

Design Analysis
RCS Sub Cooling Margin Monitoring System
Error Analysis

Rochester Gas and Electric Corporation

89 East Avenue

Rochester, New York 14649

EWR 2604

Revision 0

January 23, 1980

Prepared by:	<u>Carl J. Reinhardt, P.E.</u> Electrical Engineer	<u>1/23/80</u> DATE
Reviewed by:	<u>G. W. Daniels</u> Manager, Electrical Engineering	<u>1/23/80</u> DATE
Approved by:	<u>G. W. Daniels</u> Manager, Electrical Engineering	<u>1/23/80</u> DATE



THE UNIVERSITY OF CHICAGO
LIBRARY
540 EAST 57TH STREET
CHICAGO, ILL. 60637

1968

1968

1968
1968
1968

1968

1968

1968

1968

Revision Status Sheet

Page	Latest Rev.
i	0
ii	0
1	0
2	0
3	0
4	0
5	0
6	0
7	0

Page	Latest Rev.
------	----------------

Page	Latest Rev.
------	----------------

Design Analysis

EWR 2604

Page ii

Revision 0

Date 1/23/80

Sub-Cooling Margin Monitoring System
Error Analysis

I. Purpose

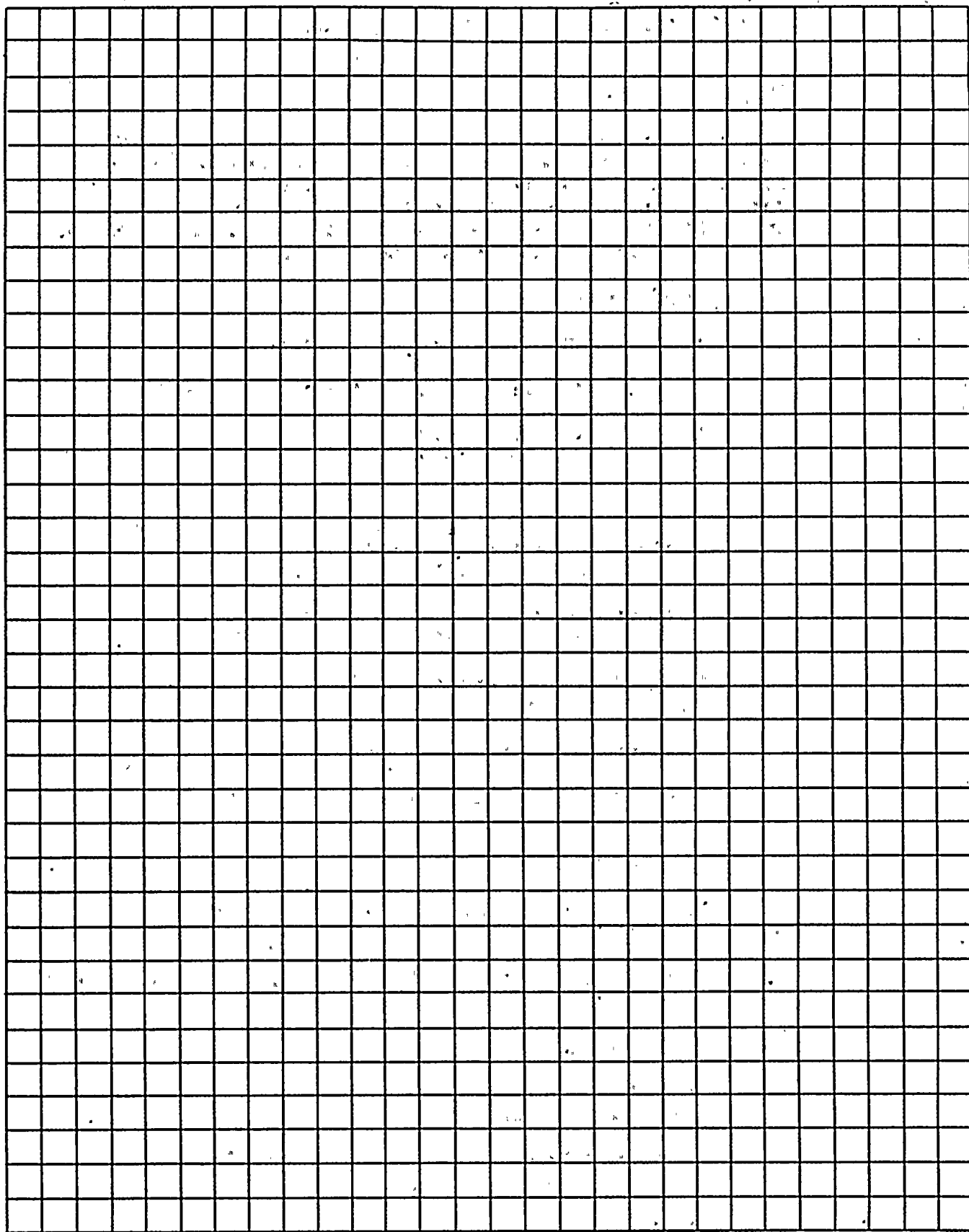
The purpose of this analysis is to compute the uncertainty in the value of RCS subcooled margin, as computed and displayed to the plant operator. This value of subcooling margin is computed by a Foxboro Spec 200 analog computer, utilizing as inputs RCS hot leg temperature and pressurizer pressure.

