



# International Agreement Report

## Benchmarking of a Generic CANDU Reactor with PARCS, MCNP and RFSP

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**Manuscript Completed:** June 2015

**Date Published:** September 2015

Prepared as part of  
The Agreement on Research Participation and Technical Exchange  
Under the Thermal-Hydraulic Code Applications and Maintenance Program (CAMP)

**Published by  
U.S. Nuclear Regulatory Commission**

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## **ABSTRACT**

The purpose of this project is to benchmark a generic CANDU reactor with the computer codes PARCS, MCNP and RFSP. RFSP is a diffusion code used by the Canadian nuclear industry for fuel management and for safety analyses. A number of changes were made to PARCS and GenPMAXS, the utility used to generate the fuel tables for PARCS. The changes were required to allow the modeling of specific aspects related to CANDU reactors.

More specifically, the benchmarking exercise involves an assessment of the Finite Difference Method and the hybrid NEM/ANM solvers available in PARCS against the results of Monte Carlo simulations performed with MCNP. The results of the simulations calculated with the Finite Difference Methods in PARCS and RFSP are compared to determine possible areas of improvement in RFSP.

This work is an in-kind contribution and has been funded by Amec Foster Wheeler.



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## EXECUTIVE SUMMARY

Amec Foster Wheeler and the U.S. NRC have an agreement for the assessment of the Code Application and Maintenance Program (CAMP). The agreement provides Amec Foster Wheeler the access to the thermal-hydraulics and neutronics codes, and requires in exchange a contribution using the CAMP toolset.

Within this project, the calculations obtained using the finite-difference solver and the hybrid NEM/ANM solvers in PARCS are benchmarked against MCNP. Identical calculations are also performed with the standard toolset used in the Canadian industry, RFSP, using the finite-difference method. The comparison of the results between PARCS and RFSP is used to identify areas of possible improvement in RFSP.

A number of changes were required in the CAMP toolset and are documented in the report. The changes were required to allow the modeling of the characteristics of a CANDU reactor in PARCS. Changes were made to the GenPMAXS code to make sure that the macroscopic cross sections used in PARCS and RFSP are the same and can also be generated at any specific burnup.

The document also provides a description of the generic CANDU model used in the analysis. The generic CANDU model was built in PARCS, RFSP and MCNP for the benchmarking analysis. A number of core configurations are also identified to test the robustness of the solvers in PARCS and RFSP.

The extrapolation distances of the energy groups used in the diffusion codes were calculated with MCNP for a one-to-one comparison for the benchmarking exercise. The results of the analysis showed:

- Better agreement is obtained between PARCS and MCNP when the PARCS finite-difference solver is used as opposed to when the hybrid NEM/ANM method is used,
- The results of the calculations using the finite-difference solver in PARCS and RFSP are very similar to each other when the same boundary conditions are used. The similarities are in terms of bundle power, channel power and reactivity worths,
- The Canadian toolset could be improved by the use of epithermal and thermal boundary conditions calculated with MCNP, instead of using the thermal boundary condition for the epithermal and thermal groups, and
- The functionalities introduced in GenPMAXS and PARCS for the modeling of a CANDU reactor have been successfully tested and can be used in future analyses.



## **ACKNOWLEDGMENTS**

The authors would like to acknowledge the financial support from Amec Foster Wheeler and the contributions from David Luxat and Julian Lebenhaft. Appreciation is also given to Jim Donnelly whose insights and experience contributed to the understanding of the results of this work and the resolution of issues identified during the course of the work.



## ABBREVIATIONS

AAs	Adjuster Absorbers
ANM	Analytic Nodal Method
CANDU	CANada Deuterium Uranium reactor
CAMP	Code Application and Maintenance Program
CR	Control Rod
FDM	Finite-Difference Method
GC	Generic CANDU
GenPMAXS	Generation of the Purdue Macroscopic XS Set
LZCs	Liquid-Zone Controllers
MCAs	Mechanical Control Absorbers
MCNP	Monte Carlo N-Particle
NEM	Nodal Expansion Model
PARCS	Purdue Advanced Reactor Core Simulator
PM	Poison Moderator
RELAP	Reactor Excursion and Leak Analysis Program
RFSP-IST	Reactor Fueling Simulation Program – Industry Standard Toolset
SORs	Shutoff Rods
U.S. NRC	United States Nuclear Regulatory Commission
WIMS-IST	Winfrith Improved Multi-group Scheme – Industry Standard Toolset



# 1. INTRODUCTION

Amec Foster Wheeler entered an agreement to participate into a work effort within the Code Applications and Maintenance Program (CAMP). The agreement is a work in-kind that provides Amec Foster Wheeler with the thermal-hydraulic and neutronic codes developed within CAMP. The thermal-hydraulic codes are the Reactor Excursion and Leak Analysis Program (RELAP5) [1] and the TRAC/RELAP Advanced Computational Engine (TRACE) [2]. The neutronic codes are the Purdue Advanced Reactor Core Simulator (PARCS) [3] and the Generation of the Purdue Macroscopic XS Set (GenPMAXS) [4].

The focus of this report is to document the work that has been done in the area of core neutronics to allow the specifics of CANada Deuterium Uranium (CANDU) reactors to be modeled in the GenPMAXS/PARCS suite of computer codes. The document provides a detailed description of the simplified model of a CANDU reactor containing a representation of the major features (dimensions, fuel type, reactivity devices) used in the study. Many minor support components and details of the fuel burnup distribution have been omitted from the model as they were not considered essential for this work.

The logic that was implemented in GenPMAXS/PARCS to model the specifics of CANDU reactors are documented in this report. Also, the Finite-Difference Method (FDM) and the hybrid Nodal Expansion Model/Analytic Nodal Model (NEM/ANM) method are assessed to determine the most appropriate method of solving the neutronic flux in the CANDU reactor. The results of the simulations calculated with PARCS are then compared to MCNP5 [5]. The results of the simulations calculated with the FDM method in PARCS are also compared to the results calculated with the FDM method in the Reactor Fueling Simulation Program (RFSP) [6] code commonly used in the Canadian industry to determine the consistency between the two solvers.

An investigation on the use of appropriate extrapolation distances is also performed using the extrapolation distances calculated with MCNP. A recommendation is made for the most appropriate boundary conditions to be used in the diffusion codes in order to reduce the errors associated to the bundle-power and channel-power distributions.





## 2. GENERIC CANDU MODEL

A generic CANDU reactor that contains 480 channels with 13 bundles each was assembled and used to benchmark the PARCS and the RFSP computer codes for a number of core configurations. In order to isolate the principal differences in the neutronics codes PARCS and RFSP and to provide consistent comparisons with MCNP, only fresh fuel was used in the simulations and the moderator was un-poisoned. It is expected that any potential neutronics differences between PARCS and RFSP which might occur because of fuel burnup heterogeneities would be less than the differences which would be revealed from the heterogeneities which might occur because of reactor control devices, which were explicitly modeled in the generic CANDU.

The model is simpler than a CANDU model in that the device locations have been set to fit lines representing whole fuel bundles or half bundles, or aligned with mesh lines. To reduce the required number of meshes, many structural materials have been omitted. The positions of the devices are not exactly at the same relative positions as in a typical CANDU reactor. However, the position deviations are of the order of a few centimetres and are less than the physical dimensions of the devices. The geometrical dimensions of the Liquid-Zone Controllers (LZCs) have also been modified from the ones that are used in a typical CANDU. Consistent generic CANDU models have been developed for use with each of PARCS and RFSP.

### 2.1 Reactor Geometry

For both PARCS and RFSP, device locations are specified by defining boundaries in a XYZ mesh where the properties representing the impact of fuel and devices are placed. The incremental cross sections of the materials are calculated with a transport code over a lattice in the XY directions (28.575 cm) and one bundle length in the Z direction (49.53 cm). The devices are mapped to their respective locations in the core and the associated incremental cross sections are applied to their respective locations in the core. This is in contrast to geometry specifications in the MCNP computer code documented in Reference [5] in which the actual shapes and positions can be represented with the exact geometry. Since the Generic CANDU (GC) is not an actual reactor, the geometry specifications presented herein have been selected to place devices at half or integral fuel bundle positions in order to simplify the PARCS and RFSP modeling. This approach is taken to avoid use of complicated meshes that would be required to match the as-built locations of an actual reactor. It should be noted that this description slightly displaces some devices from their as-built locations in an actual reactor. However, the displacements are usually small, generally within the physical dimensions of the devices.

The GC has 480 fuel channels with 13 fuel bundles per channel. One half bundle is located outside the calandria vessel at each end of each fuel channel. The reactor length is thus defined by 12 bundles within the axial length of the calandria vessel. Furthermore, the reflector is not of uniform thickness in that, at either end of the cylindrical calandria vessel, there is a section of reduced diameter (the notch).

Based on the standard CANDU pitch (XY-plane) of 28.575 cm, a bundle length of 49.53 cm, a mesh structure of half-a-bundle meshes was defined for the X, Y and Z directions (14.2875 cm for the X and Y directions and 24.765 cm for the Z direction). All devices have been specified to fit within the uniform mesh lines. This causes small displacements of device positions from the locations in an operating reactor.

Table 1 lists a summary of reactor physical characteristics and nominal operating conditions.

## 2.2 End Shield Region

The end shield region of the GC has also been simplified from the CANDU design. It consists of two stainless steel tubesheets, each 5 cm thick, penetrated by the fuel channel extensions to the outer tubesheets where the fueling machine connects, plus the endshield material which consists of a mixture of stainless steel ball bearings (60 vol%) and H<sub>2</sub>O (40 vol%) filling the space not occupied by the fuel channel extensions. The endshield region was not modeled in PARCS and RFSP, and instead an extrapolation distance was used in the axial direction. The same approach was used in the radial direction in PARCS and RFSP where an extrapolation distance was used at the boundary of the reflector region.

## 2.3 Extrapolation Distances and Extrapolation Factors

The extrapolation distances were calculated with MCNP [5] using a full-core configuration of the generic CANDU reactor without any in-core components. The thermal neutron fluxes were tallied and the radial and axial extrapolation distances were calculated and defined as the distance from the edge of the core to where the neutron flux vanishes to zero. The two extrapolation distances calculated with MCNP in the radial and axial directions in units of cm were used directly in PARCS.

RFSP uses an extrapolation factor defined by Equation 2.1

$$f = 2 \times \Sigma_{tr2} \times d \quad (2.1)$$

where

$f$  is the extrapolation factor  
 $\Sigma_{tr2}$  is the macroscopic transport cross section for the thermal group (cm<sup>-1</sup>)  
 $d$  is the extrapolation distance (cm) of the thermal group calculated with MCNP

Two extrapolation factors were calculated for RFSP: one for the axial direction and one for the radial direction. The transport cross section used to calculate the extrapolation factor in the axial direction was the thermal transport cross section of the lattice. The transport cross section used to calculate the extrapolation factor in the radial direction was the thermal transport cross section of the reflector.

## 2.4 Fuel and System Parameters

A fuel site or fuel channel is made of a fuel bundle with the associated bundle end plates immersed in heavy water coolant and enclosed in a pressure tube. The pressure tube is located inside a calandria tube with a gap filled with Helium gas between the pressure and the calandria tube.

Figure 1 represents a fuel channel with the different components.

Table 2 lists the coolant and moderator characteristics. Table 3 lists the nuclide number densities of the coolant and moderator.

## 2.5 Burnup Profile

Fresh Natural Uranium (NU) bundles were used in the whole reactor core at a zero burnup value. There was no burnup profile used in the reactor core models to eliminate an additional complexity when evaluating the differences in power profile and reactivity worth calculated with PARCS and RFSP.

## **2.6     Vertical Control Devices**

Many of the control devices enter the reactor vertically from the top of the reactor. The following sections list the details of the Liquid Zone Controllers (LZCs), Shutoff Rods (SORs), Mechanical Control Absorbers (MCAs) and Adjuster Absorbers (AAs).

### **2.6.1   Liquid-Zone Controllers**

For the purpose of spatial control, the reactor is divided into 14 zones. There are six zone controller units traversing the core, with four of them divided into two compartments and two of them divided into three, for a total of 14 compartments. Spatial power control is obtained by means of a column of light water ( $H_2O$ ) in each compartment. Bulk control is achieved by varying the water level in all compartments by the same proportion. Spatial power control is achieved by differential adjustment of the water level in individual compartments. The water level in each zone controller can be varied from 0 to 100 percent full as defined below.

In the Generic CANDU model, the integral geometry of an LZC is not modelled. The geometry has been simplified to a cylindrical Zircaloy tube with an inner diameter of 11.44 cm and an outer diameter of 11.68 cm. There are two lengths of LZCs, 642.9 cm or 700.09 cm, as appropriate for each zone control unit. The units extend downward from the XZ-plane. This means that the zone control guide tubes have the same lengths. The compartments are filled with  $H_2O$  or He-filled (voided). The top compartment of each Zone Control Unit extends to the upper surface of the calandria vessel. The He-filled space above the surface of the  $H_2O$  also extends to the upper surface of the calandria. In PARCS, there were no devices located in the reflector region of the model, compare to the RFSP model where empty tubes were located in the reflector region above the top zone control compartments.

### **2.6.2   Shutoff Rods**

The shutdown mechanism for the shutdown system consists of 32 vertical shutoff rods. In normal operation, these rods are fully withdrawn and available.

Each shutoff rod unit comprises a shutoff rod suspended by a cable from a winch mechanism and a guide tube enclosing its path in the core region. The guide tube extension lies between the calandria top and the reactivity mechanism deck where the shutoff rod is normally poised. The guide tube is heavily perforated through the core region and is filled with  $D_2O$  when the shutoff rod is poised. There are other springs and locators at the bottom end of the guide tube that were not included in the model.

The shutoff rod assembly consists of a Cd tube sandwiched between two stainless steel tubes, 572 cm long. This rod is located inside a Zr-2 guide tube that has a 24.5% volume perforation.

All shutoff rods start from the same elevation and drop to the same elevation. In the Generic CANDU model, the lower edge of the shutoff rods will be poised at the level of the highest point of the reflector (0 cm reference height or 79.125 cm above the upper edge of the calandria tubes in the top row) and fall according to the representative SOR drop characteristic.

### **2.6.3   Mechanical Control Absorbers**

There are four mechanical control absorbers. They are identical in structure and composition to the shutoff rods. Thus, the physical description of the shutoff rods also applies to the MCAs.

The purpose of the MCAs is to provide coarse control override capability when a change in

system reactivity exceeds the rate or depth capability of the LZCs.

#### **2.6.4 Adjuster Rods**

The generic CANDU has 24 adjuster rods. Adjuster rods are of three lengths according to their location in the core. Each adjuster unit comprises an element suspended by a stainless steel cable connected to a winch above the core, as for the SORs. The in-core section maintains the location within the confines of a perforated zirconium guide tube.

The adjuster rod assembly consists of a central rod (shim rod) of titanium inside a stainless steel tube. These two items together form the adjuster. They are not moved independently of each other. This rod is located inside a Zr-2 guide tube.

### 3. INCREMENTAL CROSS SECTIONS

The 2-group macroscopic incremental cross-sections for the LZCs, the AAs, the MCAs and the SORs have to be calculated for the 37-element fuel bundle in hot conditions.

#### 3.1 Methodology

The methodology for the calculation of the incremental cross-sections for the different types of reactivity devices, involves the use of DRAGON-IST [7] lattice cell code<sup>1</sup>. A 3-Dimensional super-cell model is used in the DRAGON-IST calculations, representing two lattice cells containing a fuel bundle in each cell, and an orthogonal reactivity device between them. DRAGON-IST solves the neutron transport problem for this super-cell using the collision-probability technique. The incremental cross-sections are calculated for the case where the super-cell is split into two regions: inner (containing the reactivity device) and outer (super-cell region not included in the inner region).

The homogenized cross sections are calculated for three configurations listed below.

1. No device at all,
2. Guide tube between the fuel channels,
3. Absorber and guide tubes between the fuel channels

The incremental cross sections are calculated from the cross sections of the inner region as follows:

Guide tube = set 2 – set 1

Absorber = set 3 – set 2

DRAGON-IST cannot calculate explicitly the cluster-of-tubes geometry in 3D calculations. Hence, the complex structure of the fuel and the reactivity devices must be cylindered, i.e. approximated with a cylinder of material obtained as a mixture of the materials used in the fuel or in the device. This process requires a two-step homogenization process that was applied using the following 2D models:

- 2D Fuel Cell Model, and
- 2D Super-Cell Model

In the 2D fuel cell model, the 37-element fuel bundle is located at the centre of a lattice cell, surrounded by a pressure tube, annulus gas, calandria tube, and moderator. The flux distribution obtained from the fuel neutron transport calculations for this geometry is used for material homogenization of the cell components. The cell materials are homogenized into three mixtures: homogenized fuel (includes the fuel, cladding and coolant), tube material (calandria tube, pressure tube and the CO<sub>2</sub> gas between them) and moderator. The 89 energy-group macroscopic cross sections calculated for the homogenized materials are then used in the 2D super-cell model. All the incremental cross sections were based on the ENDF/B-VI data library<sup>2</sup> and condensed to a two-energy group structure with a cutoff at 0.625 eV.

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<sup>1</sup> Small differences are found between the lattice properties calculated with WIMS-IST (lattice properties used in RFSP) and DRAGON-IST. The assumption is that the use of the lattice properties calculated with WIMS-IST or DRAGON-IST has negligible impact on incremental cross sections of the in-core structural materials.

<sup>2</sup> The ENDF/B-VI data library used in the analysis was the version generated in Canada for the CANDU reactors.



