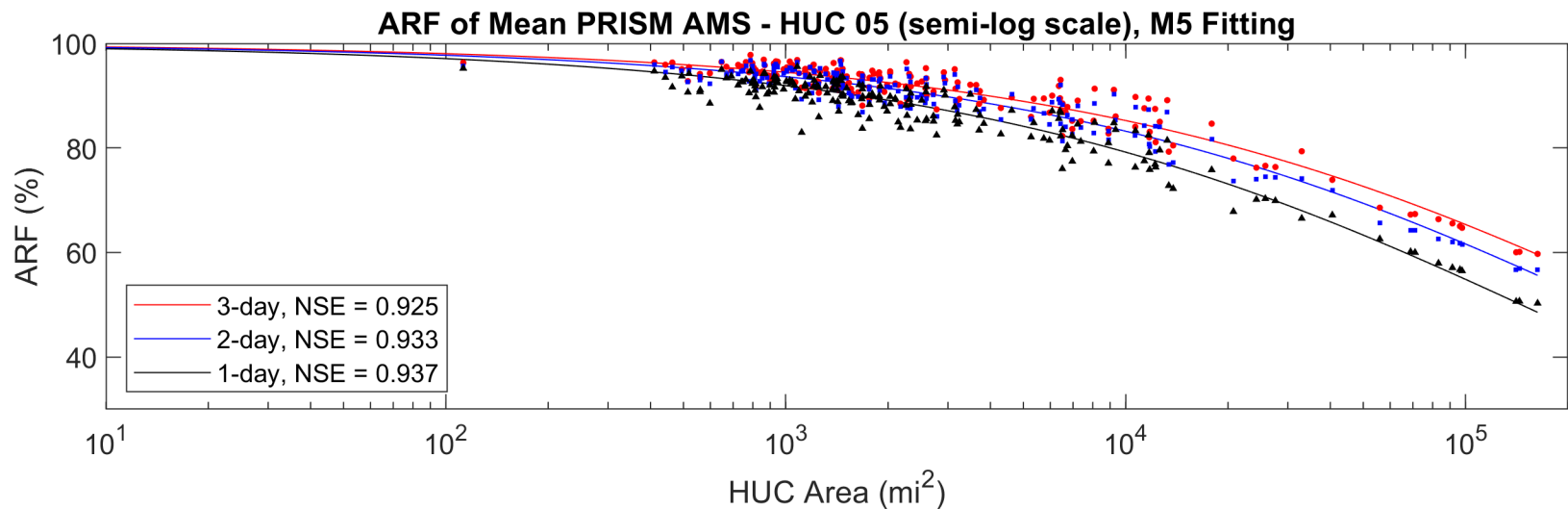
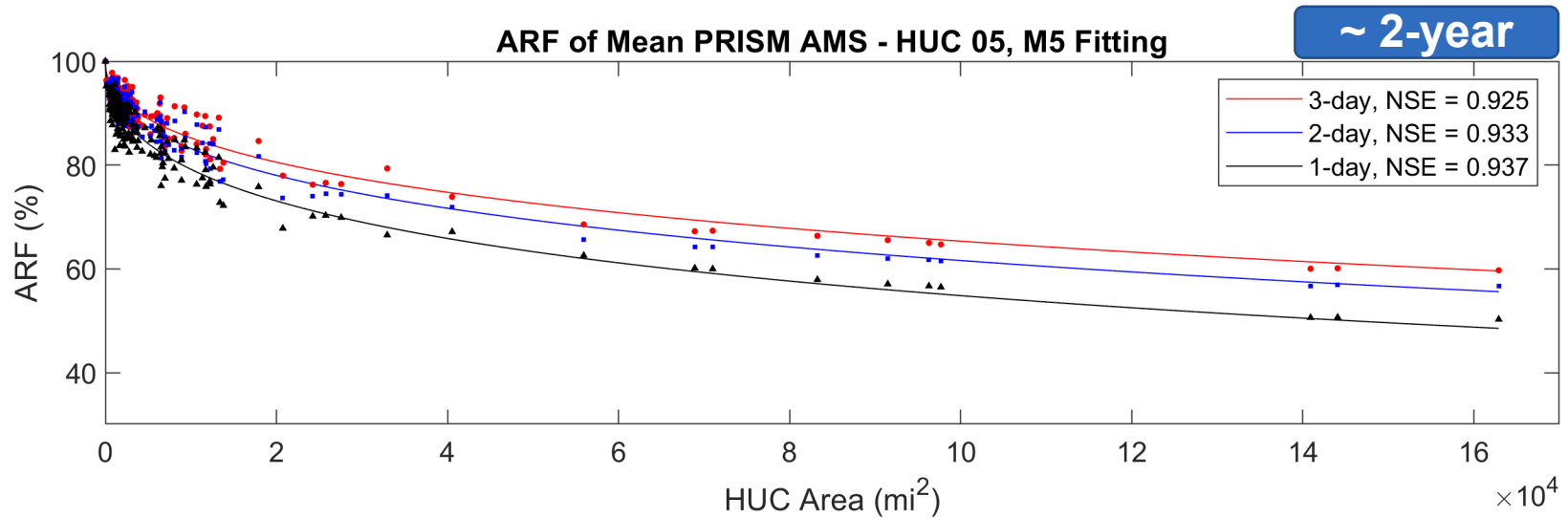
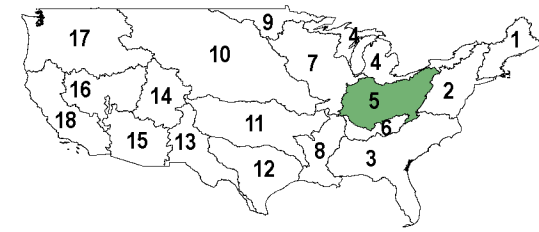
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- ARF methods may cause significant differences.
- For data sources, smaller ARF differences are found, but the differences are not negligible.
- Cool season ARF > All season ARF > Warm season ARF
- ARF varies across different regions. Using one set of ARF everywhere across the country is not justified.
- High return level ARF remains a major challenge, mostly due to relatively short data record length.

# Region 05

## M5 De Michele

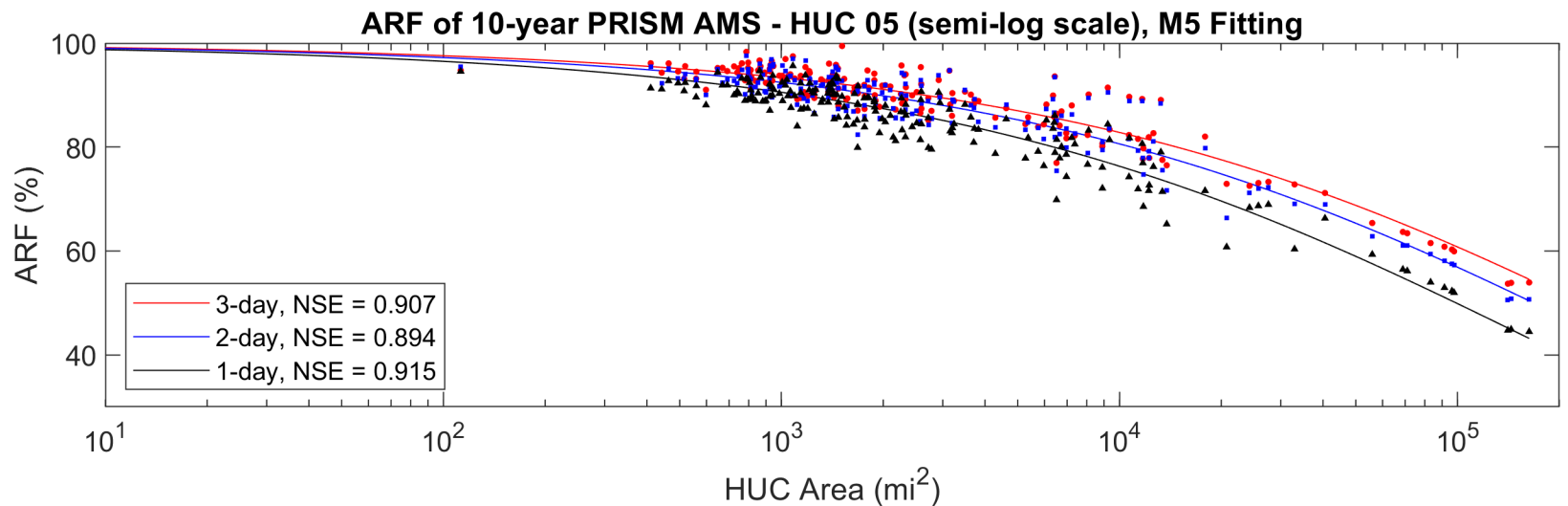
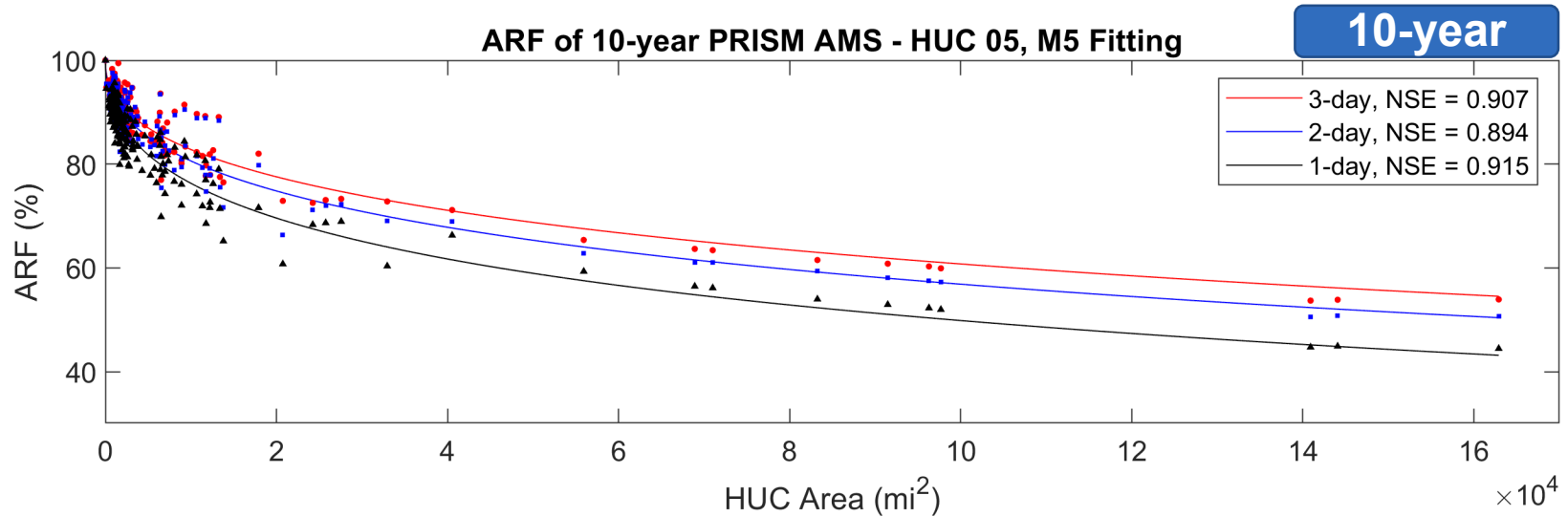
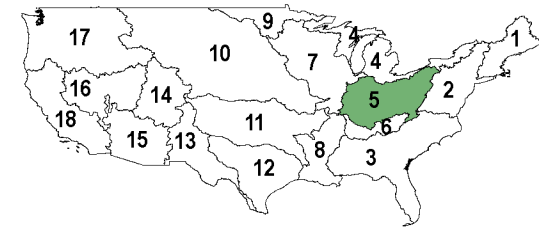
### Model

- Data: PRISM (all seasons)
- Duration: 1-day, 2-day, 3-day
- Frequency level: AMS
- ARF Fitting: M5