II. Referenced Documents

- A. Westinghouse bulletin 43-252D WE A
- B. Foxboro Company Product Specification Sheets:
 - 1. PSS 2C-2A1B 06-77
 - 2. PSS 2C-2A1C 04-77
 - 3. PSS 2C-2A1W 07-77
- C. Letter dated 12/27/79 to Westinghouse Owner's Group Representatives from R. A. Newton of Wisconsin Electric Power Company
- D. Rosemount Engineering Company drawing 176JA, Rev. C dated 12/23/66.
- E. "Signal Characterizer Calibration", Rev. 0, Foxboro Company.
- F. RG&E drawing 21489-297, Rev. 0
- G. RG&E drawings 21489-303, Rev. 1, and 21489-302, Rev. 1
- H. 1967 ASME Steam Tables
- I. Letter dated 2/15/78 from J. D. Woodward W, to J. Arthur
- J. Foxboro Instruction Sheet 18-232 for 66B Current Repeater

III. Computer Programs

- A. "Curvfit" BASIC - least squares polynomial curve fitting program.
- B. "Rootr" - BASIC - cracsk polynomials.



IV.

Assumptions

- A. Only the pressure transmitter (PT) and temperature transmitters are located inside containment, and are therefore subject to the accident environment. All other equipment is therefore assumed to be functioning under normal conditions of temperature, humidity, radiation, electrical voltage and frequency.
- B. Reference D above, states that all material used in construction of the RTD's can withstand temperatures to 650°F. In addition leadwire resistance compensation is included in the resistance to voltage converter. Therefore, the accident environment has a negligible effect on the RTD, and conversion circuitry.
- C. Errors due to calibration error are considered negligible, for the Foxboro Spec 200 equipment, since these units were factory calibrated, and have better accuracy than that stated in reference B. The calibration errors for the Foxboro 66BR are assumed to have a negligible effect on system accuracy.
- D. Accuracy and repeatability values are in terms of calibrated span, unless otherwise noted.
- E. Accuracy and repeatability errors are summed for conservatism.

V.