## 4. LATTICE AND REFLECTOR PROPERTIES

Both PARCS and RFSP require a set of cross sections to model the 37-element Natural Uranium fuel bundles of the generic CANDU model under normal operating conditions.

This section of the document provides the details required to understand how the fuel and reflector tables were generated for both computer codes. It is to be noted that only fuel tables and reflector tables were used in the full-core models with the use of extrapolation distances at the radial and axial boundary locations. No special fuel tables were used to represent the end-shield regions.

### 4.1 RFSP Fuel and Reflector Tables

WIMS-IST [8] models a 2-D slice of a 37-element fuel bundle under normal operating conditions that are listed in

Table 1. The model follows the guidelines for standard CANDU modelling with WIMS-IST with the only exception that fuel element endcaps were not included. The WIMS-IST lattice calculations were performed with the ENDF/B-VI nuclear data library<sup>1</sup>.

A number of commands to the standard WIMS-IST utilities were used to perform post-processing of the WIMS-IST output for RFSP as well as a binary file "Tape 16" that contains information saved after each cycle by the "cellav" and "region" keywords in the WIMS-IST input.

Only the compositions for the fresh core were used in the current analysis. Perturbations were also performed at different boron concentrations in the range of 0 ppm to 5 ppm, but not used in the current simulations.

The reflector properties were calculated for the fresh bundles only with a range of boron concentration varying from 0 ppm to 5 ppm boron. However, the simulations performed in the current analysis were done only at a 0 ppm boron concentration. The reflector properties were also calculated at the conditions listed in Table 1.

### 4.2 PARCS Fuel and Reflector Tables

The purpose of this section is to document the use of GenPMAXS [4] to format the fuel cross sections and device incremental cross sections for the PARCS model of the generic CANDU reactor.

GenPMAXS can organize the cross sections such that the main fuel cross section file will also contain the device incremental cross sections for the LZCs (full and empty) as well as for the AAs, SORs, MCAs and guide tubes.

#### 4.2.1 Fuel Tables

PARCS and GenPMAXS currently utilize a maximum of 12 state variables and only two variables were used for the fuel tables: Control Rod (CR) and Poison Moderator (PM). The CRs were used to define the incremental cross sections of the different devices and structural components and the PMs were used to calculate the lattice properties at different poison concentrations ranging from 0 ppm to 5 ppm boron in steps of 0.5 ppm. However, the current

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<sup>1</sup> The ENDF/B-VI data library used in the analysis was the version generated in Canada for the CANDU reactors.

simulations were all performed at a concentration of 0 ppm boron.

A total of 17 types of cross sections, or branches, were calculated for the fuel properties. The first branch corresponded to the lattice properties with 0 ppm boron and the values were tabulated for 43 different burnup values. Branches 2 to 7 corresponded to the incremental properties of the devices and were calculated at zero burnup only. The branches were: the guide tubes for the AAs, the AAs, the guide tubes for the SORs, the SORs, the empty LZCs, and the filled LZCs. Branches 8 to 17 corresponded to the fuel tables from 0.5 ppm boron to 5 ppm boron in step of 0.5 ppm. The lattice properties at each boron concentration were tabulated at 43 different burnup values. However, only the properties for the fresh fuel and at a 0 ppm boron concentration were used in the current simulations.

#### **4.2.2 Reflector Tables**

The moderator purity was used as a perturbation for the reflector tables. However, only the properties at 0 ppm boron were used for the current analysis. A total of 11 types of cross sections, or branches, were calculated for the reflector properties. The 11 branches were used to model the poison in the moderator from a 0 ppm concentration to a 5 ppm concentration in steps of 0.5 ppm. The reflector properties were calculated for the fresh fuel only as equilibrium burnup profiles were not used in the current analysis.

No specific branches were used to define structural materials or in-core reactivity components for the reflector region.



## 5. REACTOR-CORE CONFIGURATIONS

A few considerations were selected to determine a number of reactor-core configurations that could be used to assess the accuracy of the solvers in PARCS and RFSP.

- The first consideration was to use a single burnup value in the whole core to simplify the problem. A fresh core was selected because no burnup calculations are required in the lattice cells, which introduces a peak at the centre of the core and challenges the neutron-flux solver. The other advantage is to avoid any errors or inaccuracies when the cross sections are interpolated at the given burnup value.
- Full-core calculations without reactivity devices or structural components were required to assess the symmetry of the solution in both, PARCS and RFSP.
- Full-core calculations without reactivity devices and with the guide tubes were required to assess the impact of the structural materials on the numerical solution.
- Calculations with LZCs at 50% and 100% were required to calculate the reactivity worth of the light-water absorbers which is an important parameter in CANDU reactors.
- Full-core calculations were used to assess the impact of the adjusters.
- A side-to-side asymmetric case was also required to determine the accuracy of the flux solvers. The asymmetry was obtained by withdrawing all the adjusters from one side of the core.

Based on the considerations listed above, a total of six cases were established and used to assess differences in RFSP and PARCS predictions of reactivity worth and power profiles. The cases were run with the finite-difference method in RFSP and PARCS, and also solved with a nodal method in PARCS.

### 5.1 Reference Case – Configuration Number 1

The reference case consisted of a full-core with fresh bundles. There were no xenon cross sections used in the model and all the reactivity devices were withdrawn from the core. No structural materials were inserted in the core. All the parameters at the lattice-cell level were defined by the lattice code and not altered by the reactor-core calculations (i.e. fuel temperature, coolant densities etc...).

### 5.2 Guide Tubes Inserted – Configuration Number 2

In this configuration, the guide tubes for the SORs, MCAs and AAs were inserted in the core. The empty LZCs were added as control devices by changing their bank percentage insertions in the core. In RFSP the incremental cross sections for the empty LZCs also extend to the reflector region. Incremental cross sections of reactivity devices and guide tubes were not applied in the reflector region in the PARCS full-core models.

### 5.3 Guide Tubes Inserted and LZCs at 50% - Configuration Number 3

In this configuration, the guide tubes were inserted in the core and the LZCs were set at an average level of 50%. The main objective was to determine the differences between PARCS and RFSP in reactivity worth and power profile.

#### **5.4     Guide Tubes Inserted and LZCs at 100% - Configuration Number 4**

Same configuration as in 5.3 with the only difference that the LZCs were at 100%. This case was used to analyze the linearity of the reactivity worth of the LZCs as a function of fill level.

#### **5.5     Adjusters In – Configuration Number 5**

In this configuration, all the guide tubes were inserted in the model, the LZCs were set at 0% and all the adjusters were inserted. The objective was to assess the accuracy of the flux solvers when the flux is flattened by in-core devices.

#### **5.6     Asymmetric Case – Configuration Number 6**

In this configuration all the guide tubes were in the core and the LZCs were at 0%. The adjusters were inserted on one side of the core and withdrawn on the other side.

## 6. CODE CHANGES REQUIRED IN PARCS AND GENPMAXS

A number of code changes were required to PARCS and GenPMAXS to introduce the capabilities required for modelling a CANDU reactor. The following sections provide the details

### 6.1 PARCS

PARCS is a three-dimensional reactor-core code which solves the steady-state and time-dependent, multi-group neutron diffusion and SP3 transport equations in Cartesian, cylindrical and hexagonal geometries. PARCS is coupled directly to the thermal-hydraulics system codes RELAP5 and TRACE which provide the temperature and flow field information to PARCS during the transient calculations via the few group cross sections.

The major calculation features in PARCS include the ability to perform eigenvalue calculations, transient (kinetics) calculations, Xenon transient calculations, decay heat calculations, pin-power calculations, and adjoint calculations for commercial Light-Water Reactors (LWRs).

#### 6.1.1 Modeling the Shell and Sub-shell

RFSP has the capability to model CANDU reactor geometry, while PARCS was originally developed as a light water analysis code with uniform geometry. There are several unique geometric features of a CANDU reactor, including a notch region, making the model an extruded cylinder. In PARCS, this extrusion leaves an annular region at the ends of the core that need to be filled with a material.

##### 6.1.1.1 *Input Design*

The design for the input is an addition to the planar region and assembly type input cards. The planar regions are then assembled together via the planar region assign card, creating the full geometry, and the assembly type card maps one full axial assembly to the location in the radial configuration location. Both of these inputs allow a dummy region to appear anywhere in the core. A zero anywhere in this mapped input is treated as a dummy, or null region in the computational domain and therefore is not part of the solution. The rest of the nodes are used to set up the linear system.

##### 6.1.1.2 *Functionality*

The new input allows for irregular and non-uniform geometry to be modeled in PARCS. A *zero* cross section identifier can be placed anywhere in any planar region, which will call a modified Nodal Expansion Method (NEM) or Finite Expansion Method (FEM) driver<sup>1</sup>. The code zeroes out values in the specified dummy regions specified by the zeros. The drivers perform checks on each node to see if it is a dummy region or not, and solves the proper one or two nodes problems accordingly. If no dummy regions are present in the model, PARCS defaults to the original NEM sweeping methodology, leaving previous cases unaffected by these coding changes.

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<sup>1</sup> What the PARCS documentation refers to as “Finite Expansion Method” is what more commonly referred to in the literature as “Finite Difference Method” (FDM). The latter expression is used in this report.

### 6.1.1.3 Verification

A total of eight verification test cases were built. Four cases were of 2-Dimensional geometries of 3X3 nodes, and the other four cases were 3-dimensional geometries of 9X9 nodes with 11 axial planes. For each set of four cases, two used FDM solvers, and the other two used NEM solvers. For the 2-dimensional 3X3 cases, the two cases to compare were (1) the input geometry with 3X3 nodes with no dummy regions present, and (2) the input geometry with 9X9 nodes with all nodes being dummy regions except the 3X3 nodes in the centre. This setup made the models exactly the same for comparison purposes. For the 9X9 cases in 3-dimensions, the purpose was to verify that a similar solution is achieved when using black absorber cross sections. The geometry was smaller and similar to the generic CANDU model. In these cases, a notch was created using dummy regions and black absorber cross sections.

The comparison between the 3X3 dummy and no dummy region cases agree very well. The eigenvalues for the dummy and no dummy cases for both FDM and NEM solvers agreed to within a fraction of a mk. The flux values for the epithermal and thermal groups agreed to within 0.1% for the NEM solver, and match to the third decimal place for the FDM cases. It should be noted that the neutronic meshing was increased to 20 in the x direction and 20 in the y direction to ensure an accurate answer.

The 3-dimensional case comparison between the black absorber cross sections that were used in the calculations and the dummy region compared fairly well. The eigenvalue difference was about 1.5mk. The axially integrated power shape shows approximately 1% difference between the cases. Both cases used a zero incoming current albedo boundary condition.

## 6.1.2 Extrapolation Distances

To achieve more accurate comparisons between PARCS and RFSP, additional boundary conditions were added to PARCS. RFSP uses one boundary condition, or extrapolation distance, and PARCS has zero incoming current, zero flux, and reflective boundary conditions. Since the boundary conditions are fairly rigid for PARCS and not easily comparable to RFSP, albedo boundary conditions were implemented in PARCS. This boundary condition was then used to provide the structure for implementing an albedo extrapolation distance equivalent to the extrapolation distance used in RFSP.

### 6.1.2.1 Input Design

Initially in PARCS, there were three albedo cards, ALBEDO\_R, ALBEDO\_ZT, ALBEDO\_ZB, which have an energy group dependent input of net current divided by the surface flux. The same style of input was used for the creation of the albedo boundary conditions in Cartesian coordinates with some modifications. Albedo cards need to be specified for each face in Cartesian geometry; north, south, east, west, top and bottom. In these cards, more than one set of albedos can be specified. In the last line of each radial card, a map is used to apply the specified boundary condition set at that axial position. In the case of the axial cards, the card BC\_ZT\_MAP (or ZB) is to be used to map each radial assembly location to the corresponding boundary condition set.

The same type of input style is used for the extrapolation distance cards. EXTRAP\_D\_R requires an extrapolation distance to be specified for each energy group, along with an extrapolation radius to be used in calculating the nodal albedos. The same type of map used for the radial albedo cards can be used here. EXTRAP\_D\_Z requires the extrapolation distance for each energy group. Appendix C lists the new cards that were added for the treatment of the boundary conditions in PARCS.

#### 6.1.2.2 Computation

A new derivation of the NEM solution was needed and coded into PARCS to accommodate the new boundary conditions. This coding was added in the one node solver of the ANM driver in PARCS. Appendix D provides the derivation of the equations that were implemented in PARCS.

For the boundary condition associated with the extrapolation distance, the extrapolation radius and distance were used with the node positions to calculate the node-wise extrapolation distance for each face. The distance was then used with the diffusion coefficient to calculate the equivalent albedo boundary condition.

The new albedo cards provide the first step towards albedo-equivalent extrapolation distance boundary conditions. They are consistent with the boundary conditions that are already in PARCS. When using the albedo cards, the albedo boundary conditions that are equivalent to the standard boundary conditions of reflective, zero flux, and zero incoming current give the same results as the standard ones. The albedo cards also allow for a wider selection of boundary conditions to be used when running a case. The cards also allow for every axial mesh to have different radial boundary conditions and every radial node to have different axial boundary conditions.

#### 6.1.2.3 Verification

The verification process consisted of a series of simple test cases in one, two and three dimensions using the hybrid NEM/ANM and FDM solvers and comparing the results using the albedo boundary conditions to the results using the standard boundary conditions. The next set of verification cases was a 2X2 assembly using the extrapolation distances and an equivalent albedo model, a 5X5 case with extrapolation distances which was used to verify that the correct albedos were being used in each node, and a 1-dimensional case compared to an analytic calculation. Appendix E lists the results for each case.

For the FDM cases, the comparison between the two methods show that the results were the same within the sixth decimal. For the NEM cases, the results are very close in the 1-dimensional cases, but differences in the results were found between the two solutions with the higher leakage in the next 2- and 3-dimensional cases. For the other cases, the neutronics meshing remained at one, while for the NEM cases in 2- and 3-dimensions the meshing was increased to 12 and 20 meshes, respectively.

The agreement between the albedo boundary conditions and the legacy boundary conditions in PARCS, which have been verified and validated themselves, verifies the new method.

### 6.1.3 Moveable Devices

CANDU reactors have control devices that are located in vertical positions in the reactor and perpendicular to the fuel channels. The task was to use a simple way to input a large number of control devices in PARCS and be simple to use as well as versatile enough to accommodate devices that do not fall perfectly within the nodal boundaries. The objective was to use the existing linear control rod bank in PARCS to move the vertical devices in the core.

#### 6.1.3.1 Input Design

The new *lincr\_bank* input card requires the control device tip coordinates for the fully inserted and withdrawn positions, a type specifying whether the rod is to be treated like a circle, square, or rectangle, and the dimensions of the type. By using coordinate input positions, it provides the

functionality necessary for control devices positioned in the core regardless of the nodal mesh. The type and dimensions complement the coordinate positions by providing the functionality to calculate the nodal rod fractions. These values are the only information required to convert the linear control rod into a custom control rod input, allowing the user to input multiple devices with ease.

#### 6.1.3.2 Computation

The new cards were implemented as an extra step in the input processing of a PARCS input file. The names of the new cards are *linear\_cr* and *lincr\_bank*, which are analogous to the *custom\_cr* and *ccr\_bank* cards.

The linear control bank card is similar to other control rod inputs in PARCS. The specific nodal locations are controlled by the linear control rod input. The rod fraction to perturb each node with control rod branch cross sections is also controlled by the input. The insertion of the control rods is controlled by the *bank\_pos* card. The control rod branch cross sections to be used for each bank are controlled by the *crb\_def* and *crb\_type* cards.

#### 6.1.3.3 Verification

A total of 4 test cases with a sample CANDU reactor were used to verify the coding in PARCS. The first test case was a single control rod inserted from the top of the reactor and located at the centre. The second test case consisted of a single rod also inserted from the top, but with a displacement in the radial and axial directions. The third test case consisted of a control rod inserted from the bottom, but with a displacement in the radial and axial directions. The fourth test case consisted of a configuration with the four control devices with the additional guide tubes inserted from the top to the bottom.

Each of these test cases was run using the linear control rod input and the custom control rod input. The eigenvalues and the control rod positions were independently checked using the linear control rod input parameters to make sure that the incremental cross sections were applied at the correct locations. There was an exact match between the location of the rods and the eigenvalues calculated using the linear and the custom control cards. The *lincr\_bank* card is considered verified and provides a more straight forward way to move the control devices in a CANDU reactor.

## 6.2 GenPMAXS

The GenPMAXS code was developed to process the cross sections generated by a lattice physics code into the PMAXs format that can be read by PARCS. The burnup-dependent macroscopic cross sections are read by PARCS from the PMAXS file prepared by the code GenPMAXS and then used in PARCS to calculate the node-wise flux and power distribution, which is then used to calculate the region-wise burnup for time advancing the macroscopic cross sections.

### 6.2.1 Processing the Cross-sections from WIMS-IST

Changes were introduced in GenPMAXS to read the cross sections generated with the WIMS-IST lattice code and located in the TAPE16 file.

Table 4 lists the keywords used in the TAPE16 file and processed by the GenPMAXS utility code.

The module WIMS-to-PMAXS was developed to read the cross sections from the TAPE16 files and convert into the PMAXS format. Figure 2 shows the structure implemented in the WIMS-to-PMAXS module.

The WIMS-to-PMAXS module consists of two major subroutines, WIMS\_scan, and WIMS\_read. As only two group data will be processed in the current version of GenPMAXS, and all burnup, branch, and history information are given in the GenPMAXS input file, the dimensions of the data structure are already determined. In the subroutine WIMS\_scan, the data structure for describing the contents of the TAPE16 files is assigned according to the information from the GenPMAXS input file. Memory is allocated according to the dimensions of the files. In the subroutine WIMS\_read, the cross sections data are read by first checking the keywords listed in

Table 4. The cross section data are stored in the PMAXS data structure and prepared for generating partial derivatives and printing into the PMAXS file.