# Region 05 M5 De Michele Model

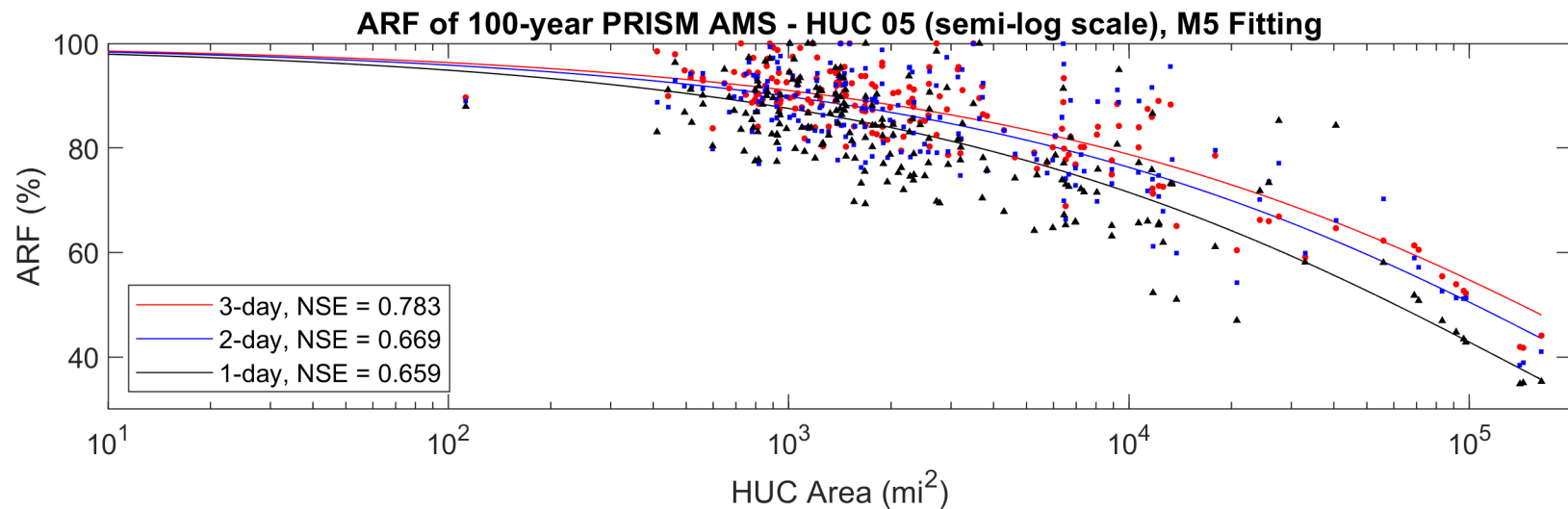
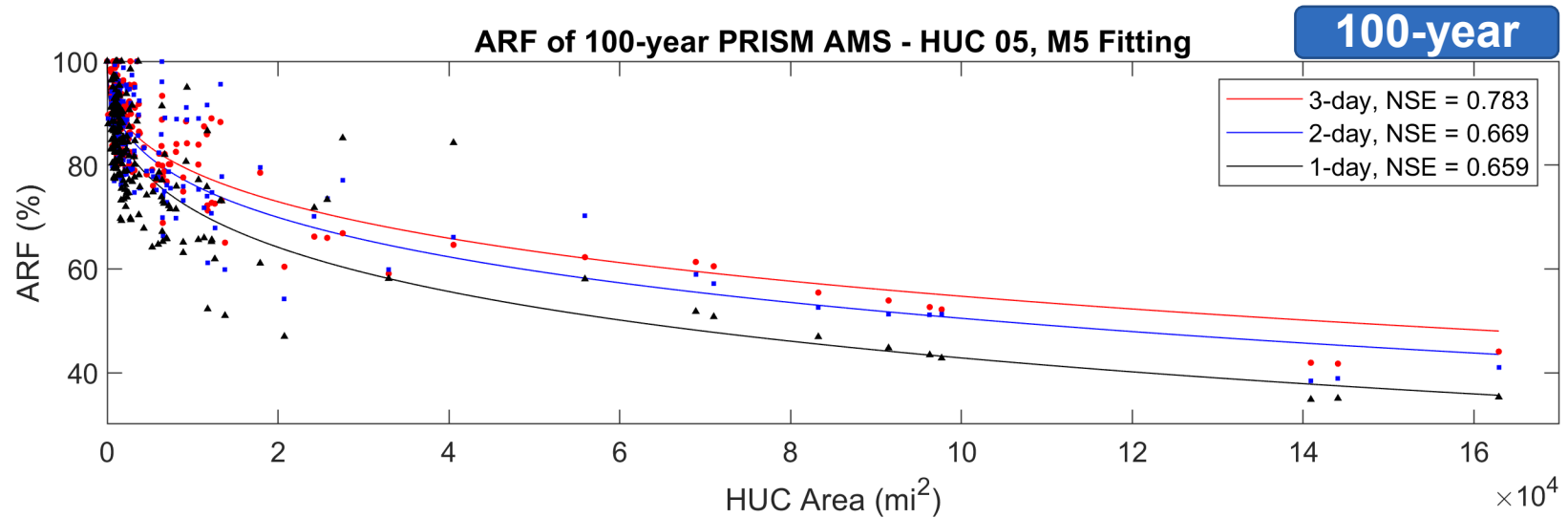
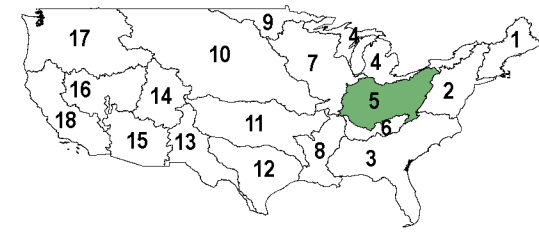
- Data: PRISM (all seasons)
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- Frequency level: 10-year
- ARF Fitting: M5





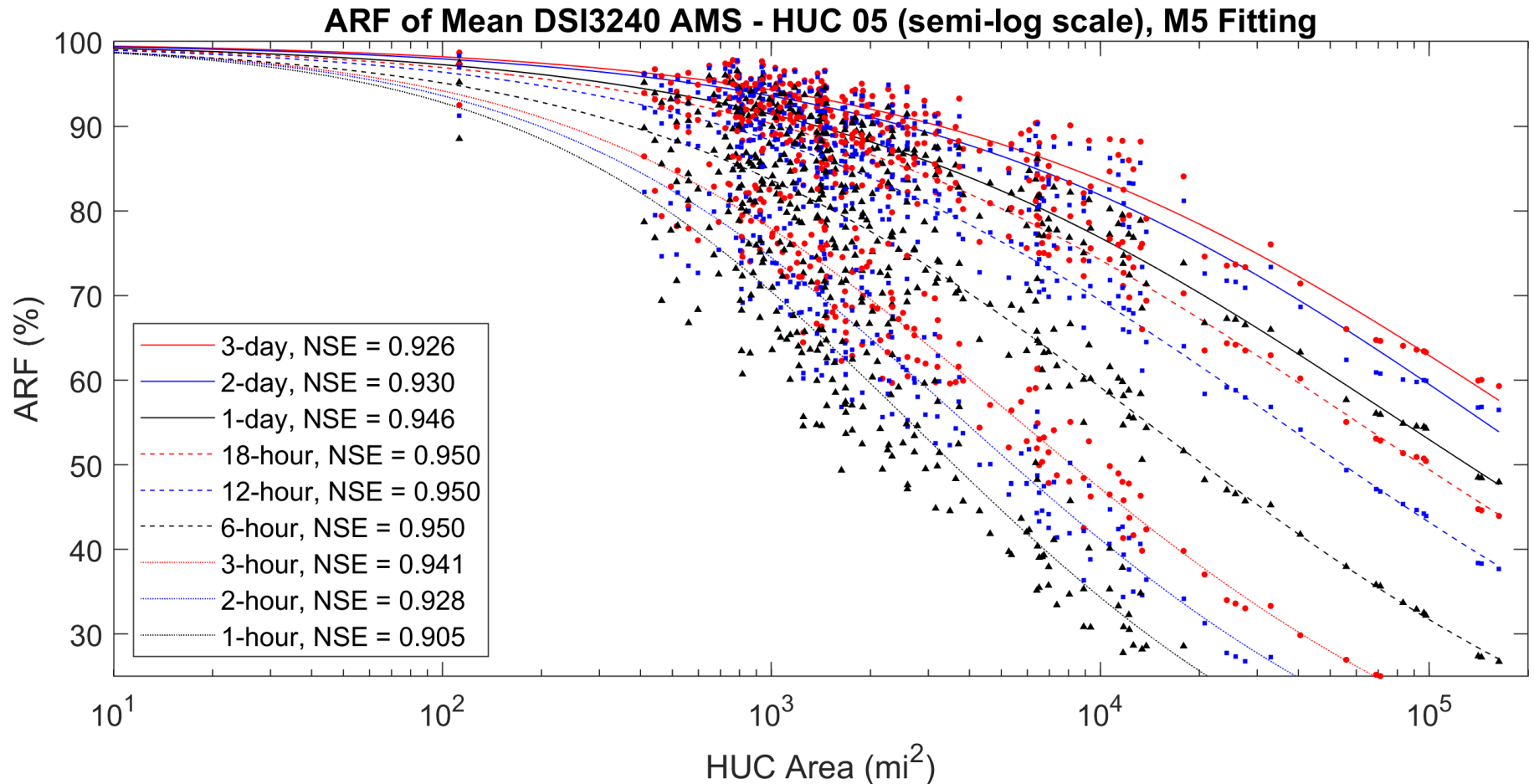
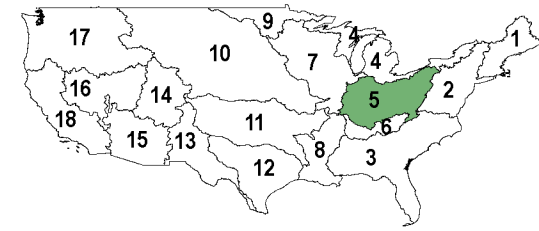
# Region 05 M5 De Michele Model

- Data: PRISM (all seasons)
- Duration: 1-day, 2-day, 3-day
- Frequency level: 100-year
- ARF Fitting: M5



# Differences across Durations

- Data: DSI3240 (all seasons)
- Duration: 3-day, 2-day, 1-day, 18-hr, 12-hr, 6-hr, 3-hr, 2-hr, 1-hr
- Frequency level: AMS
- ARF Fitting: M5