Analysis

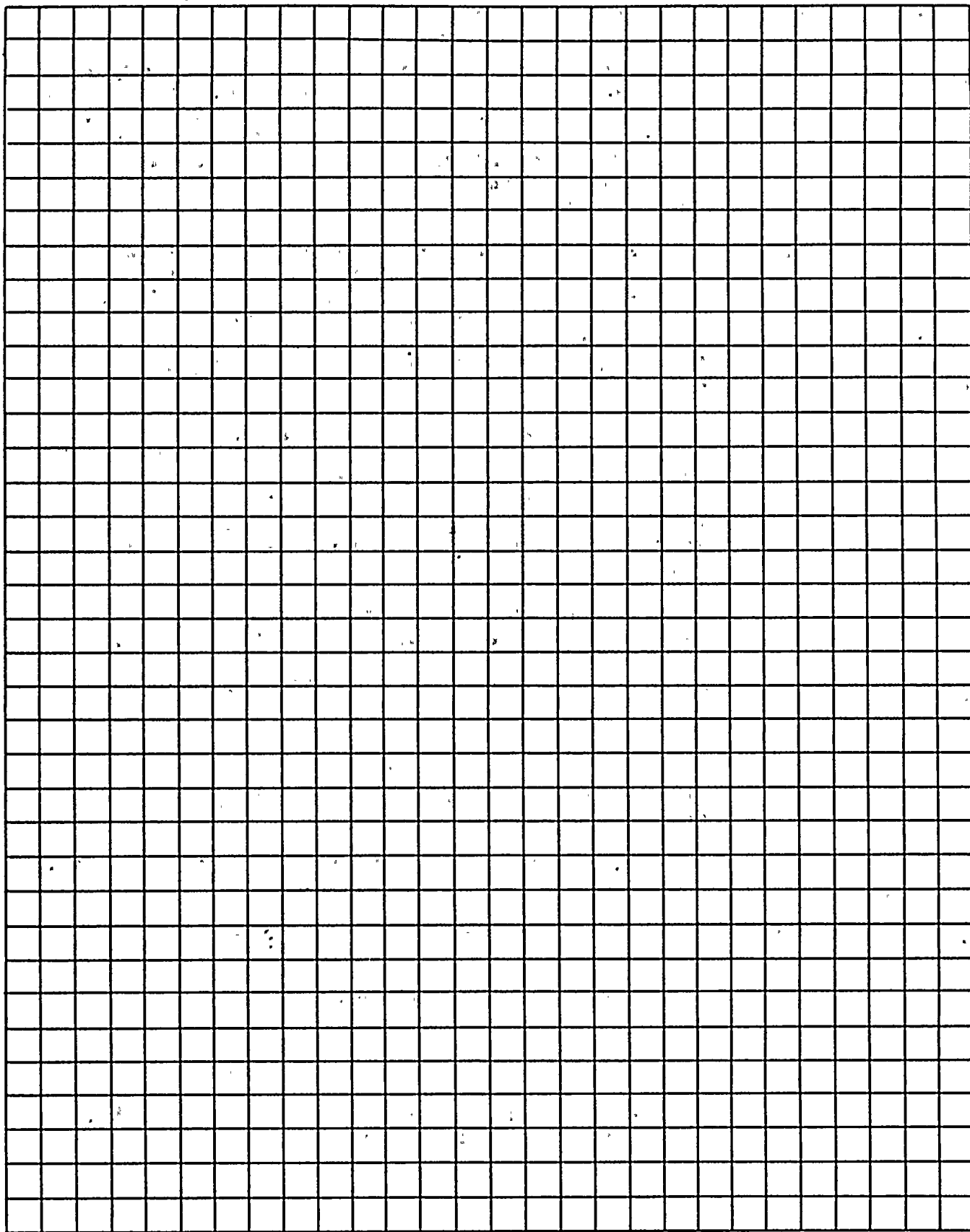
- A. This analysis utilizes some of the procedures outlined in reference C above.
- B. Instrument accuracies (refer to attached diagram #1).

- 1. Pressure transmitters (Foxboro E11GM) from ref. C. page B-2

Maximum normal instrument error =

$$\sqrt{5(4)^2 + 3^2 + 2(8)^2} = \pm 14.7 \text{ psi}$$

Maximum instrument error under accident conditions = ± 68 psi, (from ref. I).



2. Isolation amplifiers (Foxboro 66BR-OH) from ref. J accuracy $\pm 0.5\%$, repeatability = 0.1%
Total error = $\pm 0.6\%$
 $\pm 0.6\% (2500-1700) = \pm 4.8 \text{ psi}$
3. Current to voltage converter (Foxboro Spec. 200 2AI-I2V) from ref. b
accuracy = $\pm 0.25\%$ repeatability $< 0.1\%$
Total error = $\pm .35\%$
 $= \pm .35\% (2500-1700) = \pm 2.8 \text{ psi}$

4. Therefore the total normal error present at the input of the function generator is:

$$= \sqrt{(14.7)^2 + (4.8)^2 + (2.8)^2} = \pm 15.72 \text{ psi}$$

Under accident conditions total error =
 $15.72 + 68 = \pm 83.72 \text{ psi}$

This error in the pressure signal must now be transformed into equivalent error present at the output of the function generator. To do this, the steam tables between 1700 psig and 2500 psig must be modeled. Using the "Curvfit" program and steam table data (ref. H) the following polynomial was developed:

$$T_{\text{SAT}} = 1.4172591\text{E-}4 + .96584976 \times P - 6.1328799\text{E-}4 \times P^2 + 1.8916803\text{E-}7 \times P^3 - 2.2256878\text{E-}11 \times P^4$$

maximum error = $+ .0291\%$ in modeling the steam tables

The first derivative of this equation may be used to compute the error in the saturation temperature as a function of the error in the pressure signal, hence:

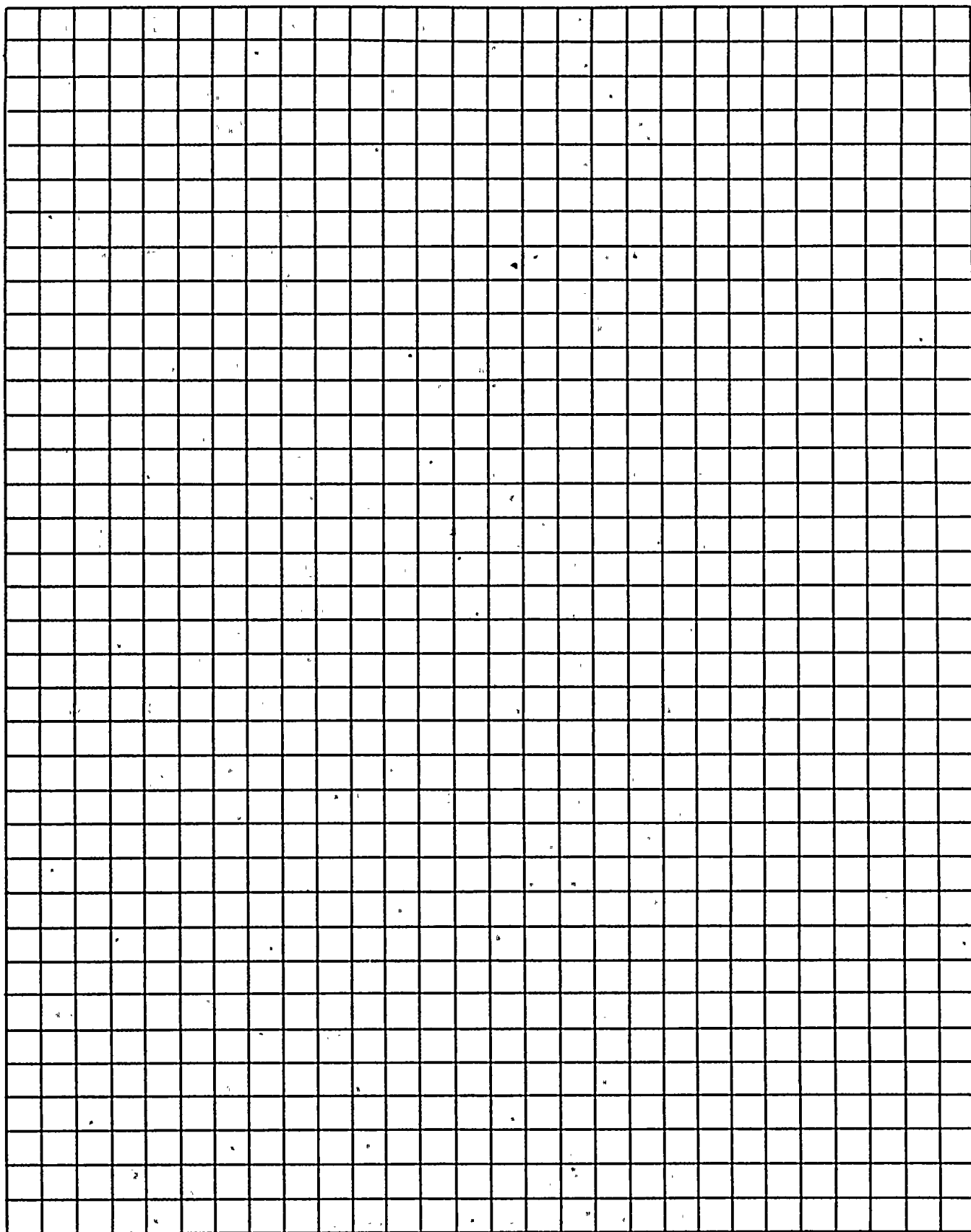
$$\Delta T_{\text{SAT}} (\text{max}) = \Delta P \times f' (P_m)$$

$\Delta P = \text{Pressure error}$
 $P_m = 2000 \text{ psig (S.I. termination)}$

$$\therefore \frac{dT_{\text{SAT}}}{dP} = .96584976 - 1.22657598\text{E-}3 \times P + 5.670409\text{E-}7 \times P^2 - 8.9027512\text{E-}11 \times P^3$$

$$\text{hence } \Delta T_{\text{SAT}} = 83.72 \times f' (2000 + 14.7) = 5.87^\circ\text{F}$$

This would be the error in the output of the function generator if: 1) the steam tables were modeled with no error, and 2) there were no inaccuracies in the function generator.