### **6.2.2 Process the Cross Sections from DRAGON-IST**

This task was to modify GenPMAXS to process the cross sections for the CANDU benchmark model. This included the generation of the cross sections for the reflector. GenPMAXS was also modified to merge the cross sections from WIMS-IST and the incremental cross sections from DRAGON-IST into one PMAXS file.

### **6.2.3 Generation of the Fuel Tables for PARCS**

The modified version of GenPMAXS was used to read the WIMS-IST cross sections and the DRAGON-IST incremental cross sections to produce a single PMAXS cross section file for PARCS. The input follows the standard GenPMAXS format used in conjunction with the new %INCREME card as described in Section 6.2.2.





## 7. SIMPLIFICATIONS USED IN THE FULL-CORE MODELS

The computer models of the generic CANDU reactor that were built in PARCS, RFSP-IST and MCNP were all made consistent within each other during the course of the analysis. A few assumptions were used and justified below.

### 7.1 Fuel Density

The modelling of each pin with the specific burnup in MCNP forces the simplification of the model where the burnups need to be binned to limit the number of universes in the model. In order to isolate the principal differences in the neutronics codes and to provide consistent comparisons with MCNP, fuel burnup was not considered.

The lattice cell calculations performed in WIMS-IST used a fuel density of 10.51 g/cm<sup>3</sup> and an endcap card was used to take into account the end caps and the coolant on both ends of the bundle. The lattice properties in WIMS-IST are calculated over a bundle length and the use of the endcap card scales down the fuel density by taking into account the length of the fuel stack over the length of the bundle. The isotopic concentrations that were calculated in WIMS-IST in units of  $\frac{\text{atom}}{\text{barn} \times \text{cm}}$  with the associated density of 10.5038  $\frac{\text{g}}{\text{cm}^3}$  was used in MCNP.

### 7.2 Incremental Cross Sections in the Reflector Regions

CANDU reactors are characterized by vertical reactivity devices inserted from the top. To each device is associated a guide tube located from the top reflector region to the bottom reflector region. To simplify the models, the incremental cross sections of the guide tubes located at the bottom reflector region were omitted. The incremental cross sections of the devices located in the top reflector region were included in RFSP-IST and MCNP and were omitted in PARCS.

The incremental cross sections of the devices located in the reflector region are calculated using a standard supercell model in DRAGON-IST that comprises the device surrounded by two fuel channels. The use of the standard supercell model in DRAGON-IST generates small incremental fission cross sections that are not fully representative of the physics phenomena in the reflector region. In MCNP this does not affect the physics because each device is modelled with its material composition and incremental cross sections are not required. In RFSP-IST, the fission cross sections are set to 0 in the reflector region. PARCS does not accept fission cross sections in the reflector region and as a direct consequence, no devices were introduced in the reflector region.

The incremental cross sections associated with the guide tubes located in the top reflector region are very small because they consist of a zircaloy material filled with heavy water. However, the incremental cross sections associated with the empty liquid-zone controllers is not negligible because the device consists of a zircaloy tube filled with void. The absence of heavy-water in the top LZC compartments located in the reflector region is expected to be noticeable at the top of the reactor.

### 7.3 Extent of the Models in the Axial and Radial Directions

The MCNP computer code has few limitations in terms of modelling capabilities and can represent complex geometries where the diffusion approximation does not hold. The model in the axial direction included the end shield region. The model also included the light water surrounding the reactor in the radial direction.

In the PARCS and RFSP-IST core models, the extent of the model in the axial direction stopped at the calandria side tubesheet where an extrapolation distance was applied. In the radial direction, the models stopped at the surface of the heavy-water reflector where an extrapolation distance was applied. Two sets of extrapolation distances were used in the PARCS and in the RFSP-IST models; one set in the axial direction and one set in the radial direction.

The impact of using extrapolation distances in the PARCS and in the RFSP-IST models should have a small impact on the flux profile and power distribution as long as the extrapolation distances are calculated using the equivalent MCNP full-core model.

#### **7.4     Energy Discretization**

An advantage of the MCNP computer code is the use of a continuous energy group and eliminates the need for self-shielding calculations. WIMS-IST and DRAGON-IST both require discrete energy group calculations and apply the 89-energy group structure using the energy cutoffs listed in Table 5 for the lattice calculations. For the supercell calculations, the energy group are condensed into a 33-energy group structure to optimize the computer resources to solve the 3-Dimensional supercell configurations. Once the supercell problem is solved in the 33-energy-group structure, the cross sections are condensed into a 2-energy group structure to define the thermal and epithermal incremental cross sections used in the full-core diffusion calculations. The energy cutoff used to define the energy group structure is at 0.625eV.

## 8. RESULTS

The first subsection provides the extrapolation distances that were calculated with MCNP with the derived extrapolation factors for use with the P card of the \*DATA GEOMETRY module in RFSP-IST. The next sections provide the results of the simulations with MCNP, PARCS and RFSP-IST. The results include the reactivity worths of the different in-core devices and the power profiles using two sets of boundary conditions. In the first set, the methodology was consistent with the approach used in RFSP-IST where the boundary condition for the thermal group was also applied to the epithermal group. In the second set, the extrapolation distances calculated for the thermal and for the epithermal groups were applied in PARCS for the thermal and epithermal groups, respectively.

### 8.1 Extrapolation Distances and Extrapolation Factors

The extrapolation distances were calculated with MCNP as described in Section 2.3 and are listed in Table 6.

The numerical values listed in Table 6 representing the average extrapolation distances were directly used in PARCS because the definition of the extrapolation distances used in PARCS is the same as what was calculated in MCNP. The extrapolation distances of the thermal group listed in Table 6 were converted into extrapolation factors using Equation 2.1. Table 7 lists the extrapolation factors that were used in RFSP-IST.

The boundary conditions listed in Table 6 and Table 7 were used in PARCS and RFSP-IST, respectively. The next sections provide the reactivity worths and the power profiles calculated with the diffusion codes.

### 8.2 Reactivity Worths

The reactivity worths of the devices were calculated in units of  $mk$  using Equation 8.1 below.

$$\rho_{dev} = \frac{k_{eff}^{in} - k_{eff}^{ref}}{k_{eff}^{in} \times k_{eff}^{ref}} \times 1000 \quad (8.1)$$

Where

$\rho_{dev}$  is the reactivity worth in  $mk$  of the device,  
 $k_{eff}^{in}$  is the k-effective value of the full-core model with the device inserted, and  
 $k_{eff}^{ref}$  is the k-effective value of the reference full-core model with no devices in.

Table 8 lists the reactivity worths that were calculated with MCNP and used as a reference to benchmark the results calculated with PARCS and RFSP-IST. Table 9 and Table 10 list the reactivity worths that were calculated with PARCS and RFSP-IST with the finite-difference method using the thermal boundary conditions only. The results show that the two codes predict very similar results. The reactivity worth of the LZCs is overpredicted by 8.5% and 8.1% in RFSP-IST and PARCS, respectively. The worth of the adjusters is underpredicted by 1.7% and 3.0% in RFSP-IST and PARCS, respectively.

The results listed in Table 11 indicate that the use of the nodal method increases the discrepancy of the reactivity worth associated with the LZCs. The worth of the LZCs is overpredicted by 12.01% compared to MCNP. However, the use of the nodal method

decreases the discrepancy of the reactivity worth associated with the adjusters compared to MCNP. The FDM method predicts a difference of 2.97% compared to MCNP and the nodal method predicts a difference of 1.49%.

Table 12 and Table 13 list the results calculated with PARCS when the two-group boundary conditions are used in the FDM and nodal methods, respectively. The reactivity worths listed in the two tables show that the use of the 2-group boundary conditions has a negligible impact on the reactivity worths when compared to reactivity worths calculated with the thermal group boundary condition only.

### **8.3      Power Profiles**

The power profiles that were calculated with MCNP for the different configurations were used as a benchmark to determine the accuracy of the solutions obtained with PARCS and RFSP-IST. The finite-difference solver and the hybrid NEM/ANM solver were tested in PARCS using two sets of extrapolation distances. In the first set, the thermal extrapolation distances were applied to the fast and thermal groups. In the second set, the thermal extrapolation distance and the epithermal extrapolation distance were applied to the thermal and fast-neutron groups, respectively.

The channel power distributions calculated with PARCS were benchmarked against MCNP for all the configurations. For the bundle power distributions, the planes located at the extremity of the reactor in the axial direction were benchmarked against MCNP. Those planes were selected because of their sensitivity to the extrapolation distances. Plane number 4 was also selected because of the presence of the LZCs.

All the figures included in this Section represent a front view of the reactor where columns 1 to 24 represent the fuel columns from the left-hand side to the right-hand side of the reactor. Rows A to Y represent the fuel rows where row A is located at the top of the reactor and row Y is located at the bottom of the reactor<sup>1</sup>.

The next sections present the results of the benchmarking exercise and cover the similarities and differences that were identified in channel-power profiles and bundle-power profiles, respectively.

#### **8.3.1   Channel Power Profiles (Thermal Extrapolation Distances Only)**

The thermal extrapolation distances that were calculated in the radial and axial directions for the thermal group only and listed in Table 6 were used in PARCS for the thermal and epithermal groups. The extrapolation factors listed in Table 7 for the thermal group were used in RFSP-IST for the thermal and epithermal groups.

##### **8.3.1.1   *Benchmarking of PARCS Against RFSP-IST***

Comparison of the results calculated with PARCS and RFSP-IST with the finite-difference solver with symmetric configurations are listed in Figure 3 and Figure 4. The results show that PARCS and RFSP-IST agree very well for the bare lattice model where no devices are inserted in the core (Figure 3). Figure 4 shows differences in power distribution located mainly at the top of the reactor. This is due to the absence of incremental cross sections in PARCS at the top of the reactor in the reflector region. This becomes evident for the largest perturbation (LZC guide tubes) with differences of the order of 2.5% at the top of the reactor.

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<sup>1</sup> Row I is not used in the model. The generic CANDU reactor has 24 rows in total.

Figure 5 shows a larger power error on the left-end side of the reactor for the asymmetric core configuration. The left-end side of the reactor is characterized by a lower power compared to the right-end side of the reactor as shown in Figure 6.

#### **8.3.1.2 Benchmarking PARCS Finite-Difference Method Against MCNP**

Figure 7 to Figure 9 show the differences in power profiles that were calculated between PARCS and MCNP. The results show a slight asymmetry from side-to-side that was due to the convergence in MCNP. Figure 8 also show larger errors at the top of the reactor due to the absence of incremental cross sections in the top-reflector region in the PARCS model.

Figure 9 shows that the FDM method overpredicts the power in the high-power zone located on the right-end side of the Figure. Figure 5 also shows that RFSP-IST predicts a higher power compared to PARCS in the same region and RFSP-IST would give larger differences compared to MCNP for the asymmetric case shown in Figure 9.

#### **8.3.1.3 Benchmarking PARCS Hybrid NEM/ANM Method Against MCNP**

Figure 10 to Figure 12 show the differences that were calculated between the hybrid NEM/ANM method in PARCS and the power distribution calculated with MCNP. The results show that the hybrid NEM/ANM method overestimates the power at the edge of the reactor and underestimates the power at the centre compared to the FDM method.

### **8.3.2 Channel Power Profiles (Thermal and Epithermal Extrapolation Distances)**

The thermal extrapolation distances were calculated in the radial and axial directions for the thermal group and epithermal groups and listed in Table 6 where used in PARCS for the thermal and epithermal groups, respectively. The extrapolation factors listed in Table 7 for the thermal group were used in RFSP-IST for the thermal and epithermal groups.

#### **8.3.2.1 Benchmarking of PARCS Against RFSP-IST**

Figure 13 to Figure 15 show the differences that were calculated between PARCS with both boundary conditions (thermal and epithermal) using the FDM method and RFSP-IST using the FDM method with the thermal-energy-group boundary condition. The figures show that the differences in channel-power distributions were smaller compared to the differences in channel-power distributions using the 1-energy-group boundary condition (Figure 3).

Figure 14 and Figure 15 show that the differences calculated between the PARCS FDM 2-energy-group boundary conditions and RFSP-IST FDM 1-energy-group boundary conditions are similar to the differences calculated between the PARCS FDM 1-energy-group boundary conditions and RFSP-IST FDM 1-energy-group boundary condition (Figure 4 and Figure 5).

#### **8.3.2.2 Benchmarking PARCS Finite-Difference Method Against MCNP**

Figure 16 to Figure 18 show the differences calculated between the PARCS 2-energy-group boundary conditions using the FDM method and MCNP. The figures show that the differences in channel-power distributions were all similar to the differences that were calculated using the 1-energy-group boundary condition (Figure 7, Figure 8 and Figure 9).

### 8.3.2.3 Benchmarking PARCS Hybrid NEM/ANM Method Against MCNP

Figure 19 to Figure 21 show the differences in channel-power distributions that were calculated between PARCS with the hybrid NEM/ANM solver and MCNP. The results show that the use of the hybrid NEM/ANM method increases the power error at the edge of the reactor in the low-power regions compared to the FDM method (Figure 7, Figure 8 and Figure 9).

### 8.3.3 Bundle Power Profiles

The differences in bundle-power profiles were calculated between PARCS and MCNP. Only the calculations performed in PARCS with the FDM method were benchmarked against MCNP because Section 8.3.2.3 showed that the hybrid NEM/ANM method tends to overestimate the power for the bundles located at the periphery of the core.

Figure 22 to Figure 24 show the differences in bundle powers that were calculated between PARCS FDM and MCNP when the thermal boundary conditions listed in Table 6 were applied to the fast and thermal groups in PARCS. Figure 22 shows for Plane number 1, located close to the end-shield region, differences close to -20% with an average value of -10.0% for Reference case. Figure 23 and Figure 24 show the differences in bundle powers for planes number 1 and plane number 4 with the LZCs at 100%. Figure 24 shows that near the centre of the core, the differences are small compared to MCNP and increase for the bundles located at the periphery of the core.

Figure 25 shows the differences in bundle power that were calculated between PARCS and MCNP at plane number 1 when the thermal and epithermal boundary conditions listed in Table 6 were used for the thermal and epithermal groups. The results listed in Figure 22 and Figure 25 show that the differences in bundle powers went down with the use of the 2-energy-group boundary conditions compared to the use of the thermal boundary condition only in PARCS. The average error in Figure 25 was -4.8% compared to -10.0% in Figure 22.

Figure 26 and Figure 27 show the differences in bundle power that were calculated between PARCS and MCNP at planes number 1 and number 4, respectively when the thermal and epithermal boundary conditions listed in Table 6 were used for the thermal and epithermal groups. Comparison of the results to Figure 23 and Figure 24, respectively show that the use of the 2-energy-group boundary conditions has a negligible impact in the regions located away from the end shields.

## 9. DISCUSSION

An improvement could be introduced in the full-core model in PARCS for the use of incremental cross sections of the devices located in the reflector region. This aspect is particularly important for the presence of the empty LZCs at the top of the reactor that reduces the amount of heavy water available for the moderation.

The incremental cross sections associated with  $\nu\Sigma_f$  could be set to zero in the reflector region, or a supercell model that extends into the reflector region could be used to calculate an incremental set compatible with the full-core model. The use of incremental cross sections at the top-reflector region in PARCS would increase the consistency between all the codes.

The extrapolation distances calculated in MCNP were based on the bare lattice model that has no in-core devices. It would be more consistent to calculate the extrapolation distances for each configuration.





## 10. CONCLUSIONS

Based on the results of the analysis, a number of observations can be drawn.

- The reactivity worth of the devices calculated with the finite-difference method with PARCS is approximately the same compared to the reactivity worth of the devices calculated with RFSP-IST. The differences are larger for the LZCs when the nodal method is used in PARCS. However, the use of the nodal method reduces the discrepancy of the reactivity worth associated to the adjusters compared to the FDM.
- The channel-power profile calculated with PARCS for the reference case when the finite-difference method is used compares very well with the channel-power profile calculated with RFSP-IST.
- When devices or structural materials are located in the core, the maximum differences in channel-power profile calculated between PARCS and RFSP-IST is approximately 2.5% at the top of the reactor close to the reflector region. This was due to the absence of incremental cross sections for the LZCs located at the top of the reactor in the reflector region in the PARCS model.
- The use of the nodal method in PARCS tends to increase the power of the channels located at the periphery of the core and slightly decrease the power of the channels located in the core.
- The power of the bundles located at the end of the channels and calculated with the FDM method in PARCS and RFSP-IST using the thermal extrapolation distances only is higher compared to the power of the bundles calculated with MCNP at the same locations.
- The use of the thermal and epithermal boundary conditions with the FDM method in PARCS reduces the average error in bundle powers in plane number 1 located close to the end shield region.
- It is recognized that the nodal method predicts larger differences in power distribution at the periphery of the core compared to the finite-difference method when benchmarked against MCNP. Further investigation is required to understand the causes of the discrepancies and identify the most appropriate options associated with each method.