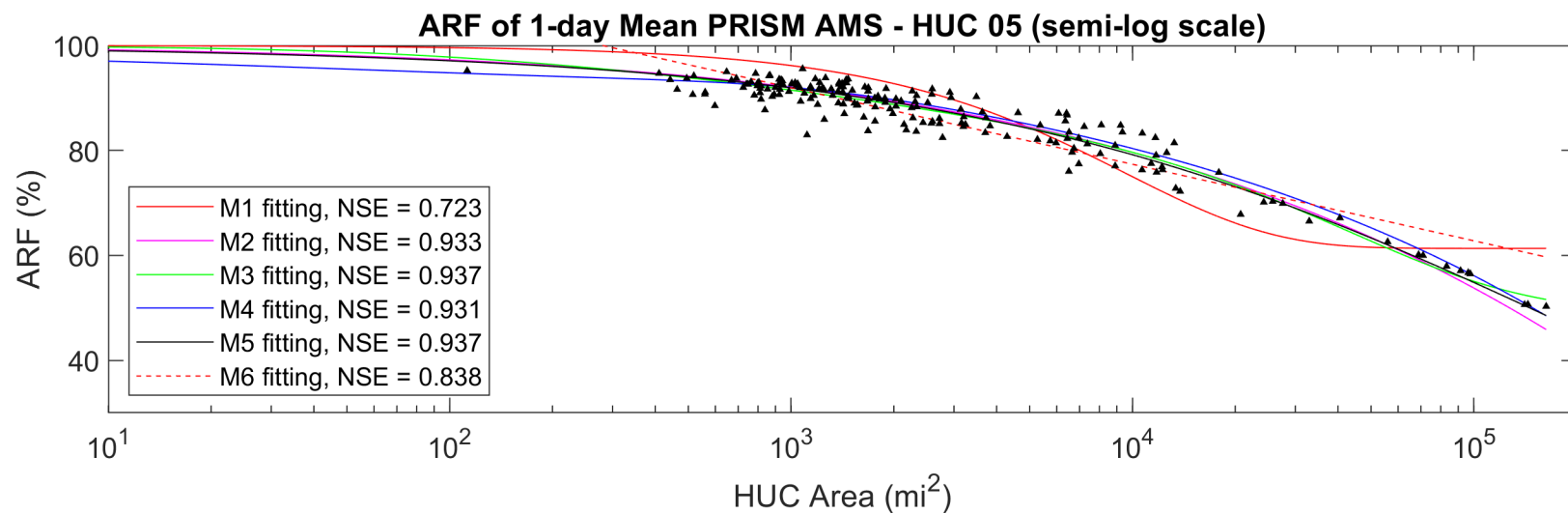
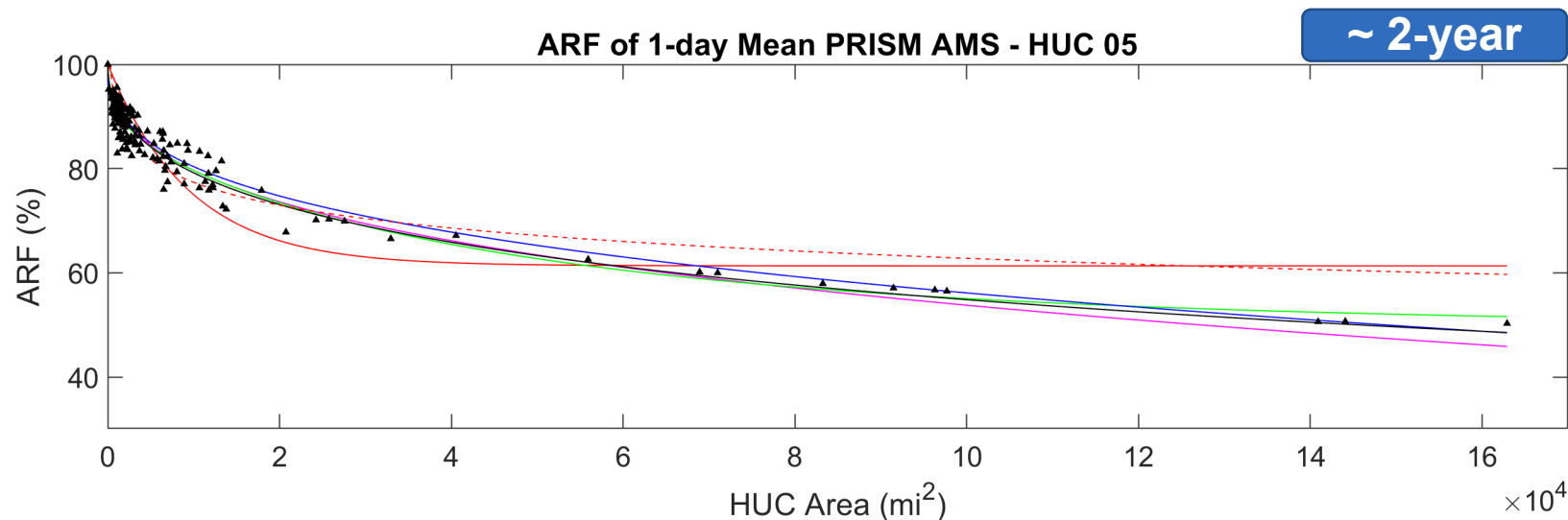
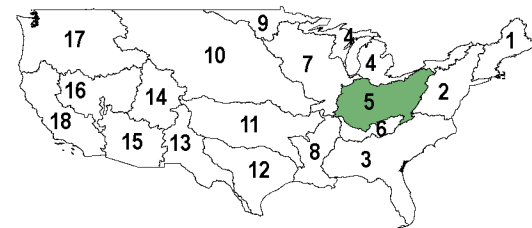


# Summary of Overall Findings

- ARF decreases with (1) decreasing duration, (2) increasing area, and (3) increasing return period.
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- For data sources, smaller ARF differences are found, but the differences are not negligible.
- Cool season ARF > All season ARF > Warm season ARF
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# Region 05 Overall M1–M6 Comparison

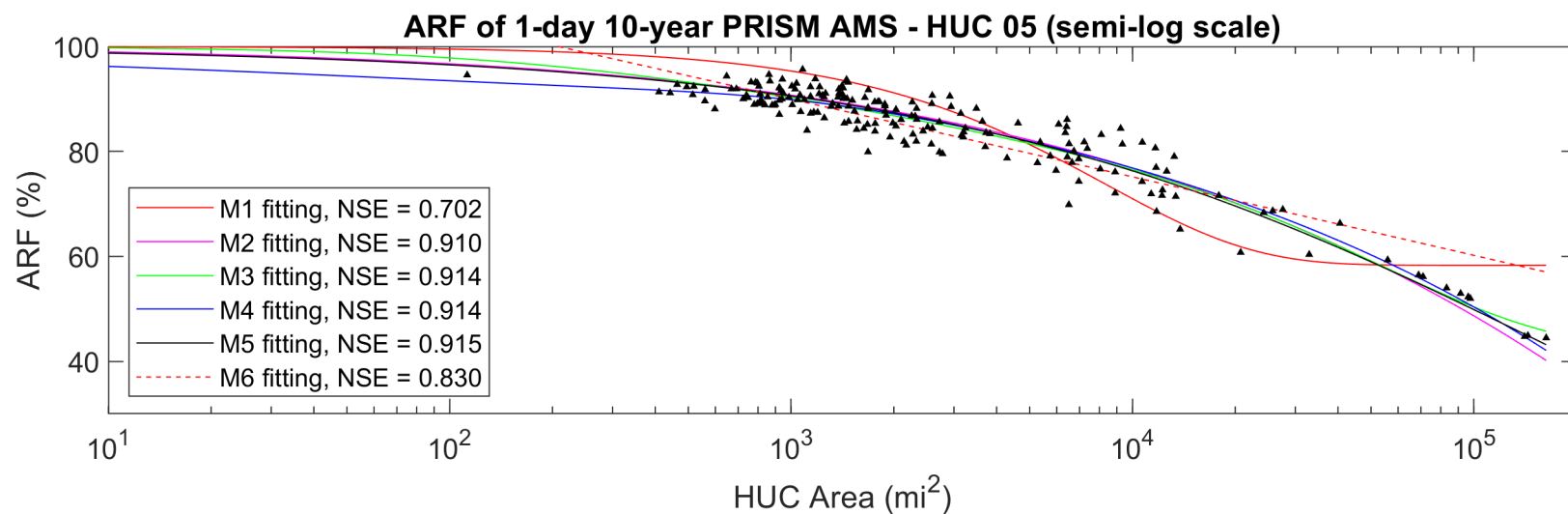
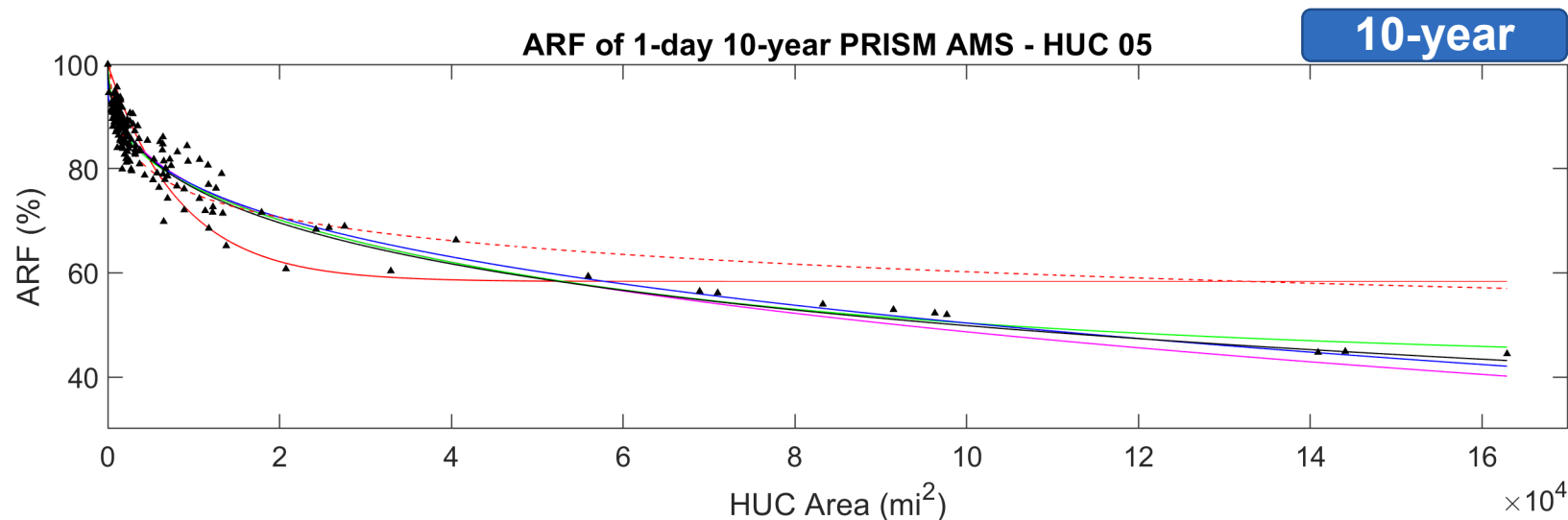
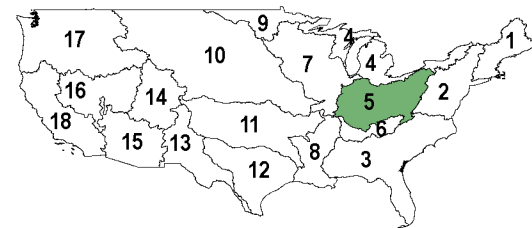
- Data: PRISM (all seasons)
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- ARF Fitting: M1–M6