Reference E, defines the function that was programmed into the function generator by Foxboro. To compare this curve with the steam tables, it is necessary to develop the polynomial for the steam tables adjusted for scaling, spanning and zeroing. This new function can then be used to compare the Foxboro calibration points with equivalent values from the steam tables. The results of these computations are shown on page 7.

The result of this computation shows that the maximum error is -2.24%, (note: all errors are negative and therefore conservative). This error also occurs at approximately 1710 psi and therefore will be used for conservatism.

$$\begin{aligned}\text{error} &= -2.24\% (669-614.3^{\circ}\text{F}) \\ &= -1.23^{\circ}\text{F}\end{aligned}$$

The error due to inaccuracies of the function generator are:

$$\begin{aligned}\text{accuracy} &\pm 0.5\% \text{ repeatability} = 0.25\% \\ \text{total error} &= \pm 0.75\% (669-614.3^{\circ}\text{F}) \\ &= \pm .41^{\circ}\text{F}\end{aligned}$$

The errors present are therefore

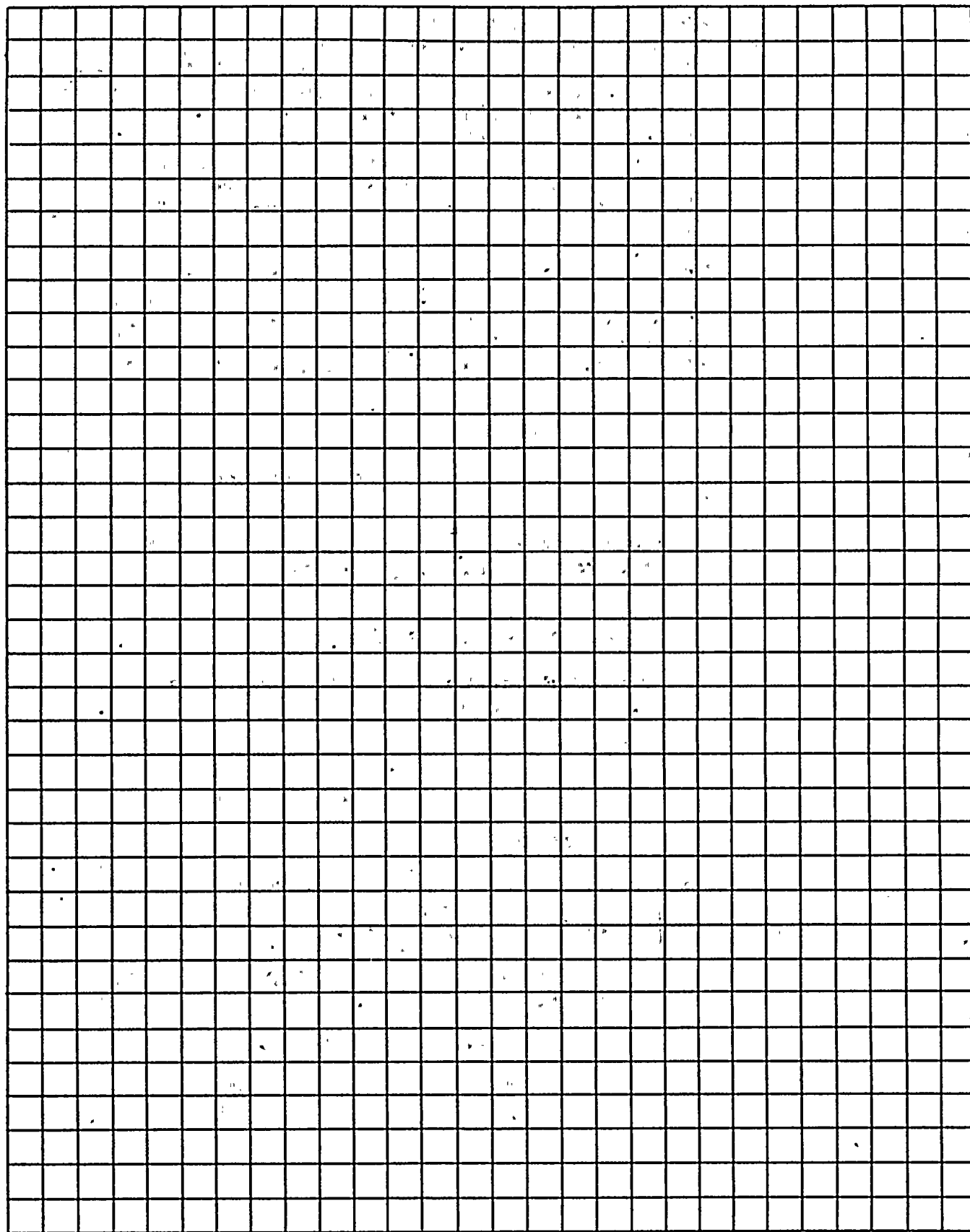
- a) $\pm 5.87^{\circ}\text{F}$ due to errors propagated by the pressure signal
- b) -1.23°F due to error in steam table modeling
- c) $\pm .41^{\circ}\text{F}$ due to "electronic" drifting