## 11. REFERENCES

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## APPENDIX A TABLES

**Table 1 Summary of Reactor Physical Characteristics and Nominal Conditions**

<b>Calandria vessel</b>	
Inner radius (cm)	414.3375
Material	Stainless Steel
Thickness (cm)	3.2
Core outer radius (cm) (variable - max)	363
Thickness of Reflector (cm) (variable - min)	51
Axial Length (cm)	594.36
Subshell inner radius (cm)	371.425
Axial extension of the sub shell – each end (cm)	49.5
<b>End Shield Region</b>	
Tubesheets (both)	
Thickness (cm)	5.0
Material	Stainless Steel
Shield	
Thickness (cm)	100.0
Material	Stainless Steel/H <sub>2</sub> O
Ratio	60% Stainless Steel and 40% H <sub>2</sub> O
<b>Fuel Channels</b>	
Number	480
Pitch (cm)	28.575
Length (cm) (12 in-core bundles+2 calandria-side tubesheets+2 endshield regions)	804.36 cm
<b>Devices</b>	
Vertical	
Shutoff rods (SDS1)	32
Adjuster rods	24
Zone controller units	6
Compartments/Zones	14
2-high units	4
3-high units	2
Mechanical control absorbers	4
<b>Nominal Conditions</b>	
Moderator Purity (at%)	99.97
Coolant Purity (at%)	99.11
Moderator poison (ppm Gd)	0
Moderator temperature (K)	339
Coolant temperature (K)	563
Fuel temperature (K)	1011

**Table 2 Moderator and Coolant Characteristics**

Coolant	Purity (at%)	99.11
	Temp (K)	563
	Density (g/cc)	0.80768
Moderator	Purity (at%)	99.97
	Temp (K)	339
	Density (g/cc)	1.08709

**Table 3 Nuclide Number Densities of Moderator and Coolant**

Coolant	
Isotope	Number Density (at/barn.cm)
DD2O	4.8280E-02
H1H2O	4.3355E-04
O16	2.4299E-02
Moderator	
Isotope	Number Density (at/barn.cm)
DD2O	6.5490E-02
H1H2O	1.9652E-05
O16	3.2677E-02

**Table 4 Keywords Used in the WIMS-IST TAPE16 File and Used by the GenPMAXS**

Keyword	Purpose
BEGIN	Beginning of a cross section data block
ABSORPTION	Absorption cross section, including fission
NU-FISSION	Nu-fission cross section
TOTAL-X	Transport cross section
FLUX	Assembly average flux
SCATTER	Scattering cross section
FISSPECT	Fission spectrum
EDGEFLUX	Assembly surface flux for ADF

**Table 5 Energy Group Structure Used in WIMS-IST and DRAGON-IST for the Lattice Calculations**

The Upper Energy Limit of Group 1 is 1.0E+07 eV							
Group	Lower Energy Limit eV	Group	Lower Energy Limit eV	Group	Lower Energy Limit	Group	Lower Energy Limit
1	7.7880E+06	24	9.1188E+03	47	4.0000E+00	70	3.0000E-01
2	6.0653E+06	25	5.5308E+03	48	3.3000E+00	71	2.8000E-01
3	4.7237E+06	26	3.3546E+03	49	2.6000E+00	72	2.5000E-01
4	3.6788E+06	27	2.0347E+03	50	2.1000E+00	73	2.2000E-01
5	2.8650E+06	28	1.2341E+03	51	1.5000E+00	74	1.8000E-01
6	2.2313E+06	29	7.4852E+02	52	1.3000E+00	75	1.4000E-01
7	1.7377E+06	30	4.5400E+02	53	1.1500E+00	76	1.0000E-01
8	1.3534E+06	31	2.7536E+02	54	1.1230E+00	77	8.0000E-02
9	1.0540E+06	32	1.6702E+02	55	1.0970E+00	78	6.7000E-02
10	8.2085E+05	33	1.3007E+02	56	1.0710E+00	79	5.8000E-02
11	6.3928E+05	34	1.0130E+02	57	1.0450E+00	80	5.0000E-02
12	4.9787E+05	35	7.8893E+01	58	1.0200E+00	81	4.2000E-02
13	3.8774E+05	36	6.1442E+01	59	9.9600E-01	82	3.5000E-02
14	3.0197E+05	37	4.7851E+01	60	9.7200E-01	83	3.0000E-02
15	2.3518E+05	38	3.7267E+01	61	9.5000E-01	84	2.5000E-02
16	1.8316E+05	39	2.9023E+01	62	9.1000E-01	85	2.0000E-02
17	1.4264E+05	40	2.2603E+01	63	8.5000E-01	86	1.5000E-02
18	1.1109E+05	41	1.7603E+01	64	7.8000E-01	87	1.0000E-02
19	8.6517E+04	42	1.3710E+01	65	6.2500E-01	88	5.0000E-03
20	6.7379E+04	43	1.0677E+01	66	5.000E-01	89	2.0000E-04
21	4.0868E+04	44	8.3153E+00	67	4.0000E-01		
22	2.4788E+04	45	6.4760E+00	68	3.5000E-01		
23	1.5034E+04	46	5.0435E+00	69	3.2000E-01		

**Table 6 Extrapolation Distances Calculated with MCNP and Used in PARCS (cm)**

	Epithermal Group	Thermal Group
Radial Direction	$4.13021 \pm 0.25$	$3.55150 \pm 0.07$
Axial Direction	$9.58116 \pm 0.22$	$5.21171 \pm 0.15$

**Table 7 Extrapolation Factors Used in RFSP-IST**

	Extrapolation Factor <sup>1</sup>
Radial Direction	2.85925
Axial Direction	3.94223

**Table 8 Reactivity Worths Calculated with MCNP**

Configuration	Reactivity Worth (mk)
Guide Tubes	$-2.37 \pm 0.02^2$
LZCs at 50%	$-2.98 \pm 0.03$
LZCs at 100%	$-5.08 \pm 0.02$
Adjusters	$-22.19 \pm 0.02$
Core Asymmetry	$-7.54 \pm 0.02$

**Table 9 Reactivity Worths Calculated with RFSP-IST with Thermal Boundary Conditions**

Configuration	Reactivity Worth (mk)	(RFSP-IST-MCNP)/MCNP (%)
Guide Tubes	-2.20	-7.3
LZCs at 50%	-3.15	5.7
LZCs at 100%	-5.52	8.5
Adjusters	-21.81	-1.7
Core Asymmetry	-7.36	-2.5

**Table 10 Reactivity Worths with PARCS (Finite-Difference Method) with Thermal Boundary Conditions Only**

Configuration	Reactivity Worth (mk)	(PARCS-MCNP)/MCNP (%)
Guide Tubes	-2.19	-7.9
LZCs at 50%	-3.15	5.5
LZCs at 100%	-5.49	8.1
Adjusters	-21.53	-3.0
Core Asymmetry	-7.30	-3.3

<sup>1</sup> The extrapolation factors were calculated using Equation 2.1 with a thermal transport cross section of  $3.7821 \times 10^{-1} \text{ cm}^{-1}$  in the axial direction (fuel) and  $4.0259 \times 10^{-1} \text{ cm}^{-1}$  in the radial direction (reflector).

<sup>2</sup> The +/- values represent the uncertainties associated with the stochastic calculations in MCNP



**Table 11 Reactivity Worths with PARCS (Nodal Method) with Thermal Boundary Conditions Only**

Configuration	Reactivity Worth (mk)	(PARCS-MCNP)/MCNP (%)
Guide Tubes	-2.18	-8.1
LZCs at 50%	-3.25	9.0
LZCs at 100%	-5.69	12.0
Adjusters	-21.86	-1.5
Core Asymmetry	-7.36	-2.5

**Table 12 Reactivity Worths with PARCS (Finite-Difference Method) with Fast and Thermal Boundary Conditions**

Configuration	Reactivity Worth (mk)	(PARCS-MCNP)/MCNP (%)
Guide Tubes In	-2.18	-8.0
LZCs at 50%	-3.15	5.8
LZCs at 100%	-5.51	8.4
Adjusters In	-21.43	-3.4
Core Asymmetry	-7.28	-3.5

**Table 13 Reactivity Worths with PARCS (Nodal Method) with Fast and Thermal Boundary Conditions**

Configuration	Reactivity Worth (mk)	(PARCS-MCNP)/MCNP (%)
Guide Tubes In	-2.18	-8.1
LZCs at 50%	-3.26	9.2
LZCs at 100%	-5.71	12.3
Adjusters In	-21.77	-1.9
Core Asymmetry	-7.34	-2.7



## APPENDIX B FIGURES

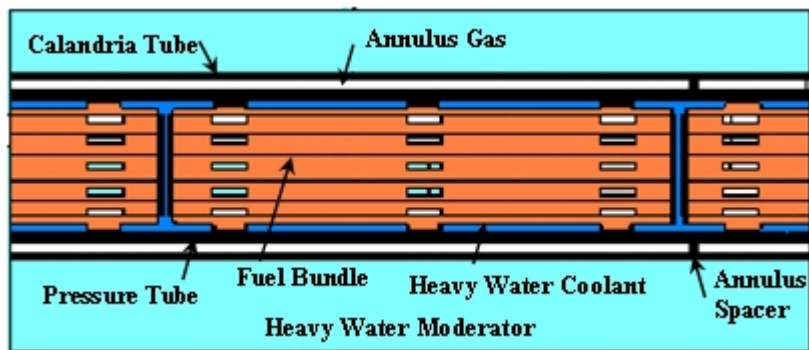


Figure 1 Representation of a Fuel Channel

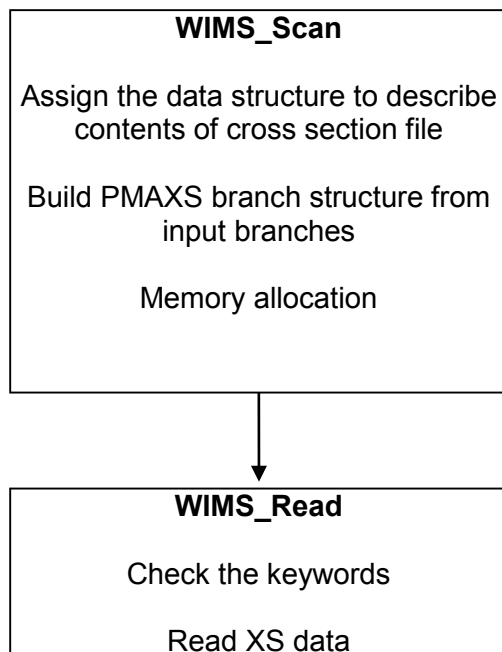
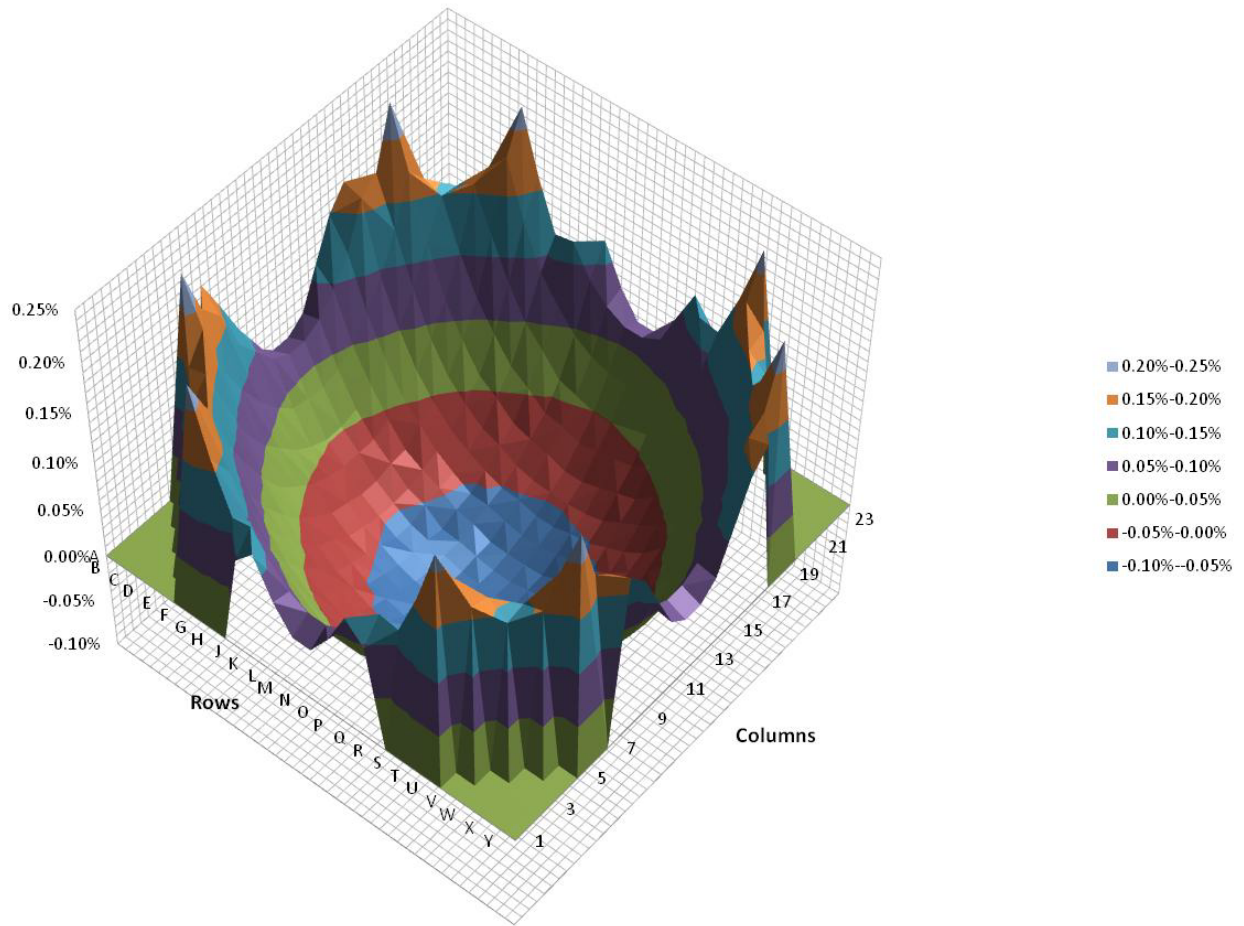
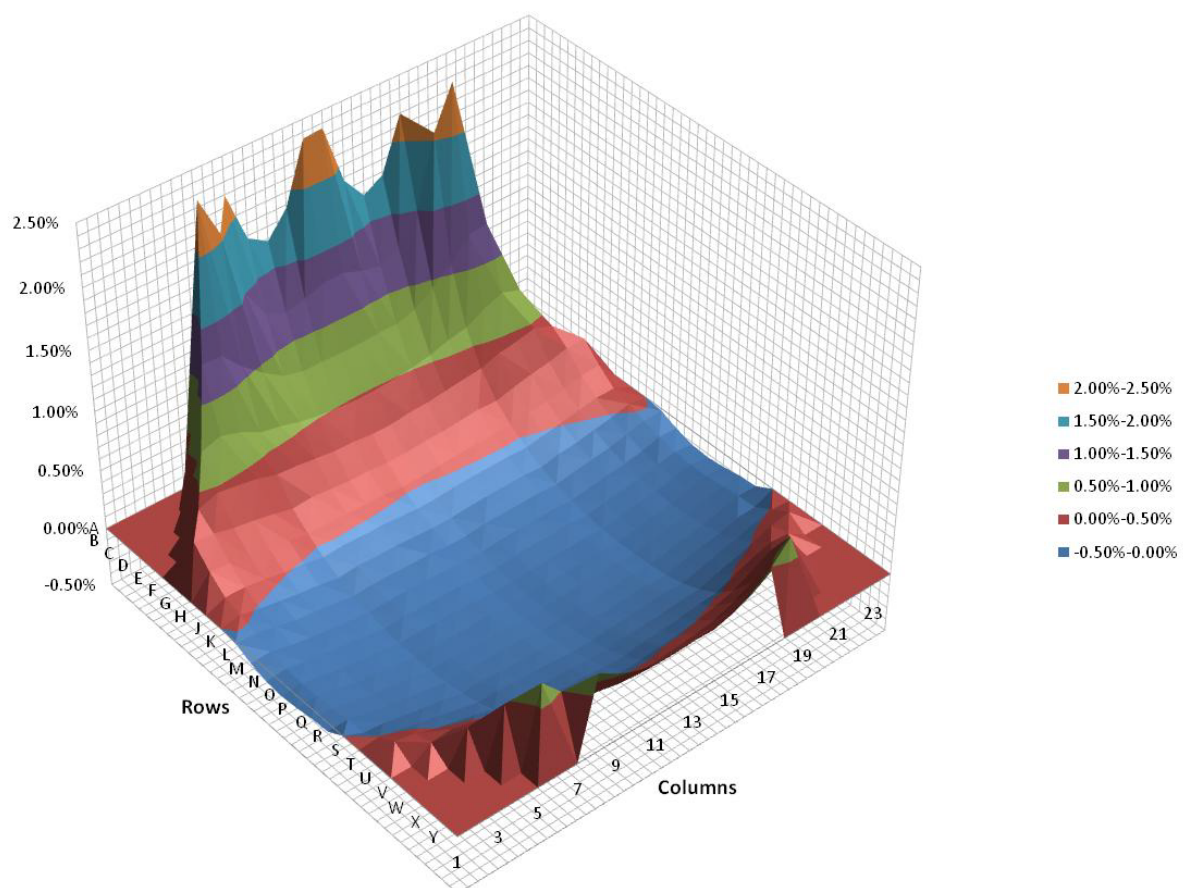