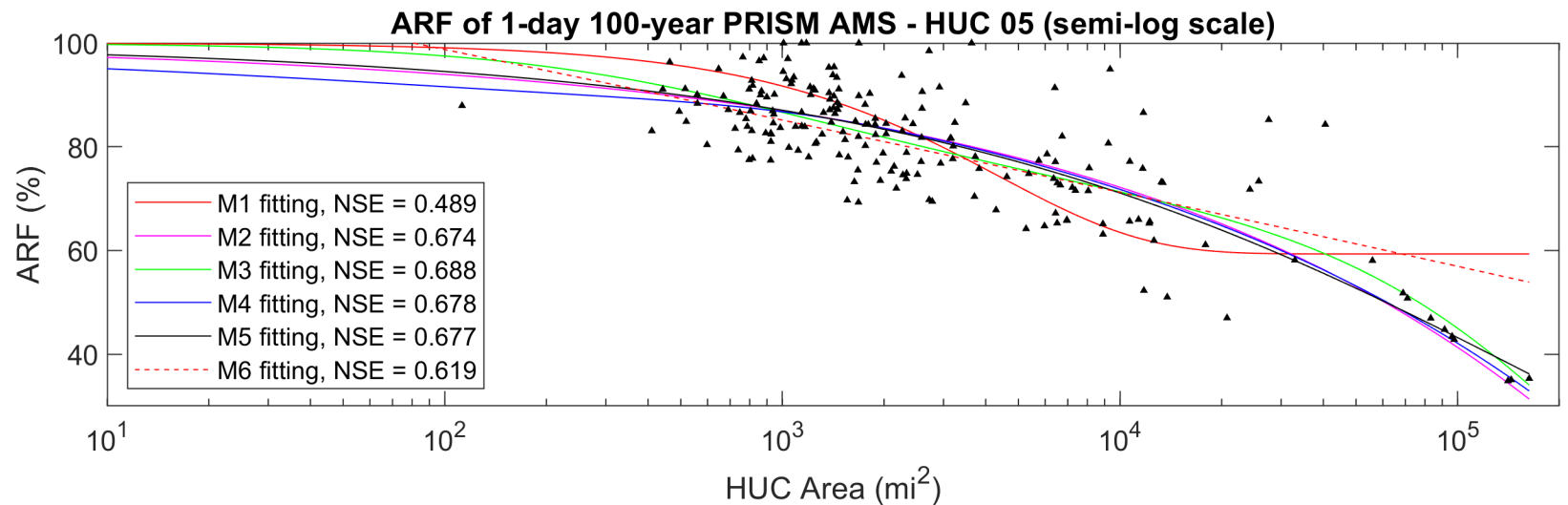
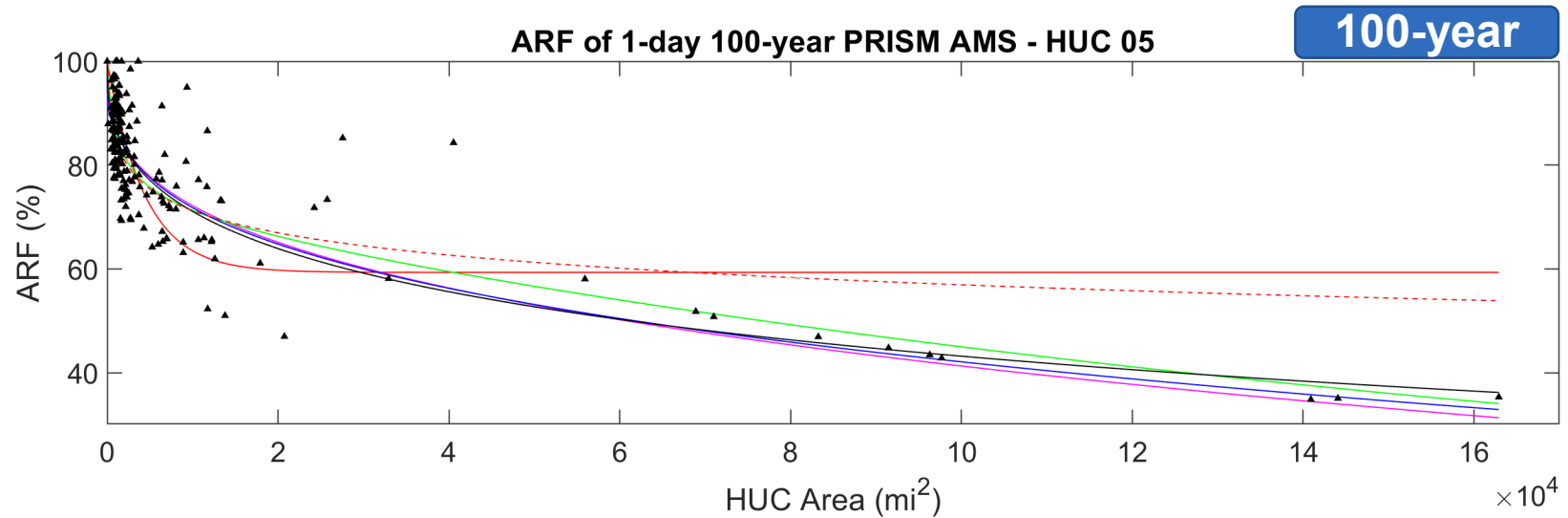
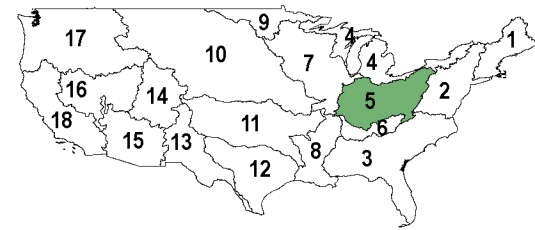
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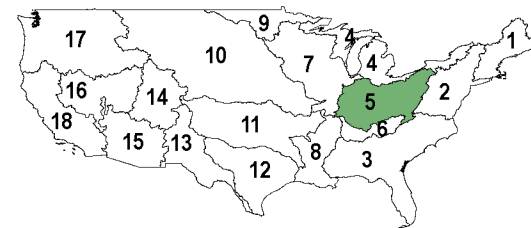
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- Duration: 1-day, 2-day, 3-day
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- ARF Fitting: M1–M6



Duration	NSE					
	M1	M2	M3	M4	M5	M6
	<b>Average AMS (approximately 2-year)</b>					
1-day	0.72	0.93	0.94	0.93	0.94	0.84
2-day	0.76	0.93	0.93	0.93	0.93	0.77
3-day	0.75	0.92	0.93	0.92	0.93	0.67
	<b>10-year</b>					
1-day	0.70	0.91	0.91	0.91	0.91	0.83
2-day	0.69	0.89	0.90	0.89	0.89	0.75
3-day	0.73	0.90	0.91	0.91	0.91	0.70
	<b>100-year</b>					
1-day	0.48	0.67	0.69	0.68	0.68	0.62
2-day	0.45	0.70	0.70	0.70	0.70	0.61
3-day	0.59	0.80	0.81	0.81	0.80	0.71

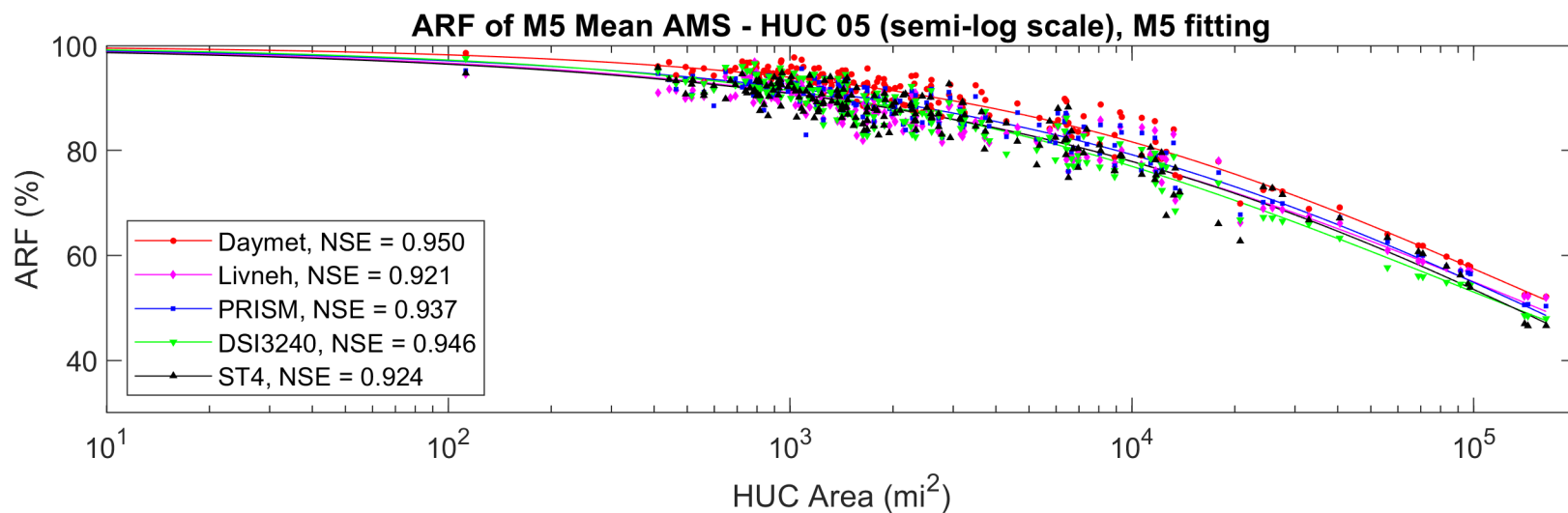
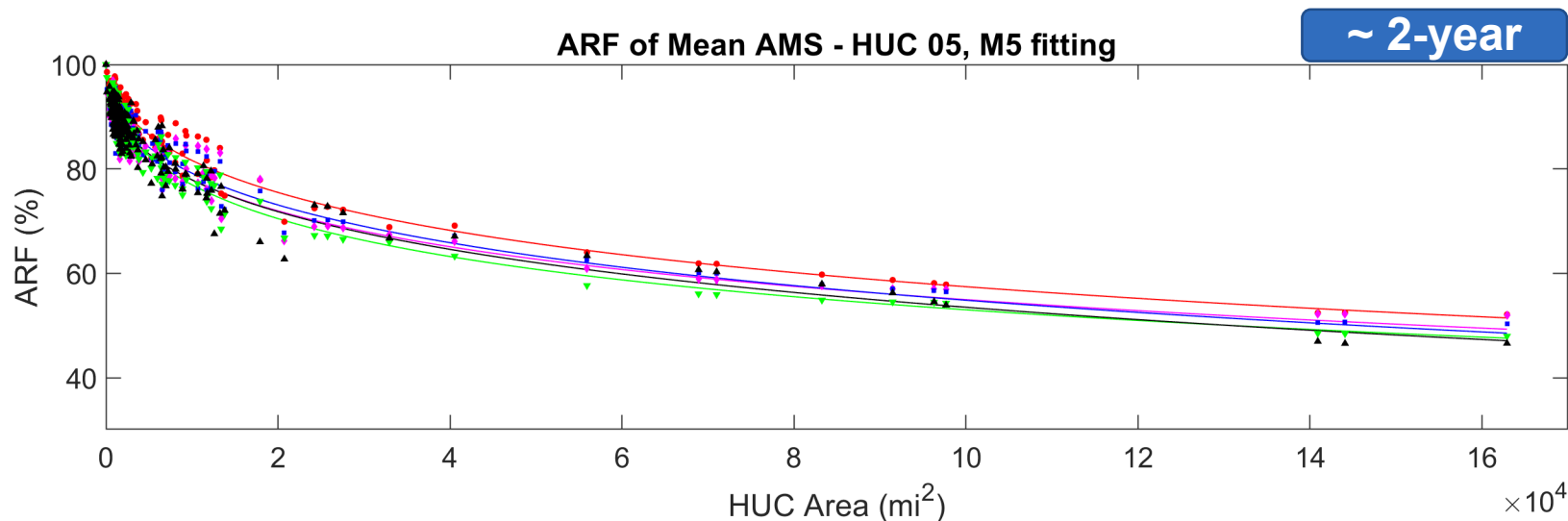
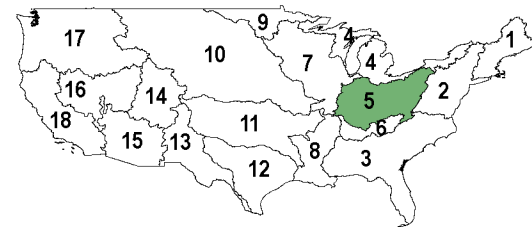
\*Red cell highlights NSE < 0.5