These errors are each generated by a separate random process, therefore, the total error at the output of the function generator is:

$$\sqrt{(5.87)^2 + (1.23)^2 + (.41)^2} = \pm 6.01^{\circ}\text{F}$$

- 5. Temperature transmitter (RTD) (Rosemount 176JA) Reference D lists the accuracy as

<u>Temperature °F</u>	<u>Accuracy \pm °F</u>
32	.011
525	.055
625	.065



Repeatability $\therefore 2^{\circ}\text{F}$ or 1% of span whichever is greater

$$\therefore \text{error} = .065 + 1.0\% \times (700-500) = \underline{\pm 2.065^{\circ}\text{F}}$$

6. Resistance to voltage converter (Foxboro 2AI-P2V) from ref. B, accuracy $\pm .25\%$, repeatability $< 0.1\%$
error = $\pm .35\%$ (700-500)
= $\pm .7^{\circ}\text{F}$

Total error at input of summer from temperature measurement and conversion =

$$\sqrt{(2.065)^2 + (.7)^2} = \underline{2.18^{\circ}\text{F}}$$

7. The signal present at summer inputs are

- 1) $T_{\text{HOT}} \pm 2.18^{\circ}\text{F}$
2) $T_{\text{SAT}} \pm 6.01^{\circ}\text{F}$

Since both these errors are generated by separate, random processes, the total error as a result of the summing function is

$$\sqrt{(6.01)^2 + (2.18)^2} = \underline{\pm 6.39^{\circ}\text{F}}$$

8. The error introduced by the summer itself is:
accuracy $\pm 0.5\%$, repeatability $< .25\%$ (Ref. B)

$$\text{error} = \pm .75\% (100^{\circ}\text{F}) \\ = \underline{\pm .75^{\circ}\text{F}}$$