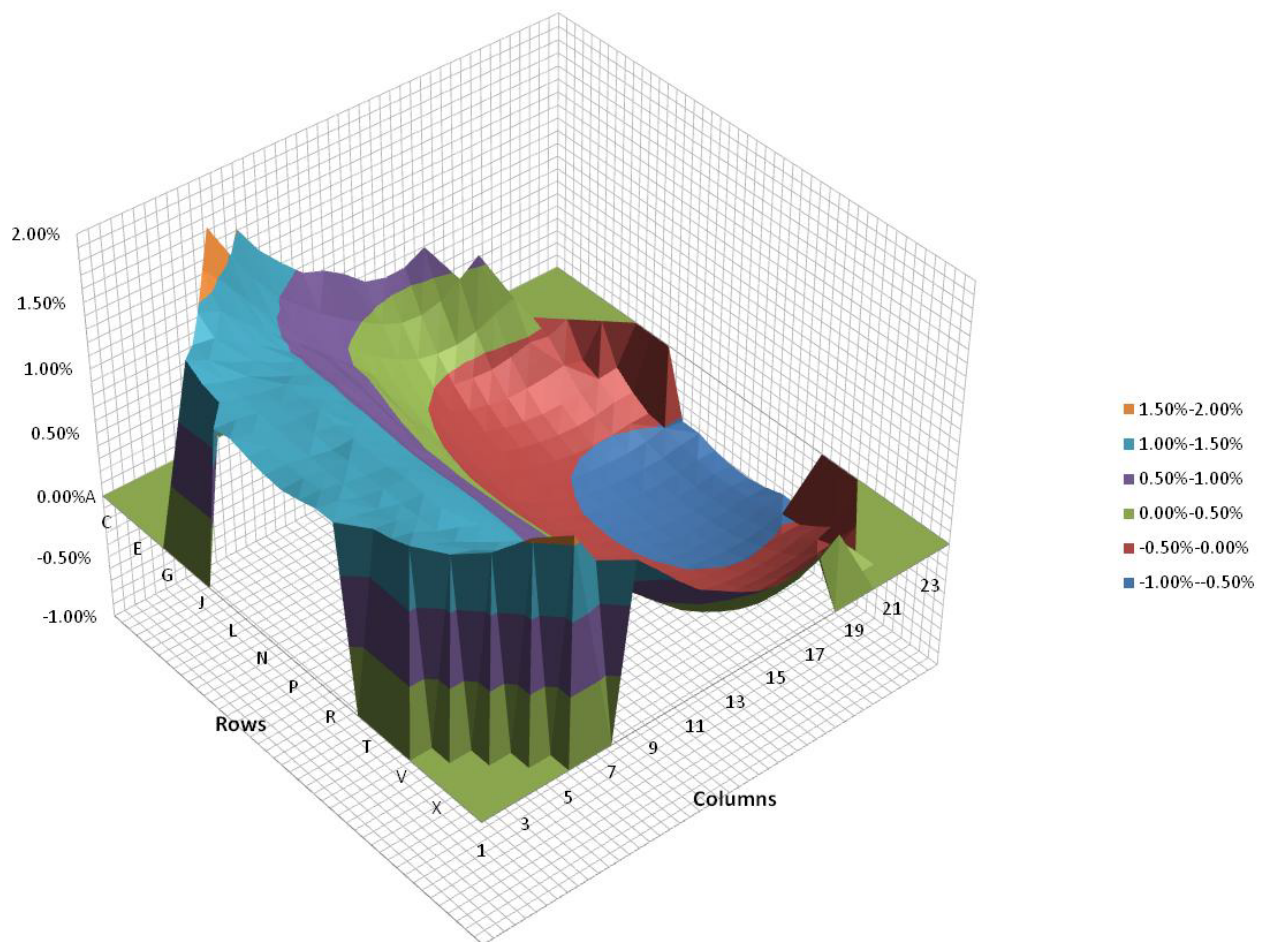
Figure 2 Code Structure Implemented in the WIMS-to-PMAXS Module



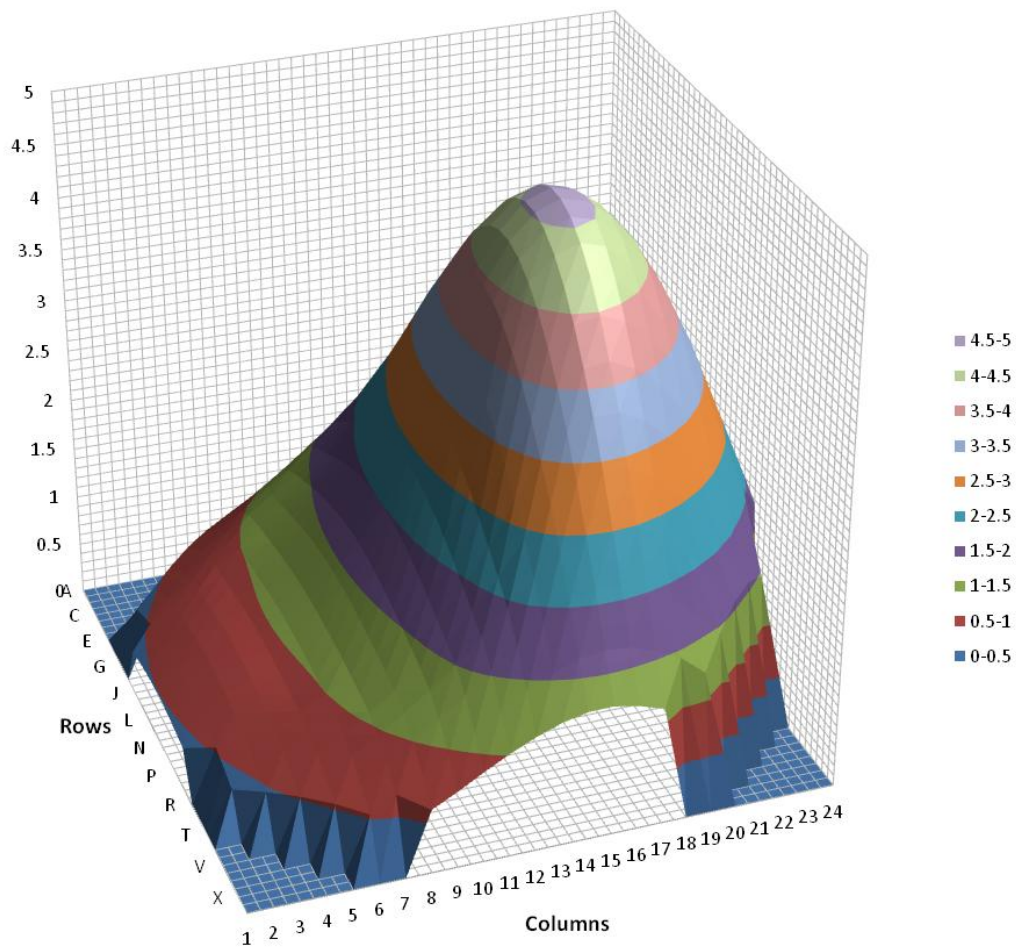
**Figure 3 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and RFSP-IST for the Reference Case (PARCS-RFSP-IST) $\times 100\%$ /RFSP-IST**



**Figure 4 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and RFSP-IST for the LZCs at 100% (PARCS-RFSP-IST)X100%/RFSP-IST**



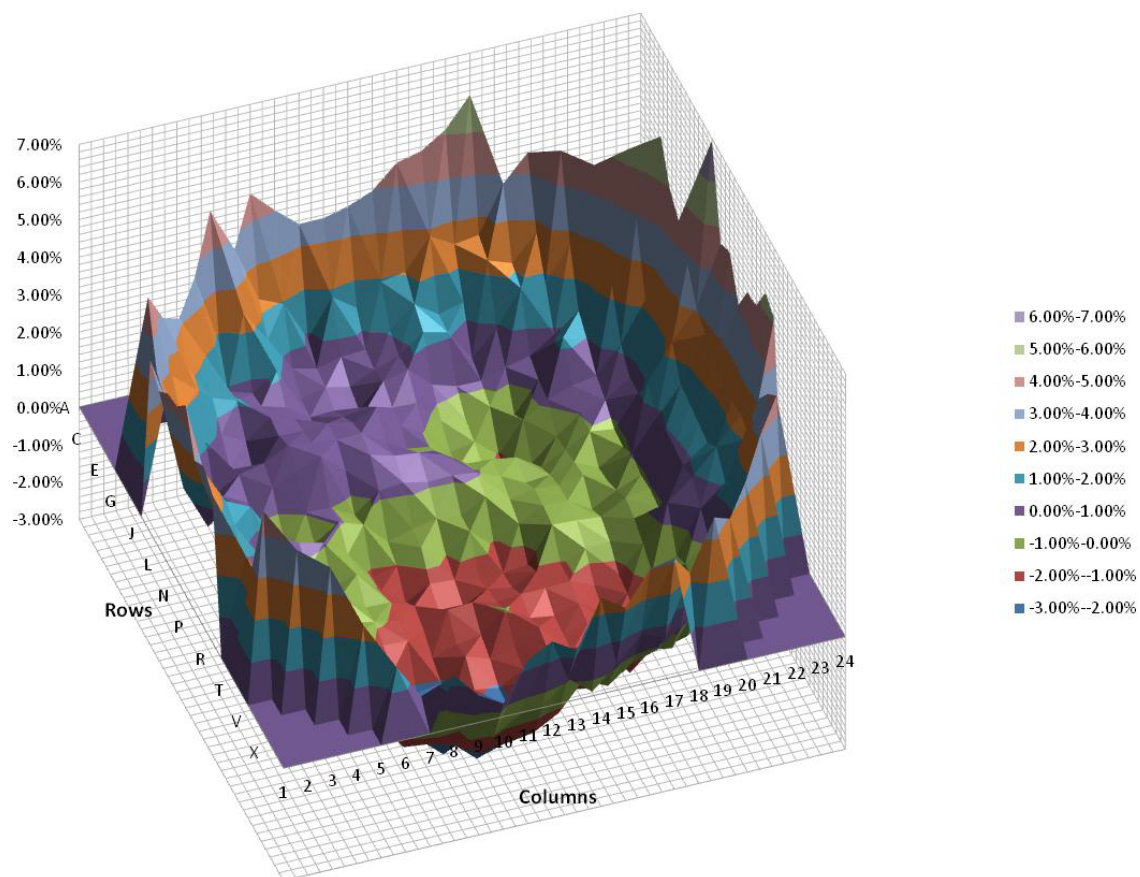
**Figure 5 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and RFSP-IST for the Asymmetry (PARCS-RFSP-IST)X100%/RFSP-IST**



**Figure 6 Channel Power Distribution Calculated with PARCS (FDM, 1-group Boundary Condition) for the Asymmetric Case<sup>1</sup>**

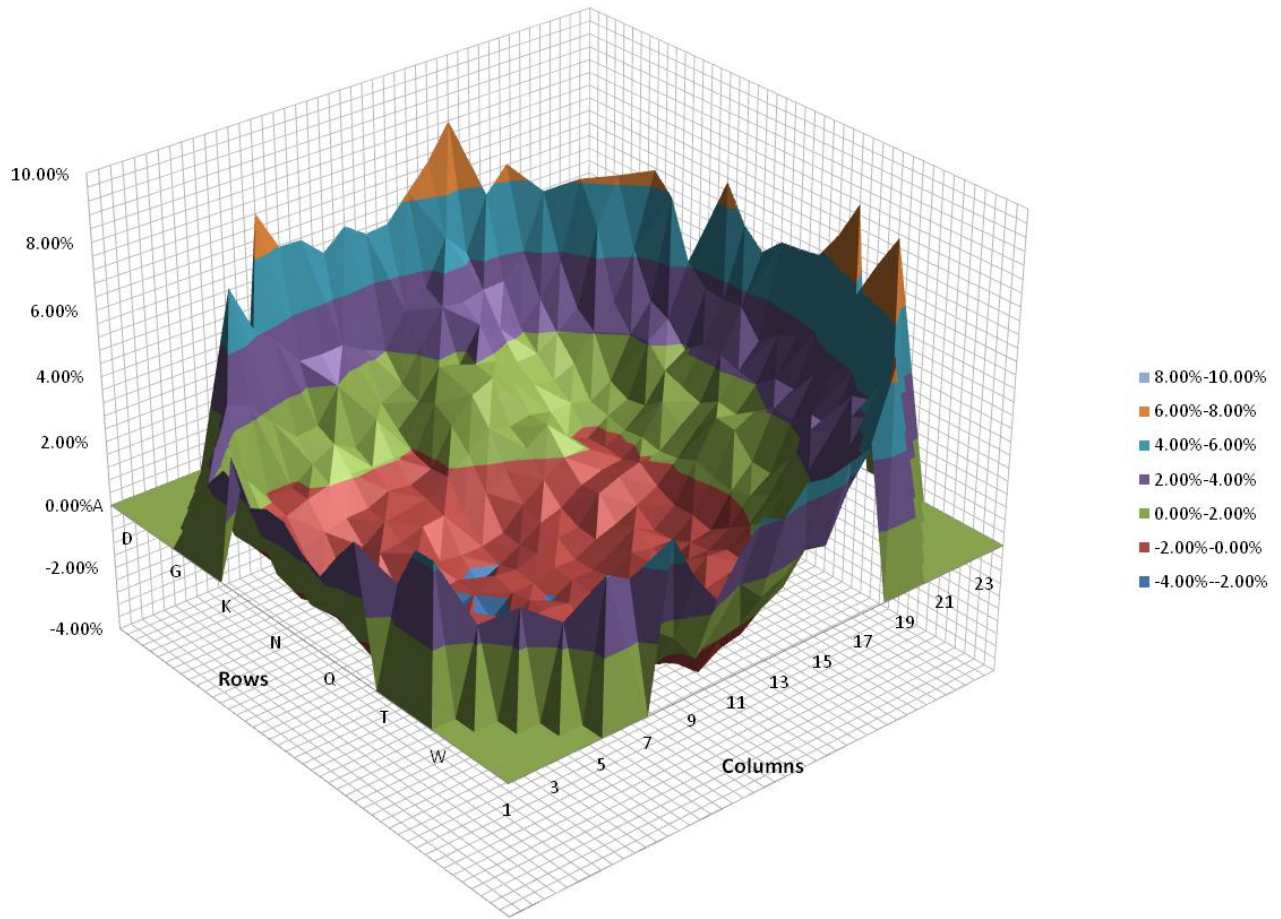
<sup>1</sup> Sum of all channel powers is equal to 1000.