# Summary of Overall Findings

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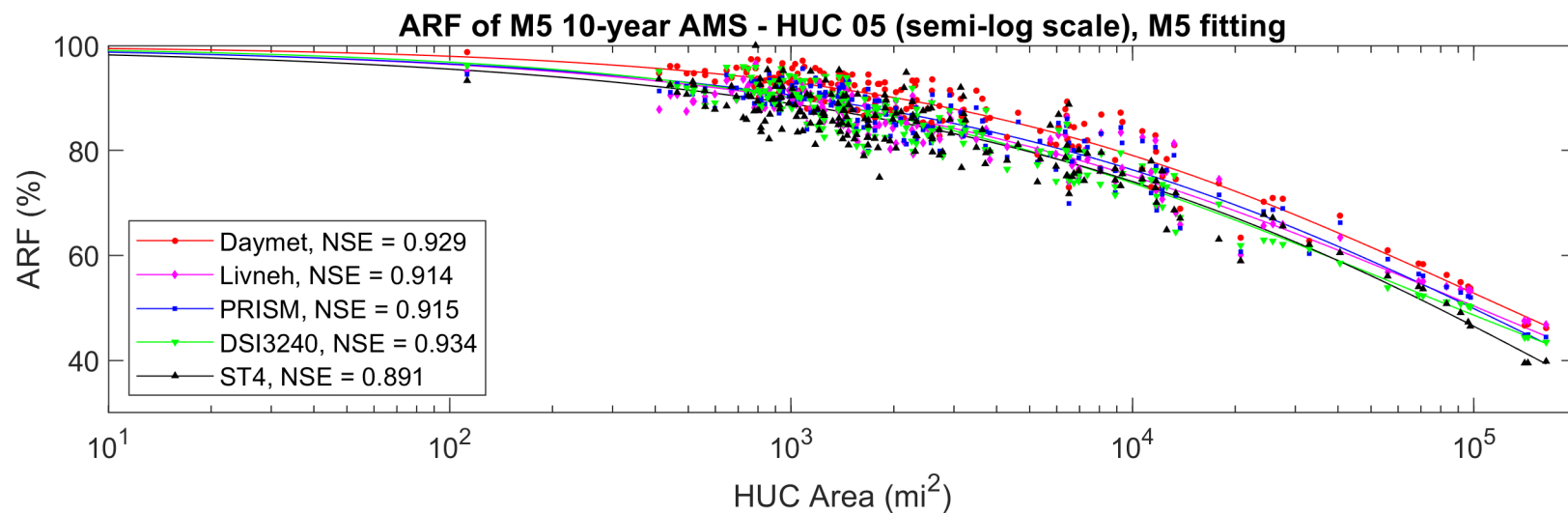
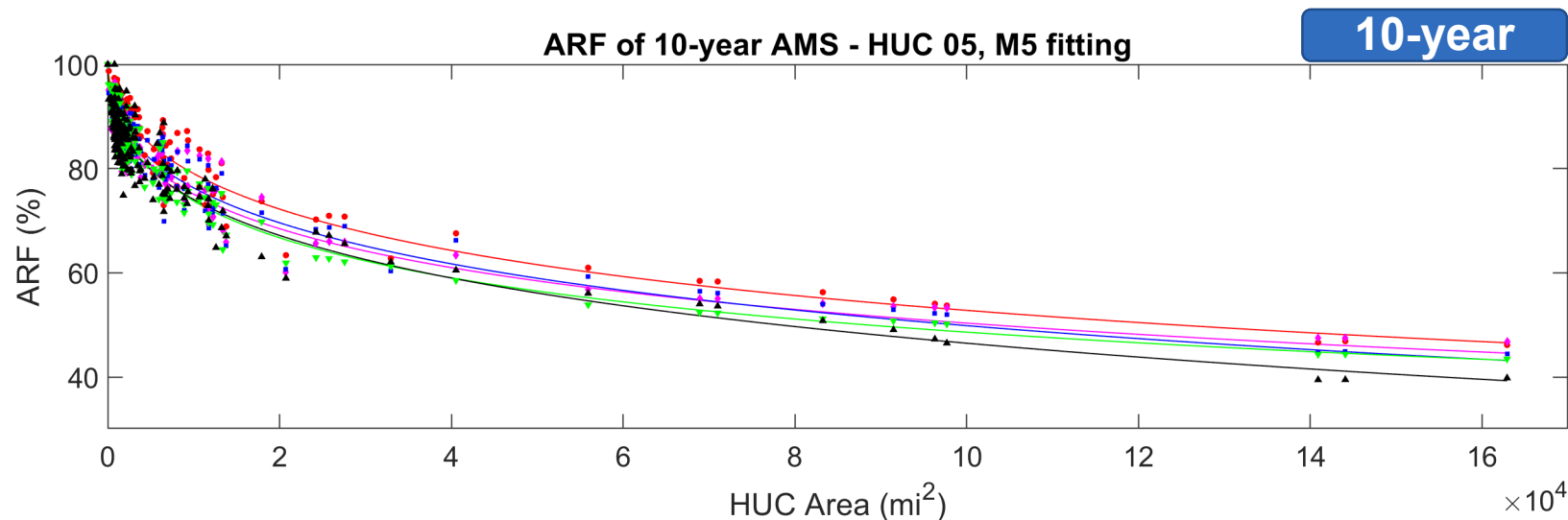
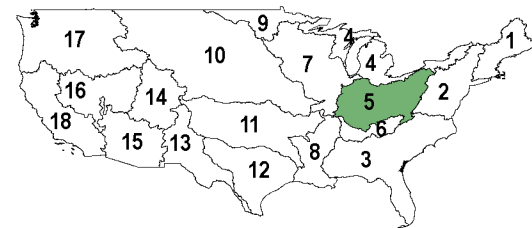
- Data: All (all seasons)
- Duration: 1-day
- Frequency level: AMS
- ARF Fitting: M5





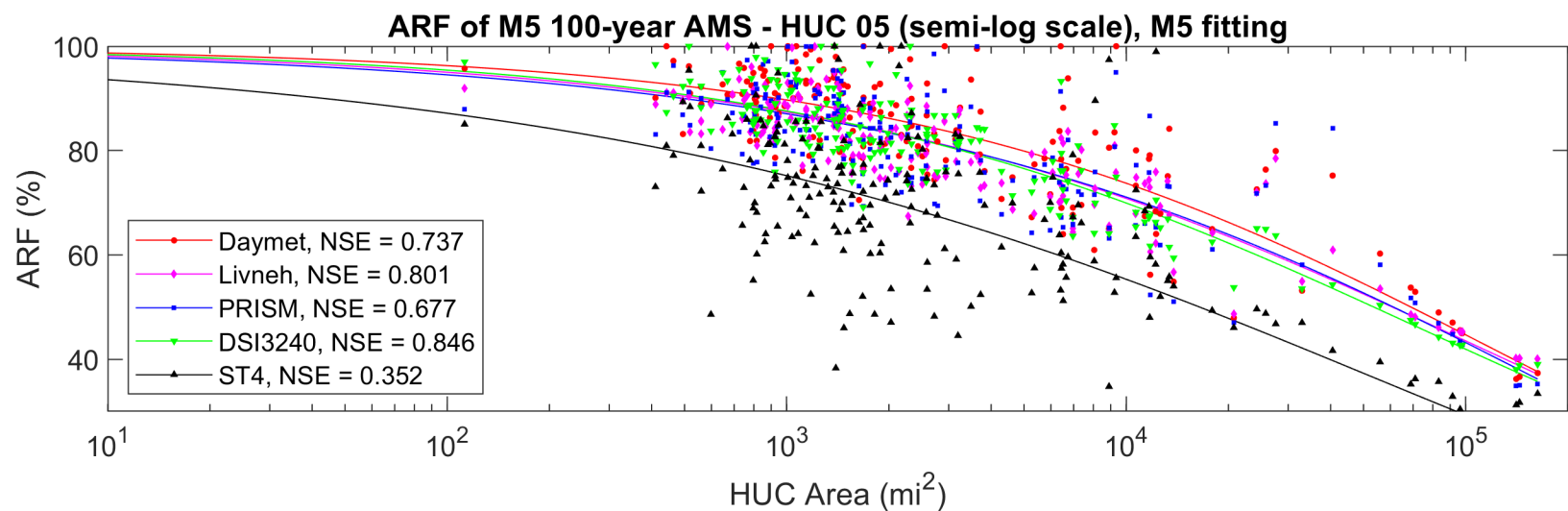
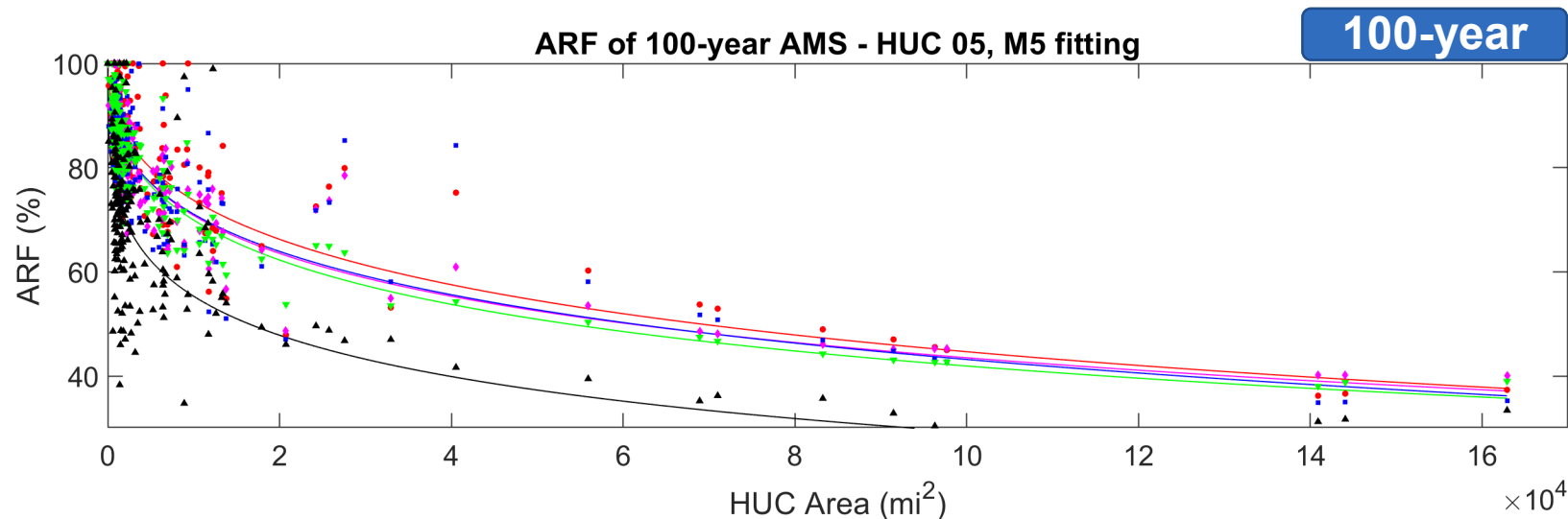
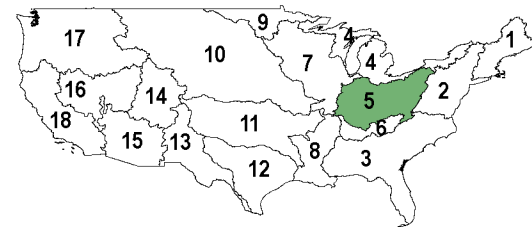
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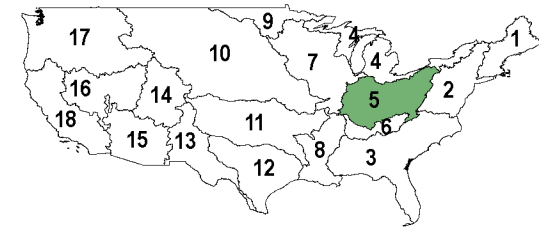
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# Region 05 Data Source Comparison

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- Duration: 1-day, 2-day, 3-day
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Duration	NSE				
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2-day	0.93	0.95	0.92	0.93	0.93
3-day	0.92	0.94	0.92	0.92	0.93
	<b>10-year</b>				
1-day	0.91	0.93	0.89	0.91	0.93
2-day	0.89	0.92	0.88	0.92	0.92
3-day	0.91	0.93	0.87	0.91	0.91
	<b>100-year</b>				
1-day	0.68	0.74	0.35	0.80	0.85
2-day	0.70	0.74	0.39	0.77	0.80
3-day	0.80	0.82	0.36	0.82	0.80