10. The error from the indicator (W V252) is
accuracy $\pm 1.5\%$, readability $\pm 1/2$ of division

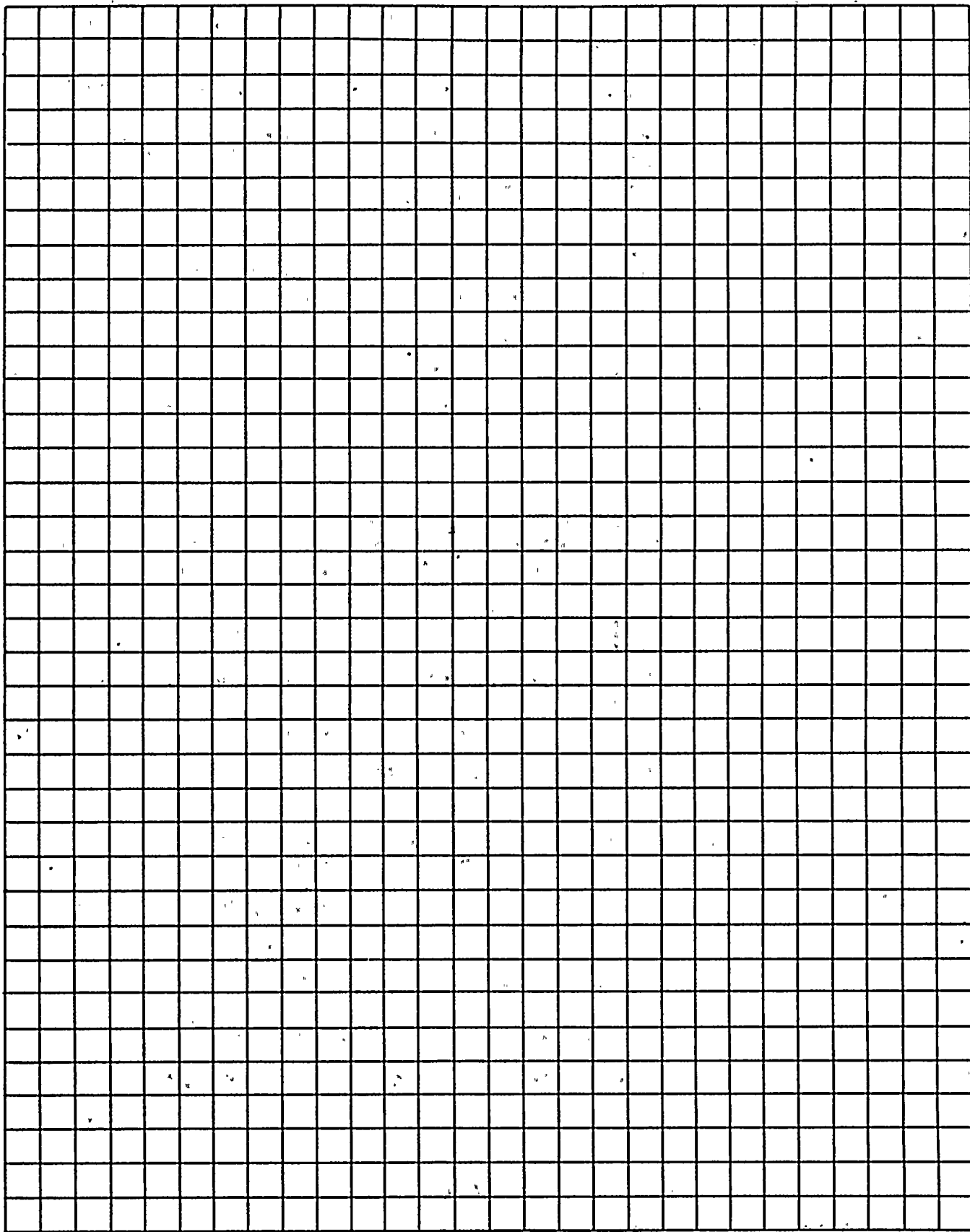
$$\text{error} = 1.5\% (100-0^{\circ}\text{F}) = \underline{\pm 1.5^{\circ}\text{F}} \text{ (accuracy)}$$

$$\text{error} = \pm 1/2 \text{ division} \times \frac{2^{\circ}\text{F}}{\text{division}} = \underline{\pm 1^{\circ}\text{F}}$$

11. The total process error is therefore the square root of the sum of the squares of the errors computed in sections 7, 8, 9, and 10 above

Total system error =

$$\sqrt{(6.39)^2 + (.75)^2 + (1.5)^2 + (1.0)^2} = \underline{\underline{\pm 6.71^{\circ}\text{F}}}$$



VI.

Conclusion

From the foregoing analysis, the maximum error in the value of subcooling margin is 6.7°F .