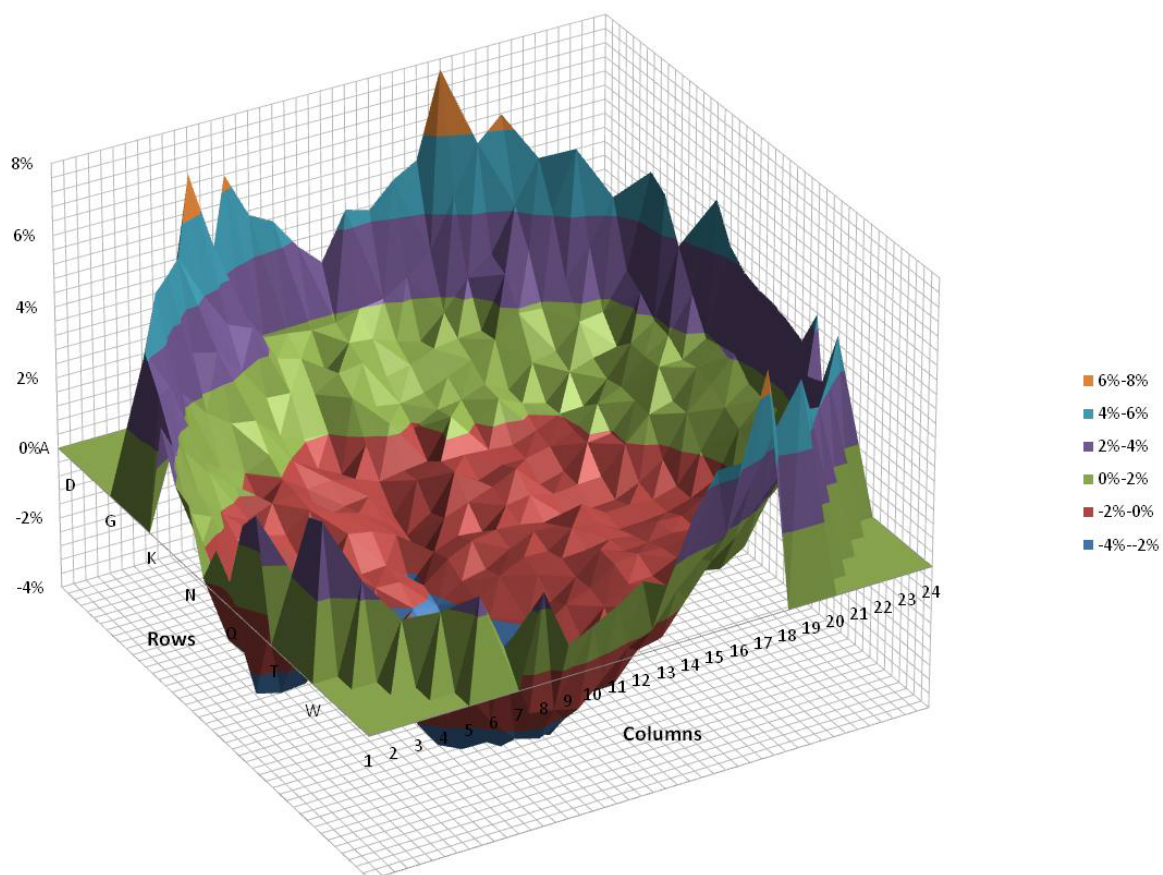


**Figure 7 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP**

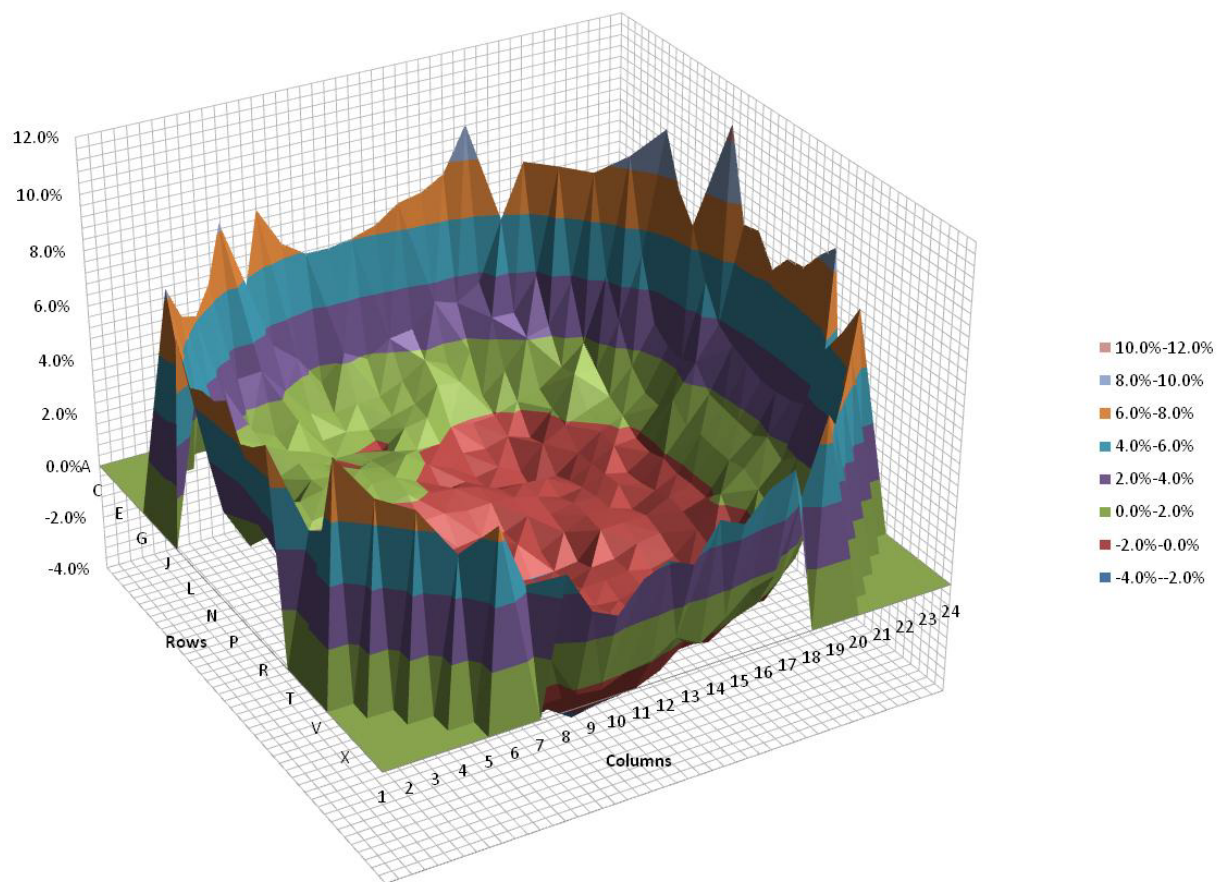




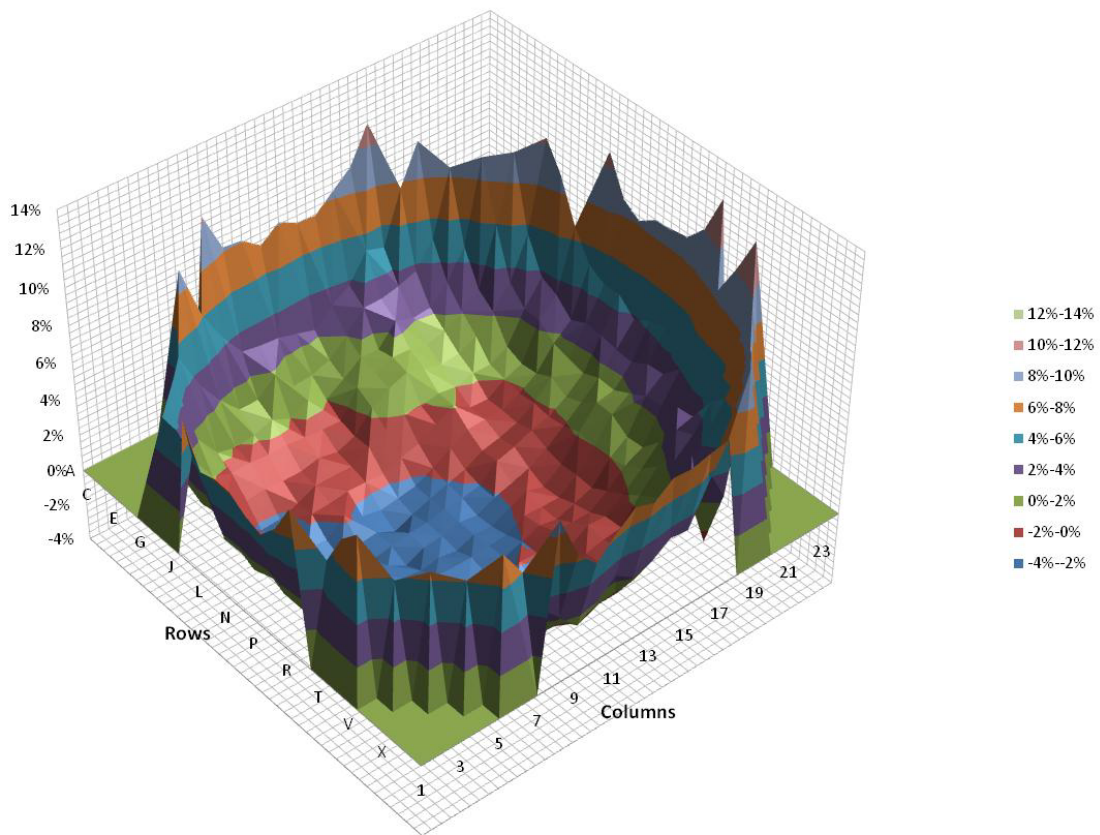
**Figure 8 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP**



**Figure 9 Differences in Channel Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the Asymmetry (PARCS-MCNP) X100%/MCNP**

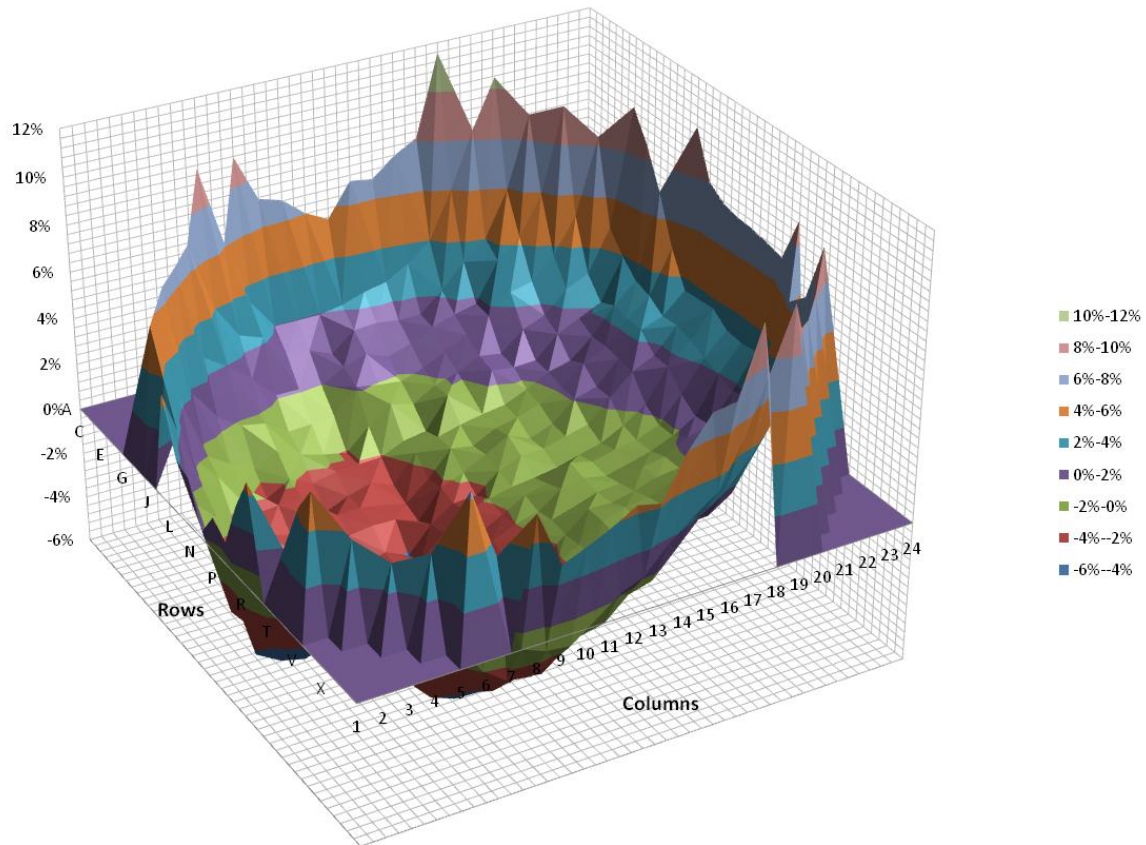


**Figure 10 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 1-group Boundary Condition) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP**

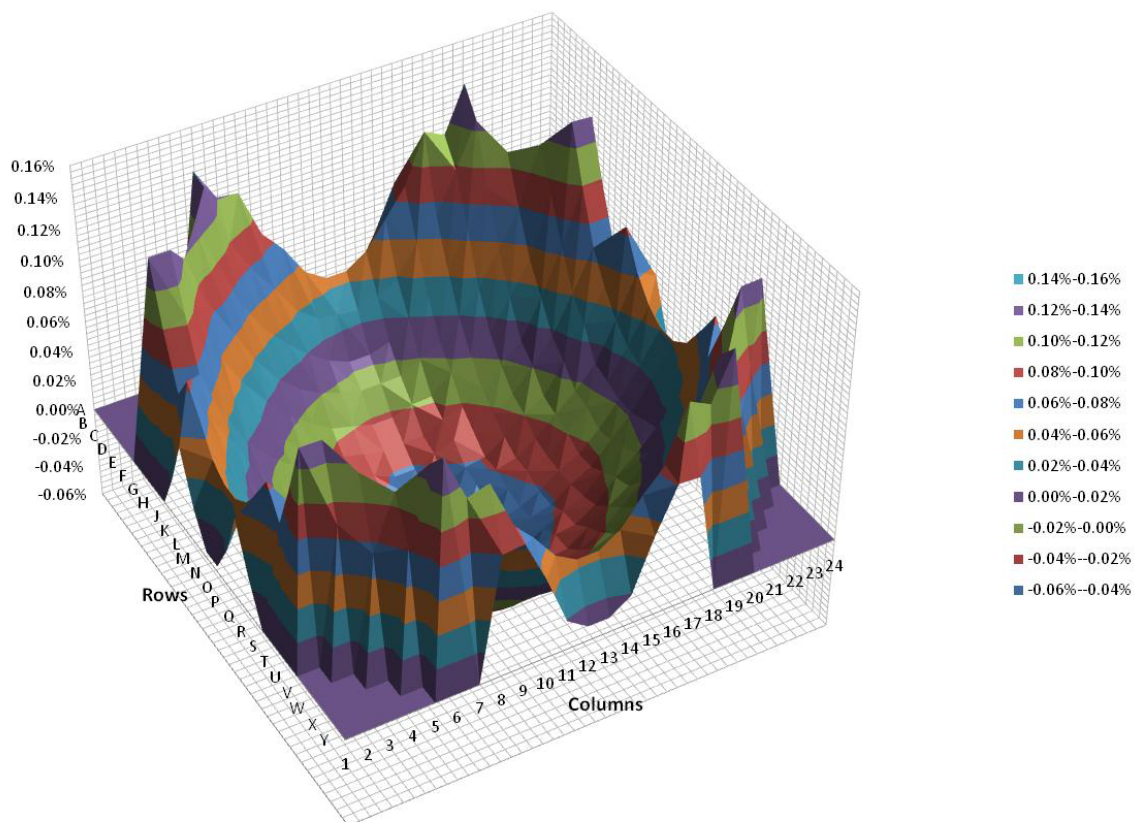


**Figure 11 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 1-group Boundary Condition) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP**

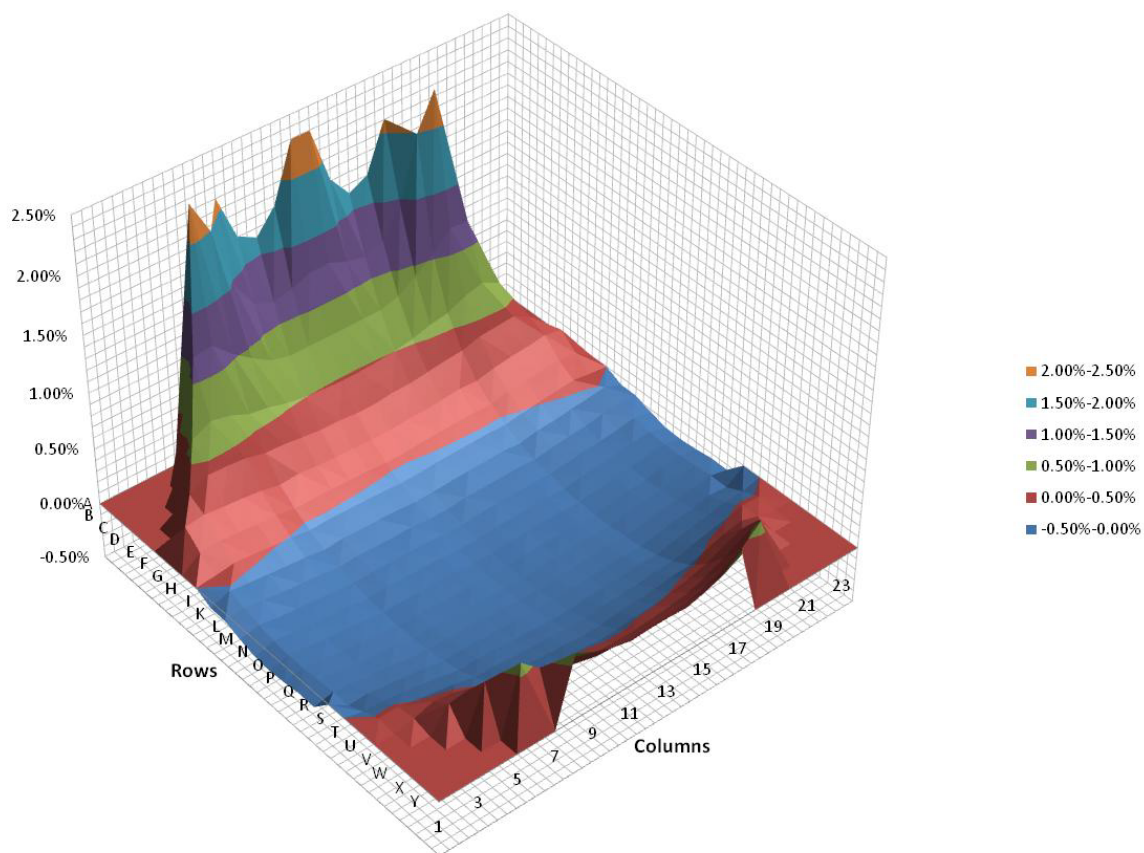




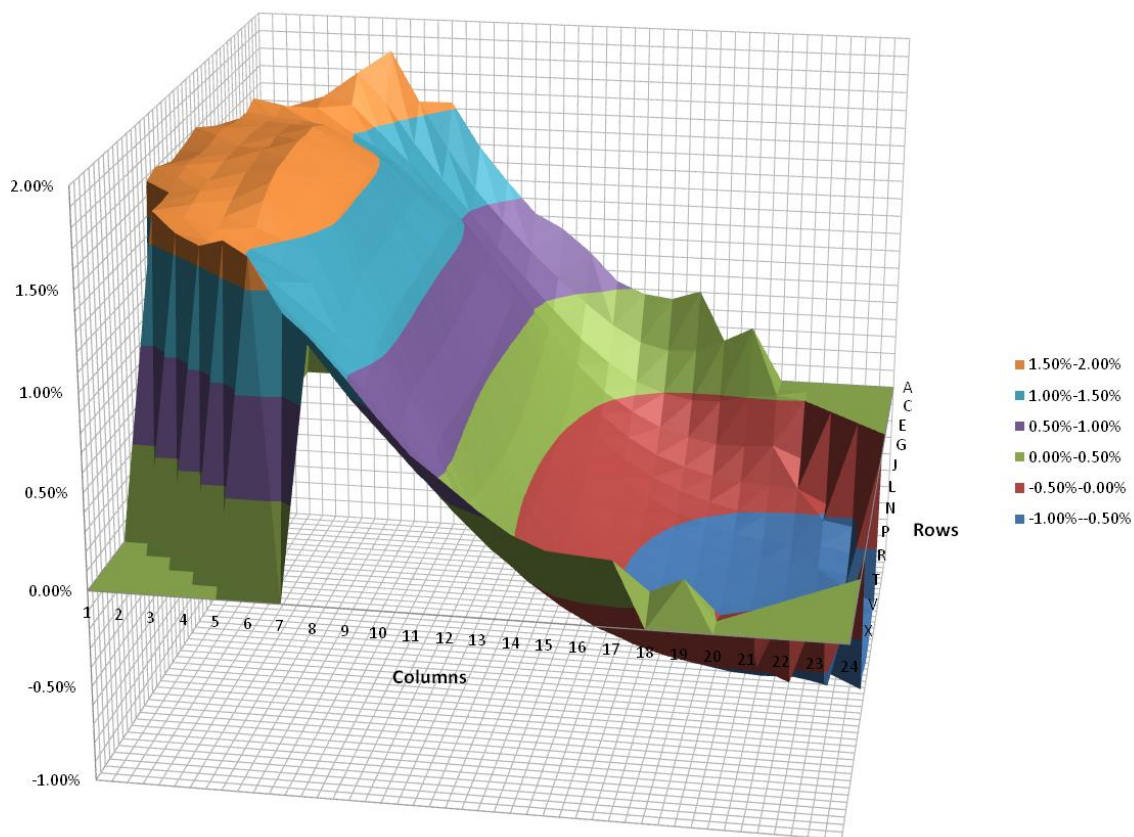
**Figure 12 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 1-group Boundary Condition) and MCNP for the Asymmetry (PARCS-MCNP)X100%/MCNP**