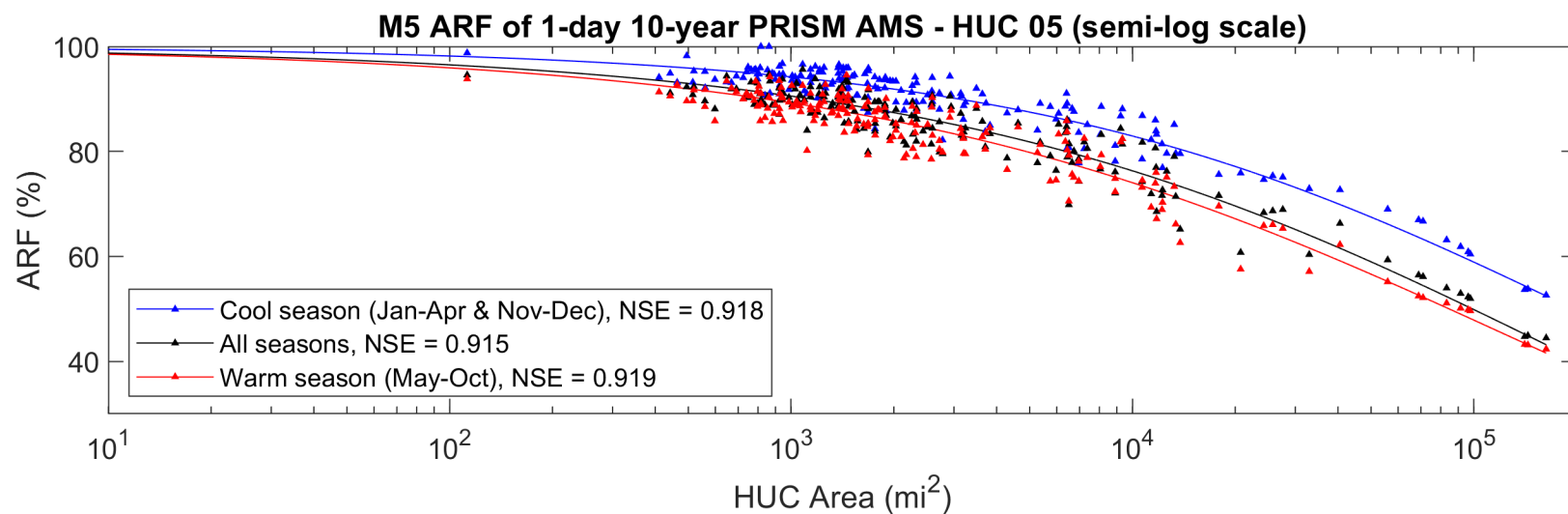
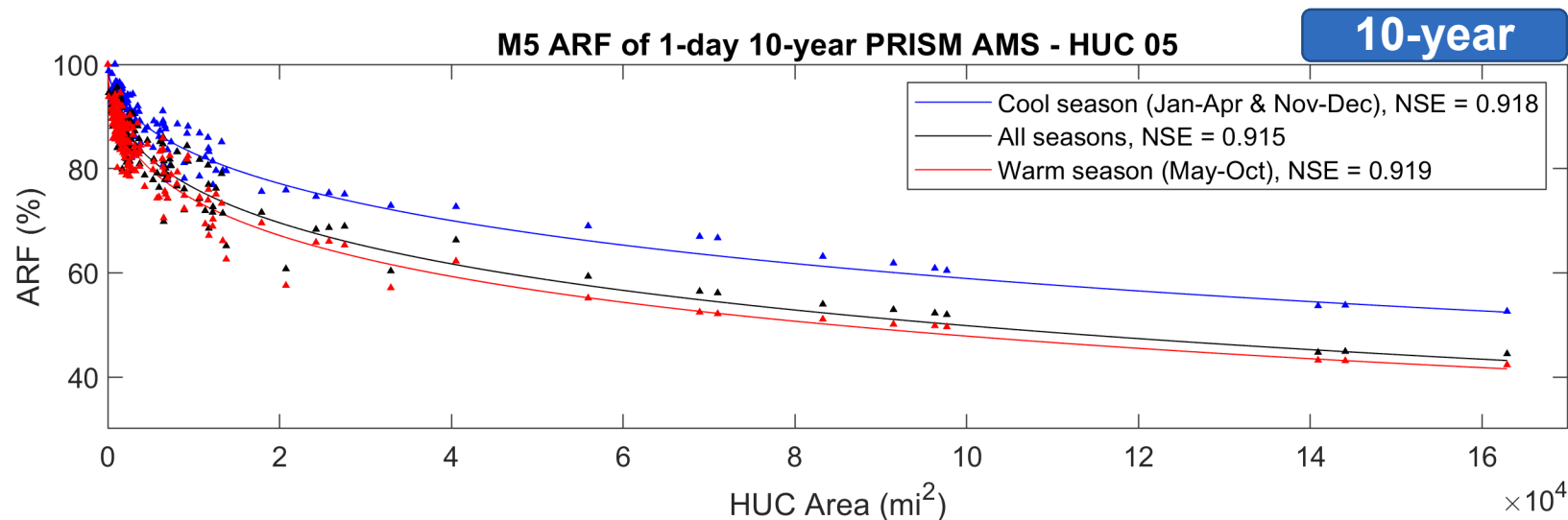
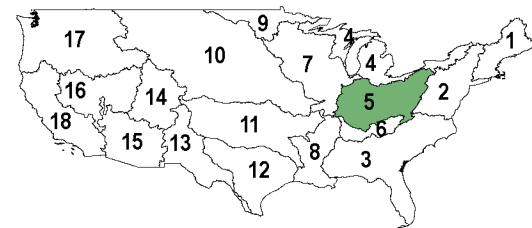
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- ARF varies across different regions. Using one set of ARF everywhere across the country is not justified.
- High return level ARF remains a major challenge, mostly due to relatively short data record length.

# Region 05 Seasonal Variability

- Data: PRISM (all, warm, cool)
- Duration: 1-day
- Frequency level: 10-year
- ARF Fitting: M5



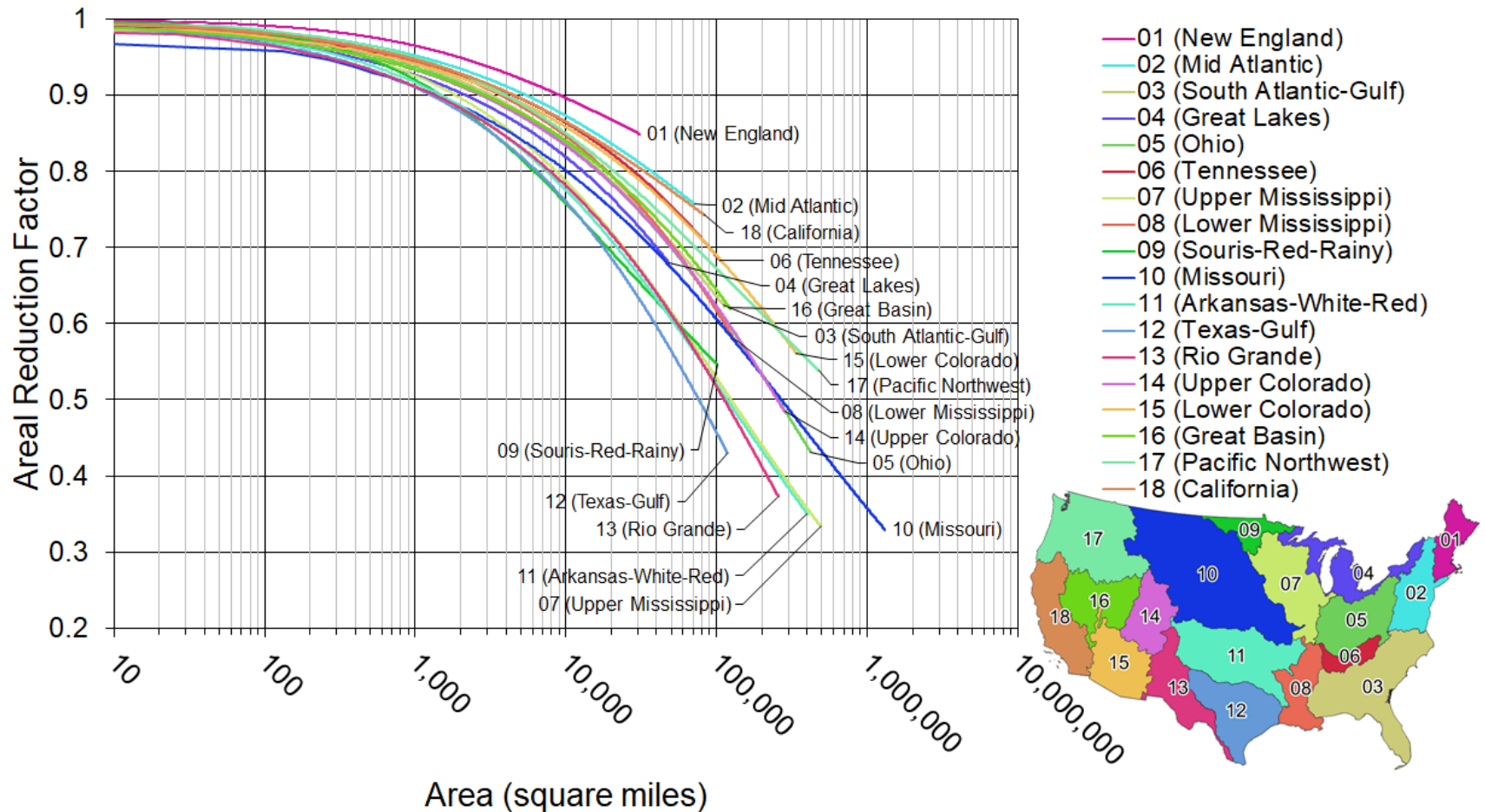


# Summary of Overall Findings

- ARF decreases with (1) decreasing duration, (2) increasing area, and (3) increasing return period.
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# National Comparison Results: 1-day 10-year

Areal Reduction Factors by HUC02 using PRISM-daily data and M5 fitting  
1-day Duration | 10-y Return Period

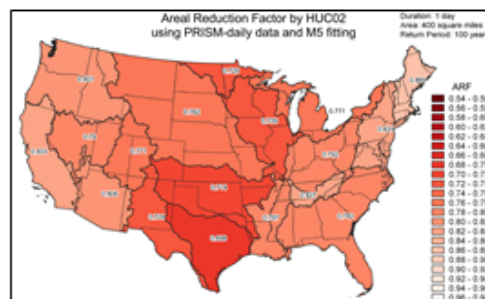
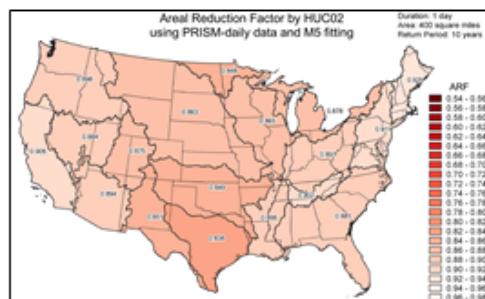
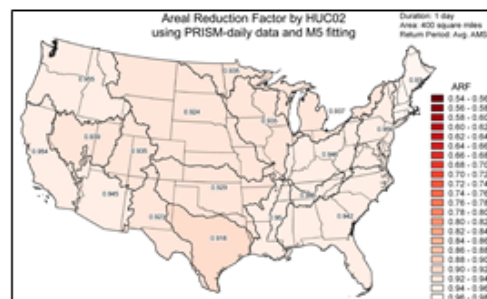