DESIGN ANALYSIS

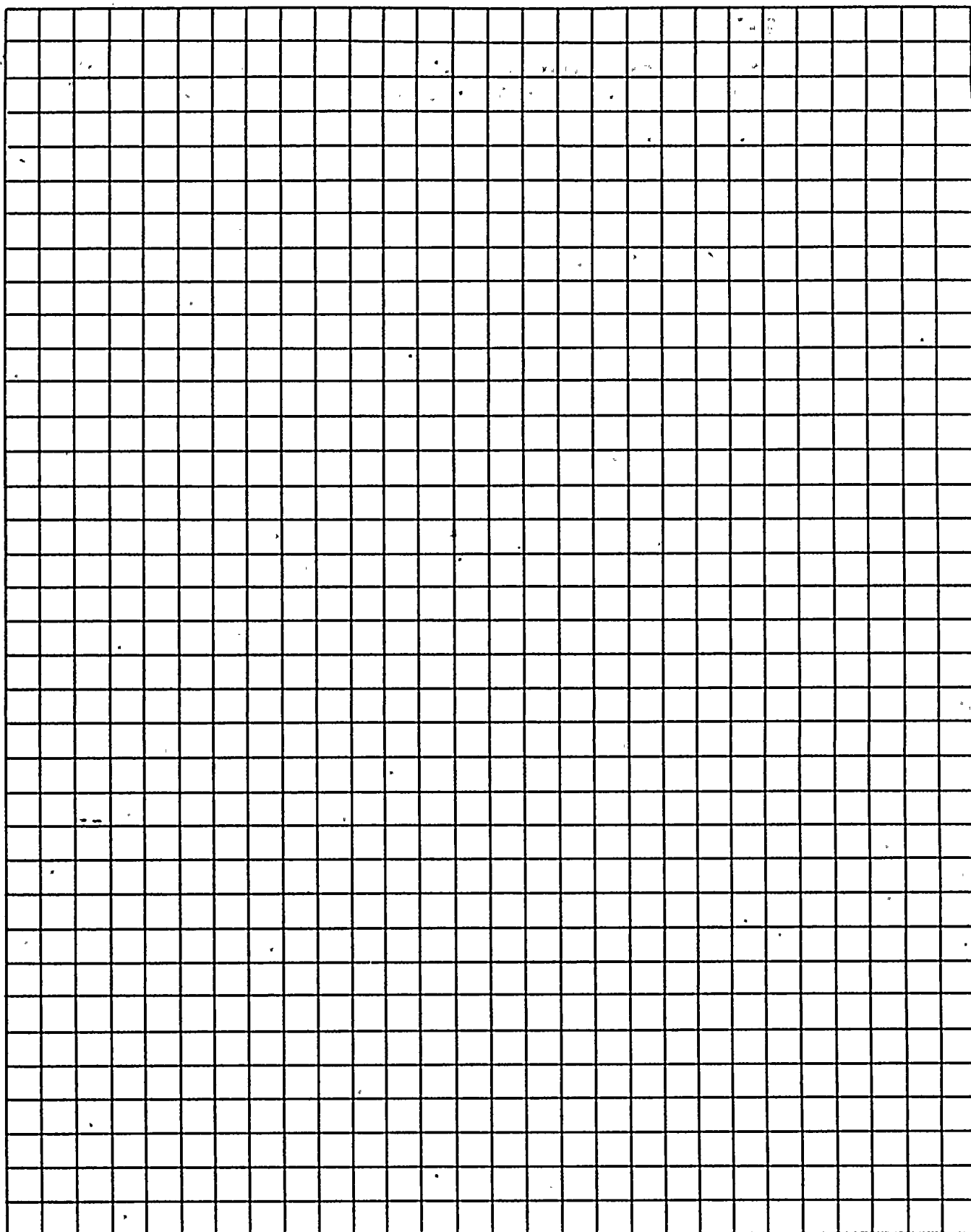
EWR NO. 2604

PAGE 6 of

REV. 0

DATE 1/23/80

42-60
REV. 2/77



X	Y	FNA(X)	FNA(X)-Y	% ERROR
0	5.71	5.584865	-.125135	-2.2406092
1.25	6.11	5.9911195	-.11888052	-1.984279
2.5	6.48	6.3713626	-.10863742	-1.7050892
3.75	6.84	6.7333361	-.1066639	-1.5841167
5	7.19	7.0821079	-.10789215	-1.5234468
6.25	7.52	7.4200717	-9.9928261E-02	-1.346729
7.5	7.84	7.7469477	-9.3052297E-02	
-1.2011479				
8.75	8.15	8.0597818	-9.0218245E-02	
-1.1193634				
10	8.45	8.352946	-.09705404	-1.1619139
0	0	5.584865	5.584865	100

END AT 0120

* LIST

0010 DIM A(50)

0020 DEF FNA(X)=5.584865+.33800739*X-.011585362*X^2+.001002896*X^3-.000045635274

*X^4

0030 DIM B(20),C(20),D(20)

0035 LET I=1

0040 PRINT "TYPE IN X,Y PAIRS.... 0,0 TO END"

0045 INPUT A(I),B(I)

0050 IF B(I)=0 THEN GOTO 0100

0060 LET I=I+1

0070 GOTO 0045

0100 PRINT "X ", "Y ", "FNA(X)", "FNA(X)-Y", "% ERROR"

0110 FOR K=1 TO I

0115 LET Y=FNA(A(K))

0117 PRINT A(K),B(K),Y,Y-B(K),((Y-B(K))/Y)*100

0120 NEXT K

* SAVE*COMPARE

* B

NOTE: X&Y values from Reference E

FNA(X) is value for Y computed using steam
table polynomial approximation.