**Figure 13 Differences in Channel Power Calculated Between PARCS (FDM, 2-group Boundary Condition) and RFSP-IST (FDM, 1-group Boundary Condition) for the Reference Case (PARCS-RFSP-IST)X100%/RFSP-IST**

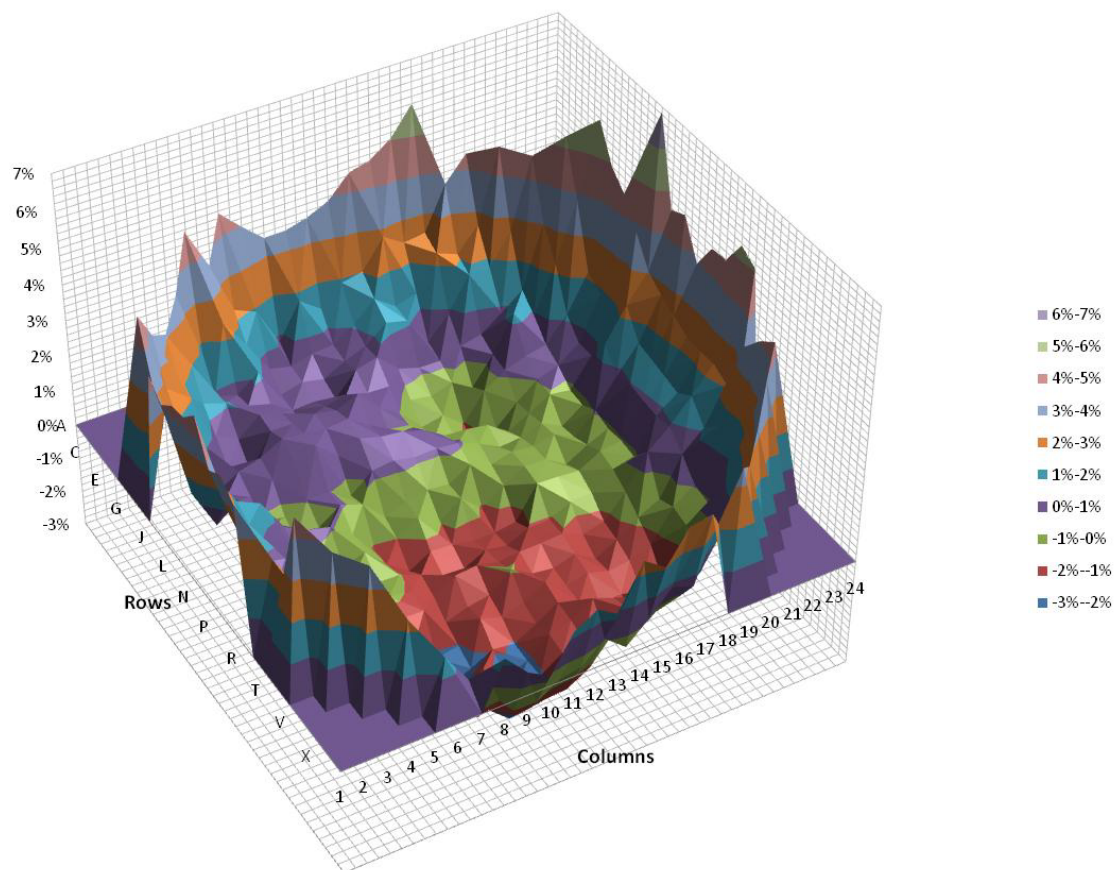


**Figure 14 Differences in Channel Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and RFSP-IST (FDM, 1-group Boundary Condition) for the LZCs at 100%  $(\text{PARCS}-\text{RFSP-IST}) \times 100\% / \text{RFSP-IST}$**

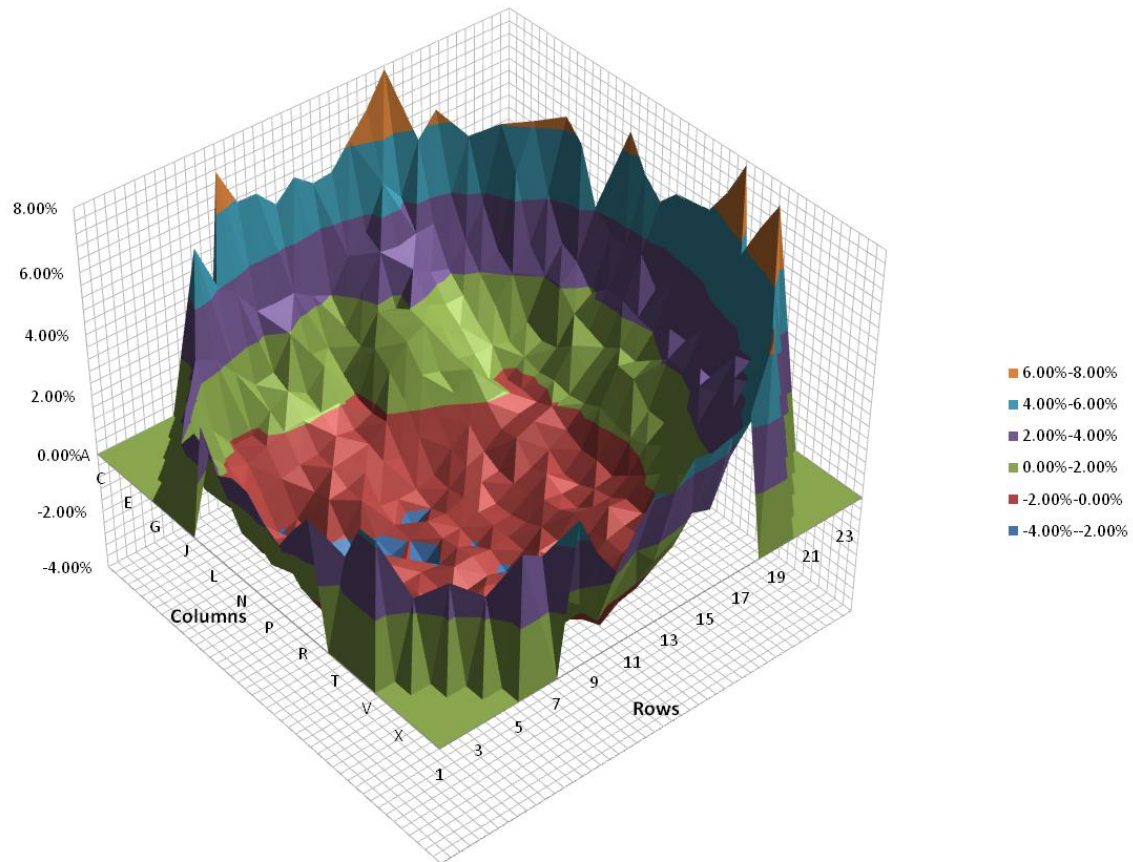


**Figure 15 Differences in Channel Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and RFSP-IST (FDM, 1-group Boundary Condition) for the Asymmetry  $(\text{PARCS}-\text{RFSP-IST}) \times 100\% / \text{RFSP-IST}$**

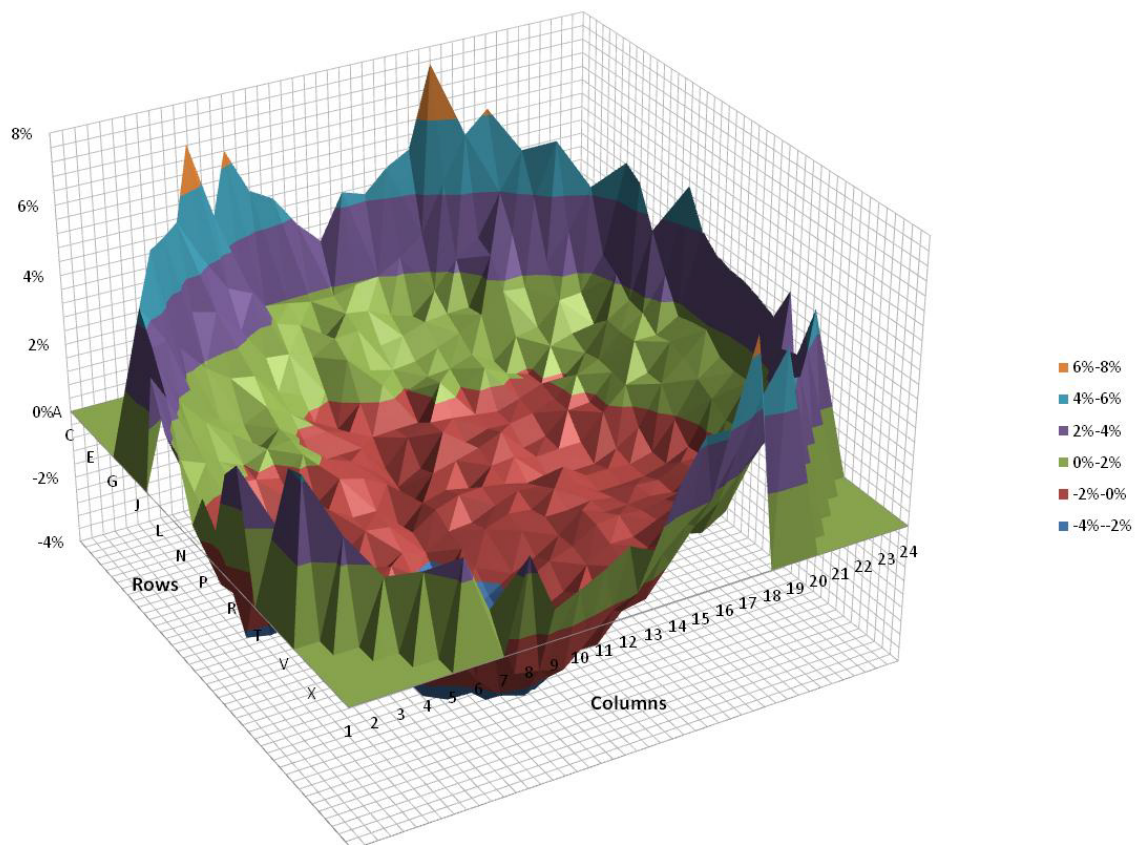




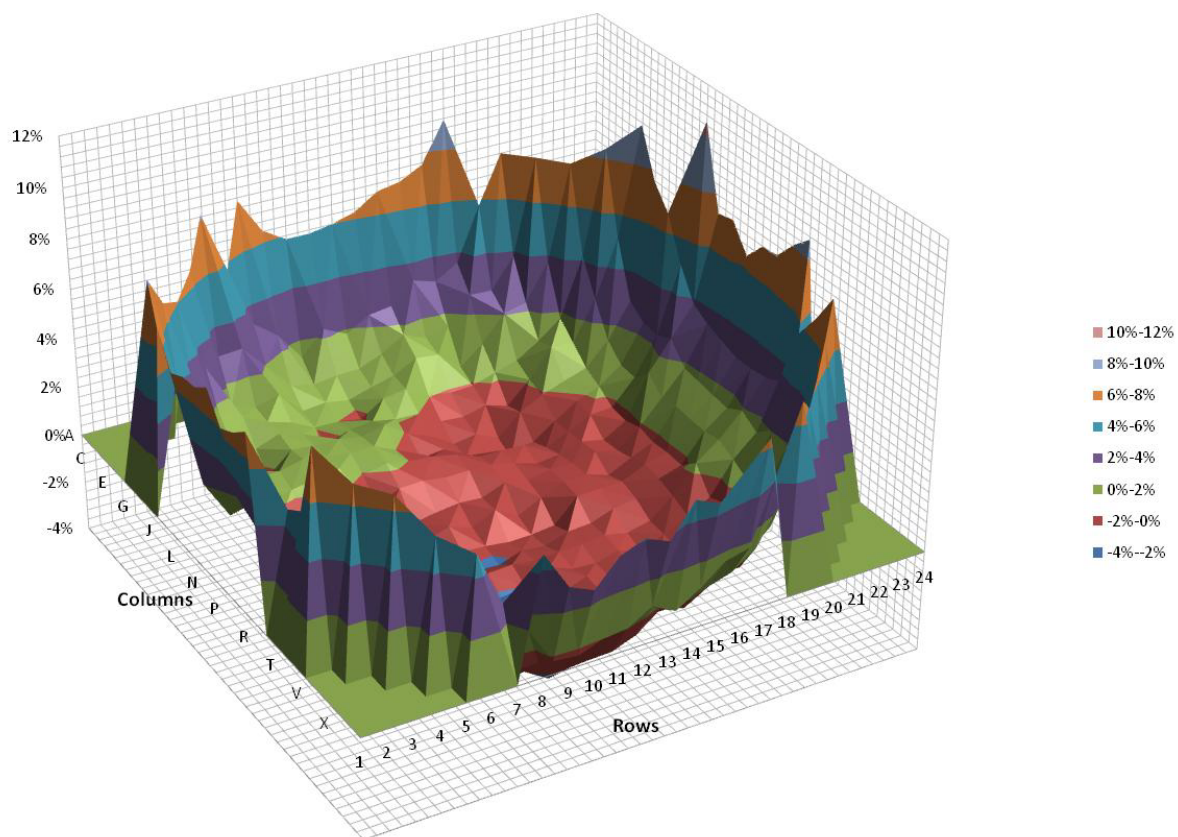
**Figure 16 Differences in Channel Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP**



**Figure 17 Differences in Channel Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP**

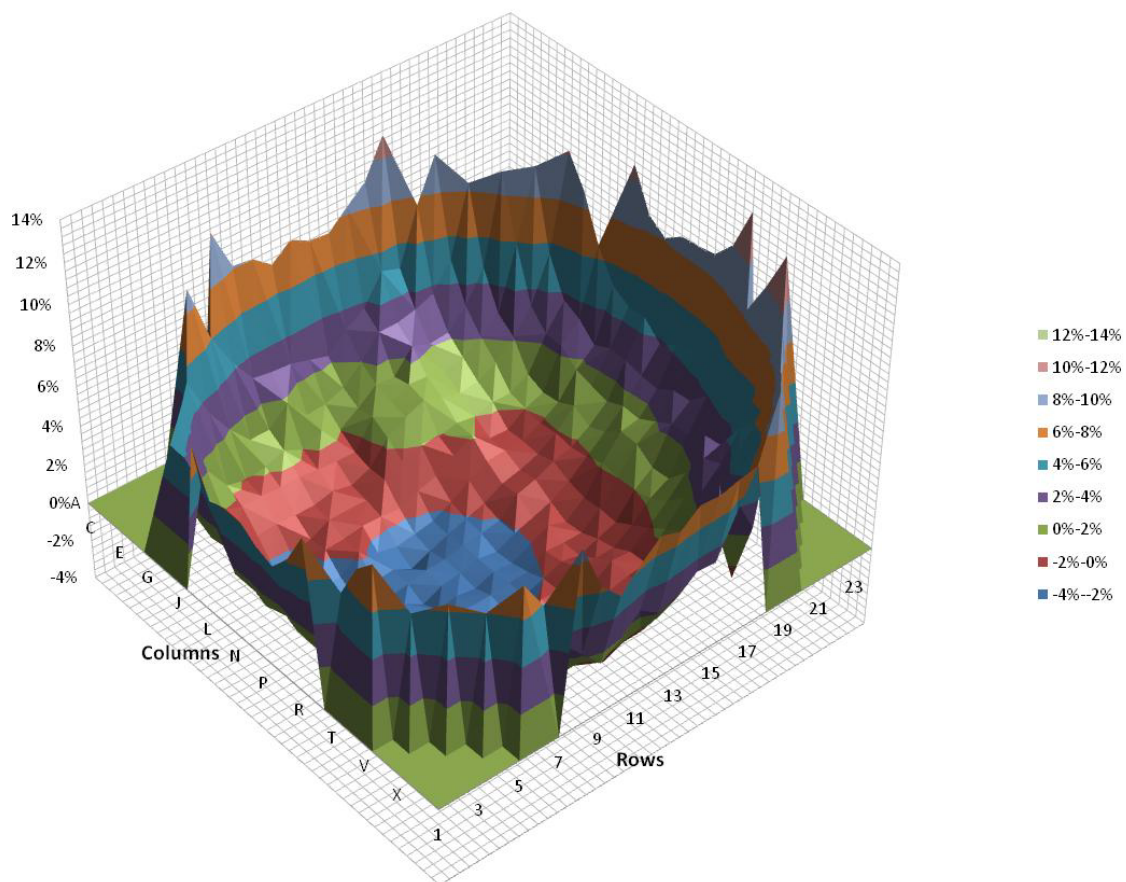


**Figure 18 Differences in Channel Power Calculated Between PARCS (FDM, 2-group BoundaryConditions) and MCNP for the Asymmetry (PARCS-MCNP)X100%/MCNP**