# National Comparison Results: 1-day

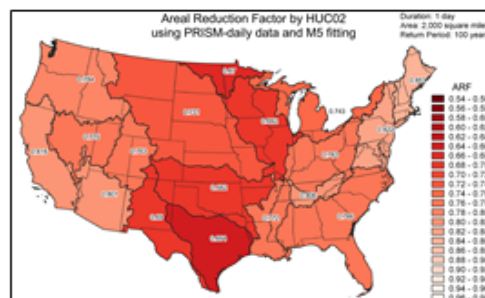
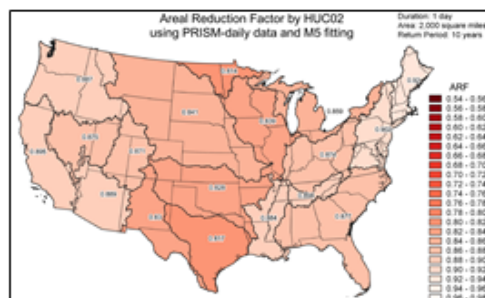
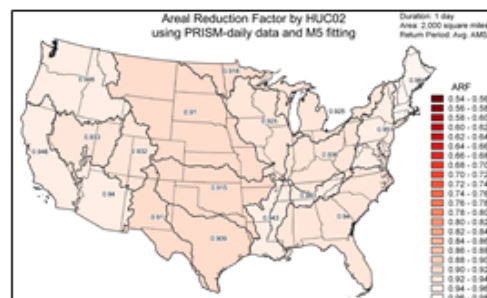
Areal Reduction Factors by HUC02 using PRISM-daily data and M5 fitting  
1-day Duration

Avg. AMS      10-y      100-y

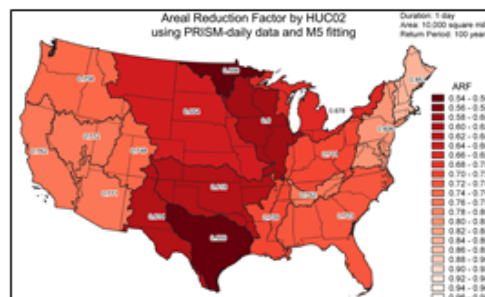
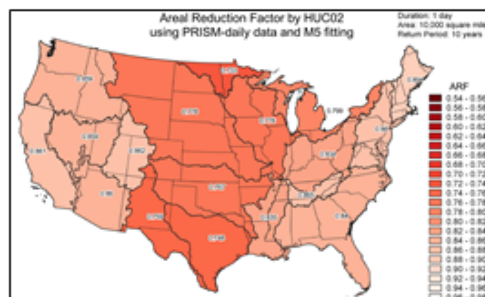
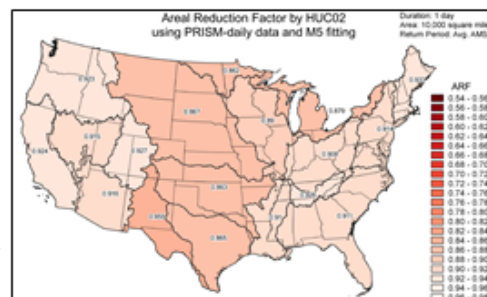
400 mi<sup>2</sup>



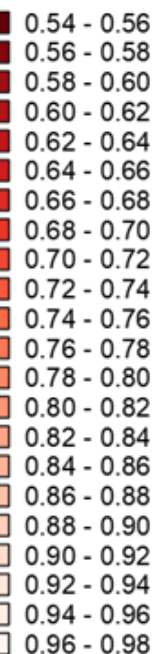
2,000 mi<sup>2</sup>



10,000 mi<sup>2</sup>



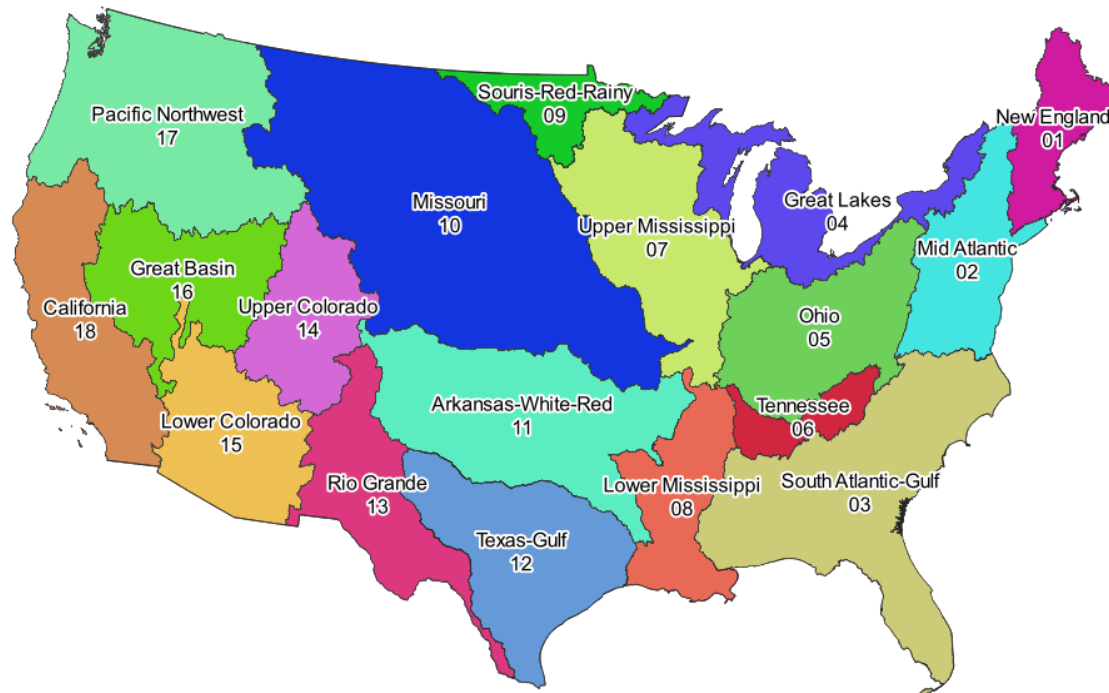
ARF



# National Comparison Results: 1-day NSE

Comparison of 1-day CONUS regional M5 ARF fitting using PRISM precipitation across different return periods.

Return Period	NSE																	
	Region Number																	
	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18
Avg. AMS	0.68	0.80	0.72	0.69	0.94	0.91	0.93	0.87	0.88	0.85	0.87	0.88	0.92	0.83	0.84	0.81	0.85	0.72
GEV 10-yr	0.66	0.67	0.72	0.58	0.91	0.89	0.90	0.83	0.85	0.78	0.81	0.89	0.90	0.81	0.79	0.77	0.84	0.74
GEV 100-yr	0.20	0.15	0.44	0.31	0.68	0.46	0.72	0.59	0.73	0.57	0.59	0.70	0.72	0.65	0.51	0.37	0.70	0.63





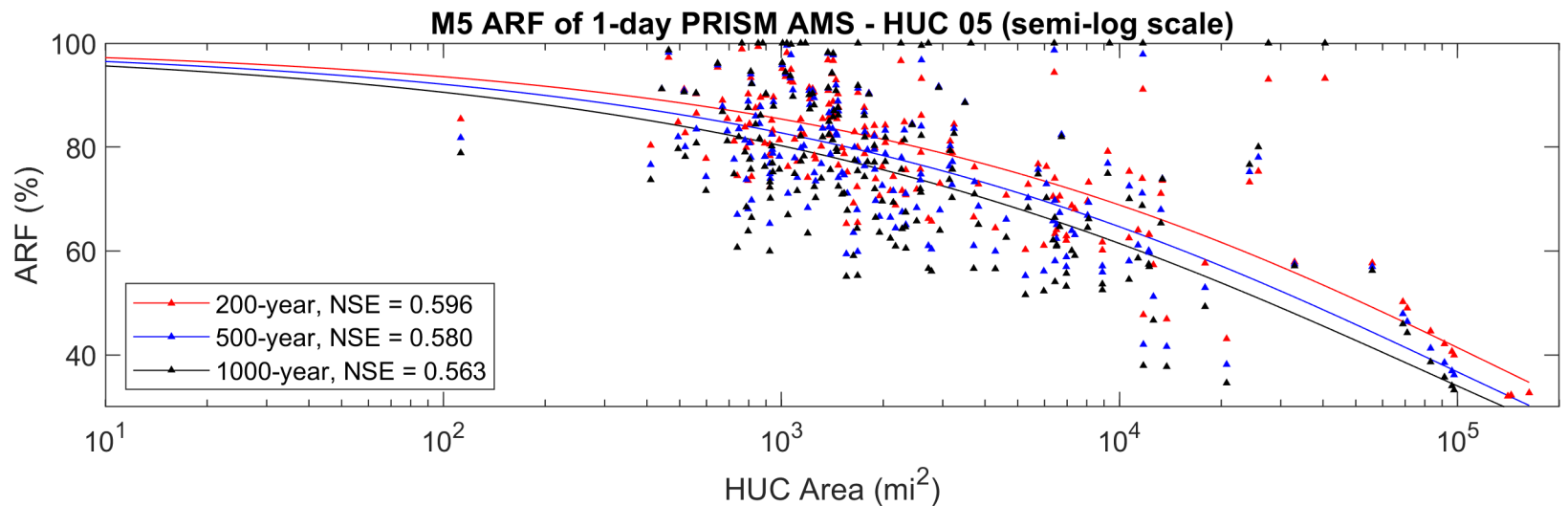
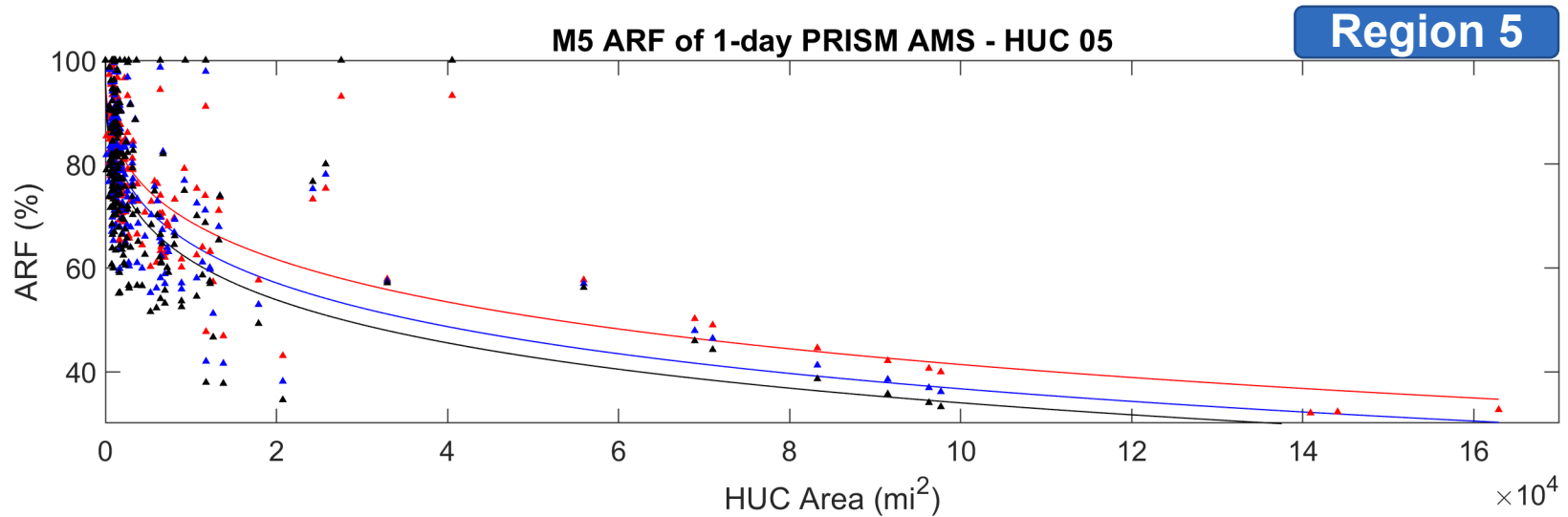
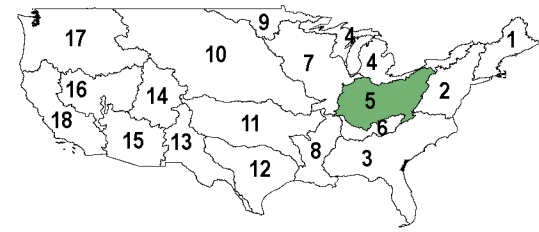
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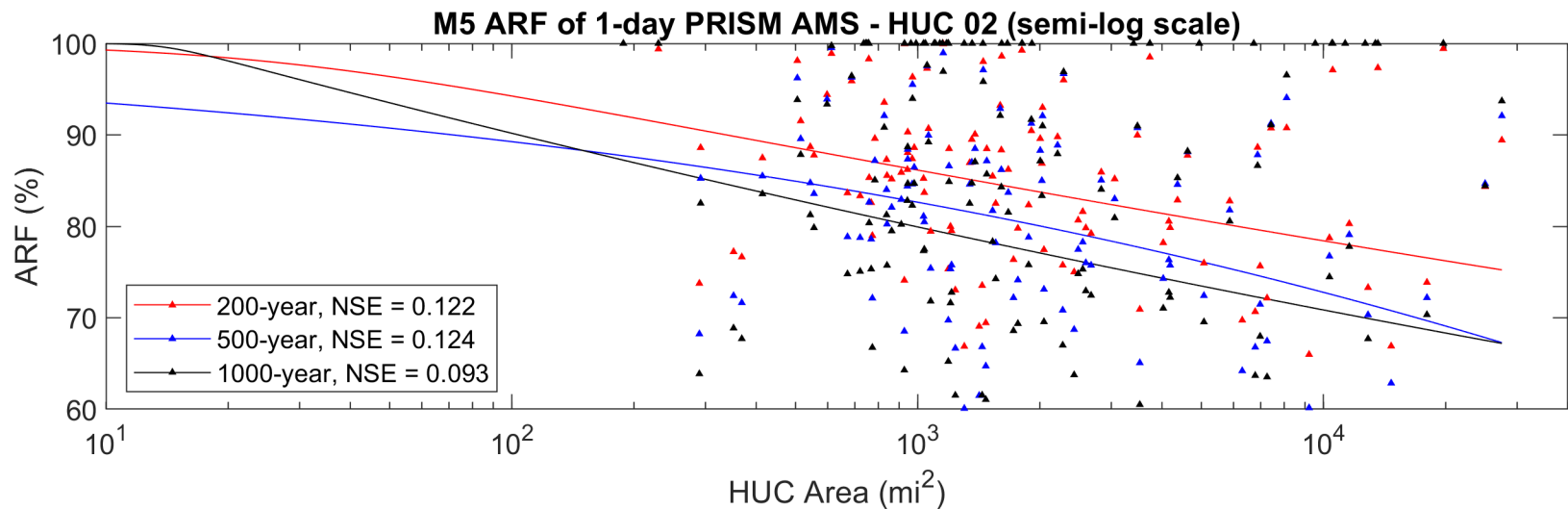
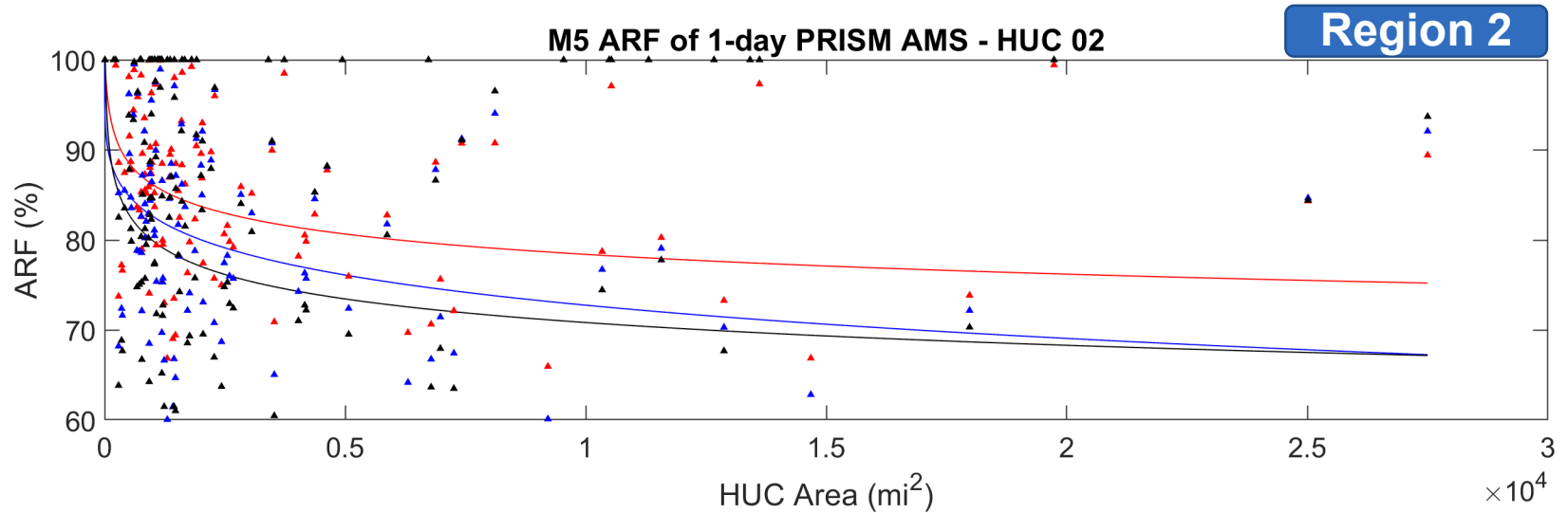
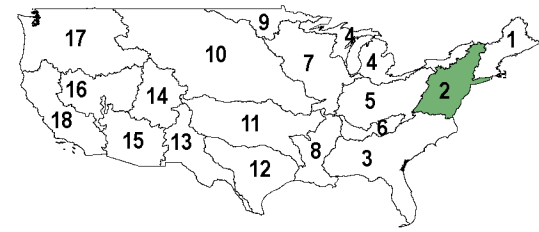
# High Return Levels

- Data: PRISM (all seasons)
- Duration: 1-day
- Frequency level: 200-year, 500-year, 1000-year
- ARF Fitting: M5



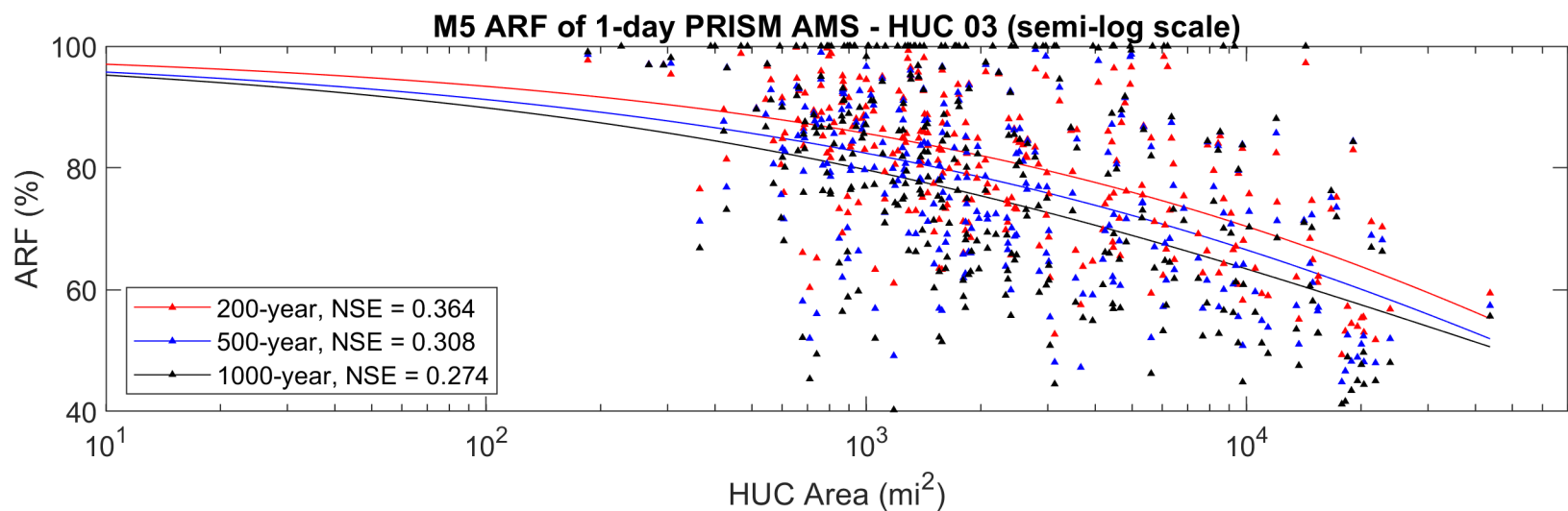
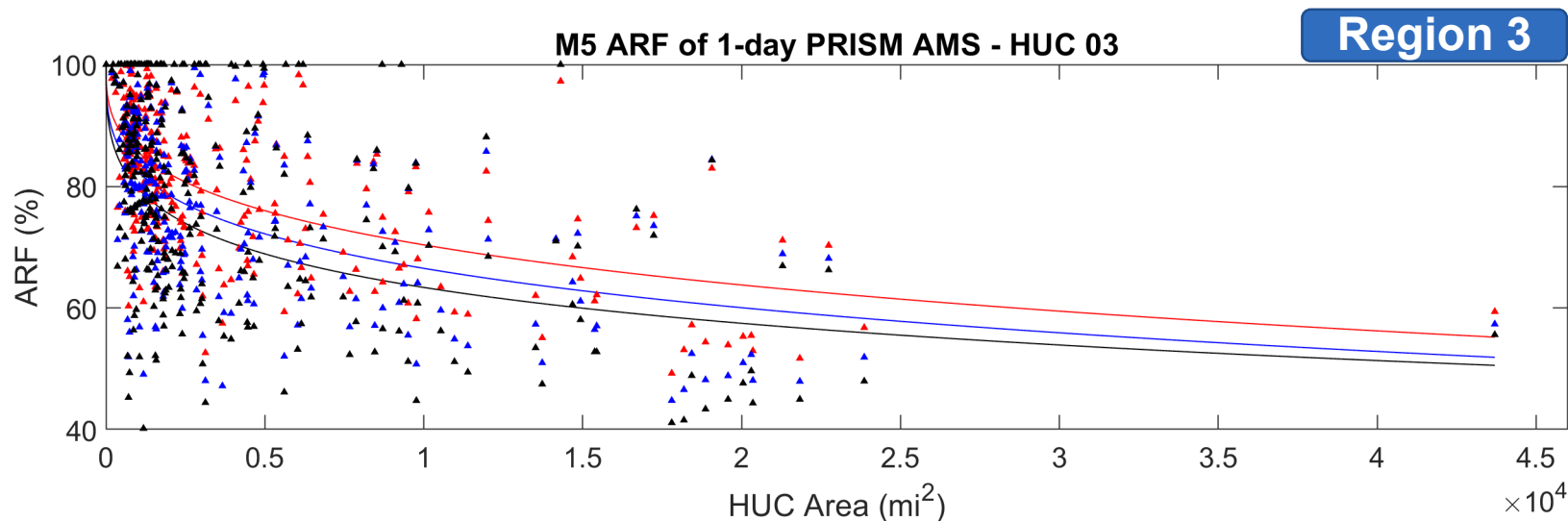
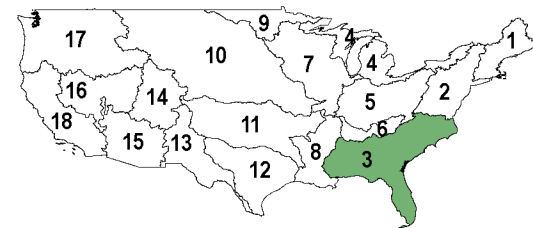
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# High Return Levels

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- Duration: 1-day
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# Issues to be Explored

- **Development of ARF for long return period**
- **Uncertainty quantification**
- **Lack of long-term, high spatiotemporal resolution dataset**
- **Subwatershed application**
- **Need for a national ARF product**

# Thank you!

# Questions?

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**Scott T. DeNeale** ([denealest@ornl.gov](mailto:denealest@ornl.gov))