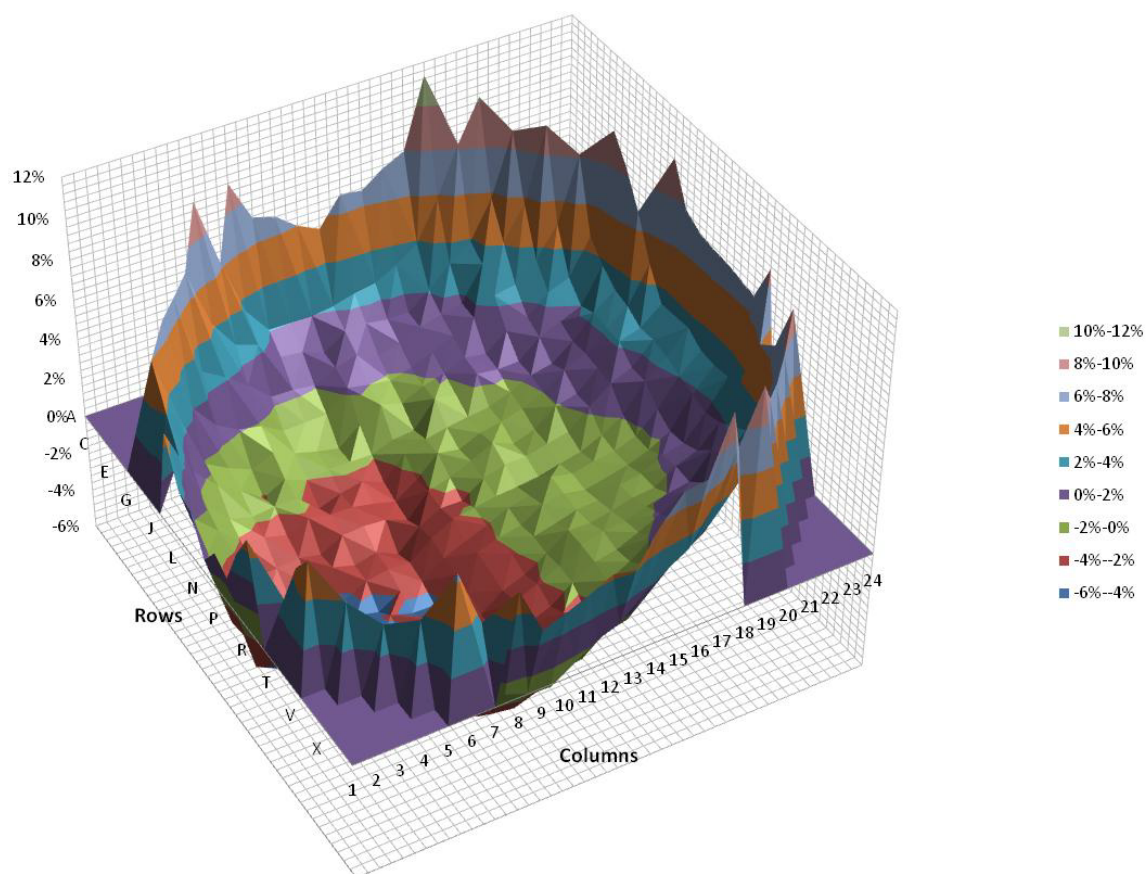


**Figure 19 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 2-group Boundary Conditions) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP**

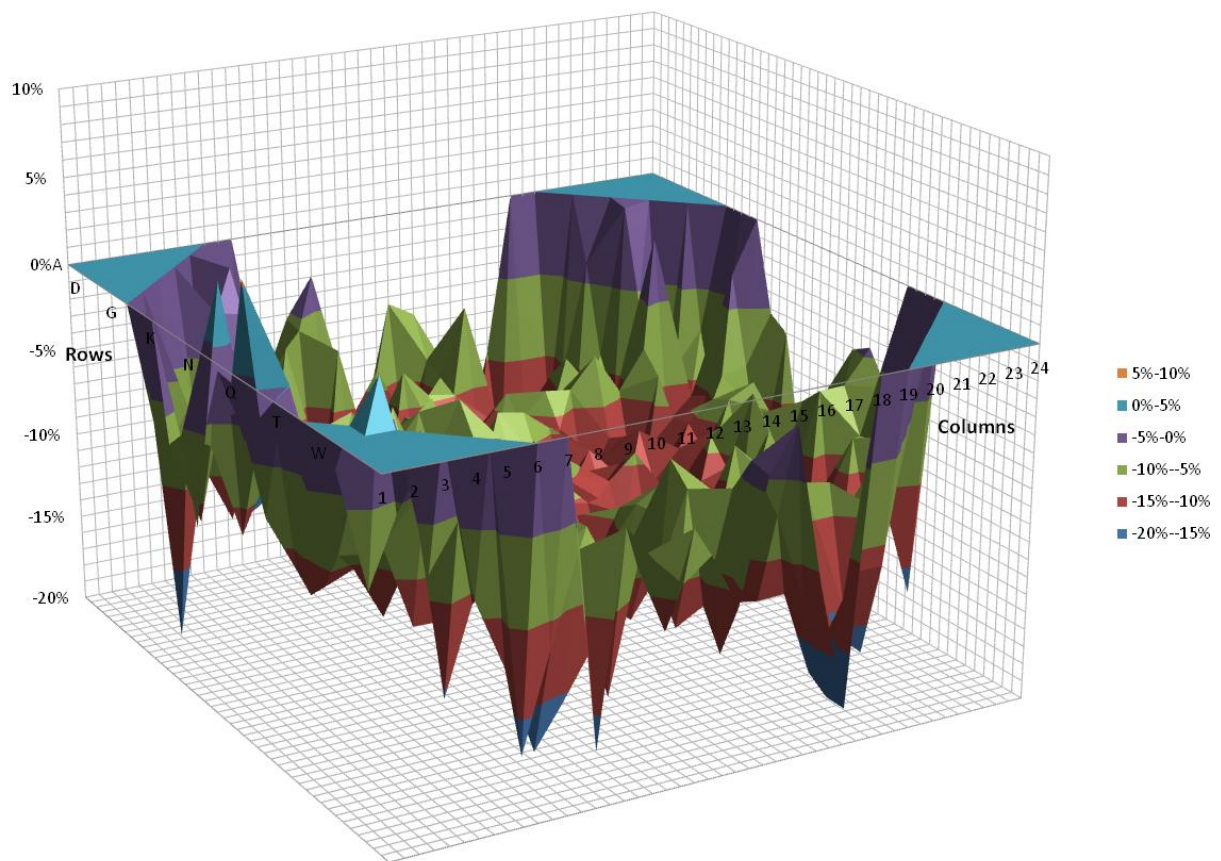




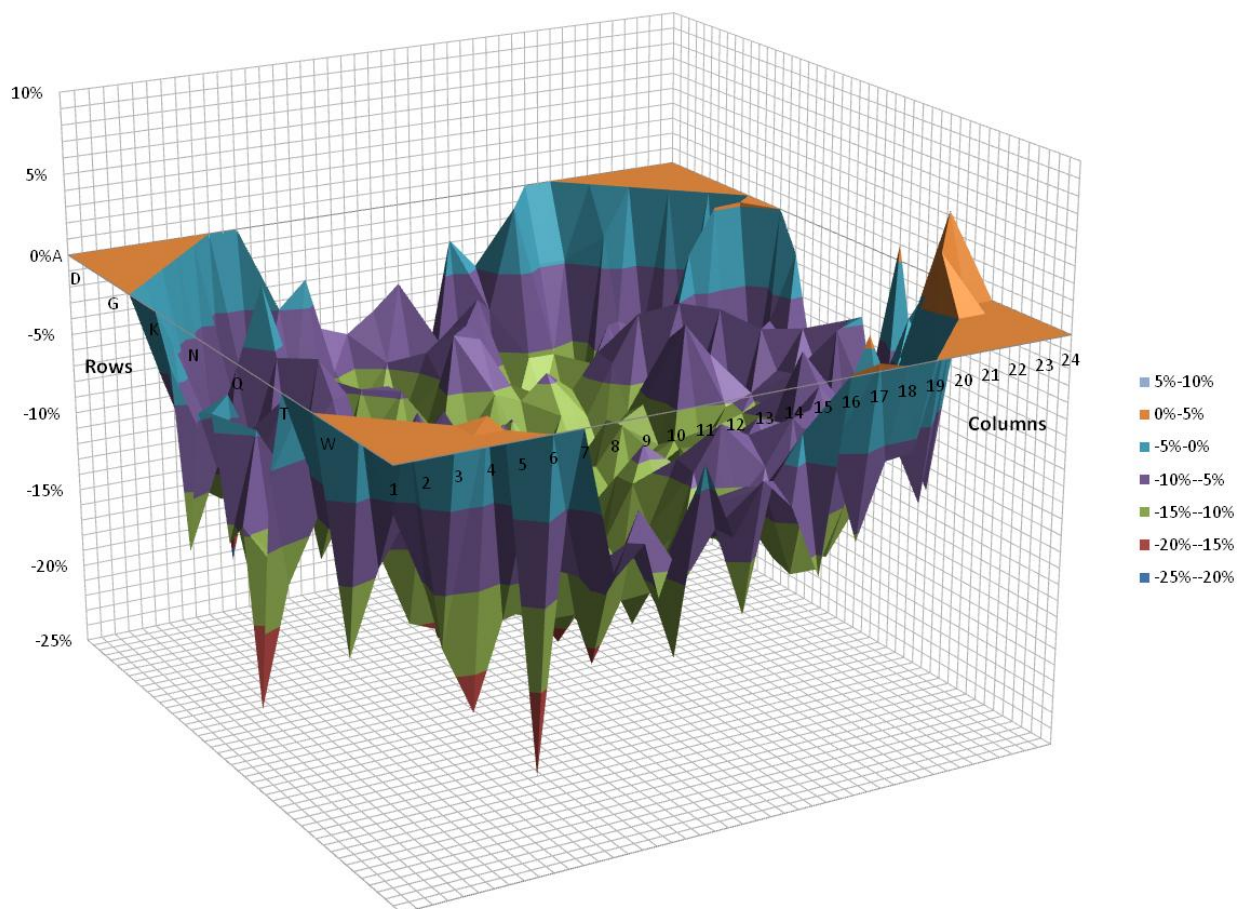
**Figure 20 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 2-group Boundary Conditions) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP**



**Figure 21 Differences in Channel Power Calculated Between PARCS (Hybrid NEM/ANM, 2-group Boundary Conditions) and MCNP for the Asymmetry (PARCS-MCNP)X100%/MCNP**

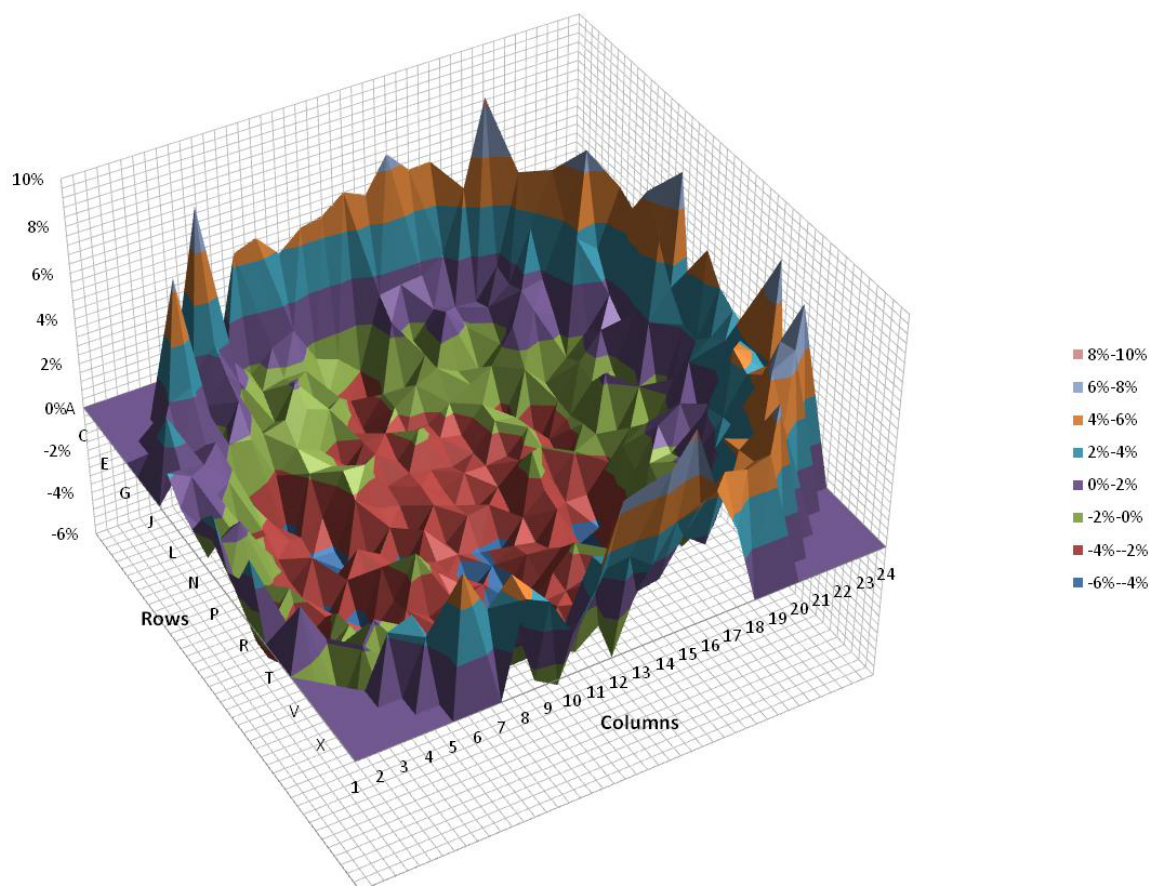


**Figure 22 Differences in Bundle Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP – Plane Number 1**

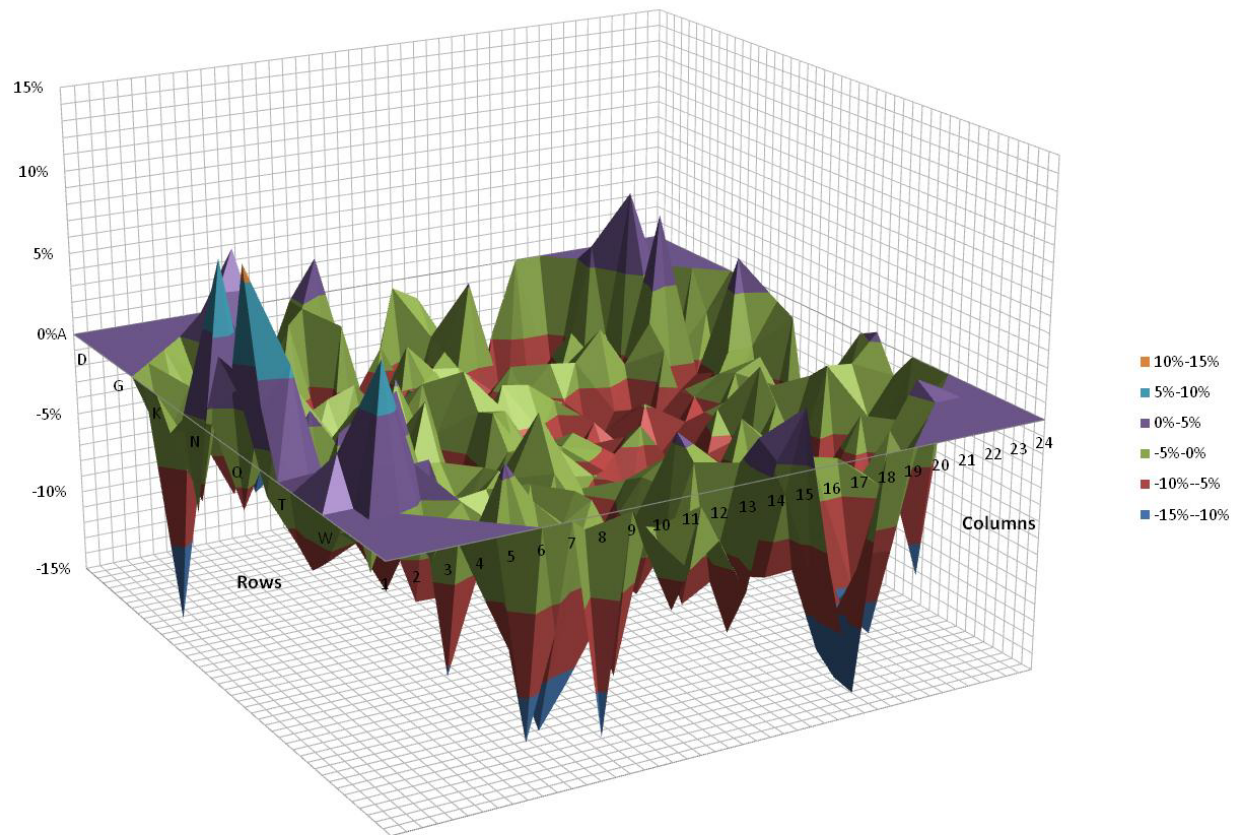


**Figure 23 Differences in Bundle Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP – Plane Number 1**

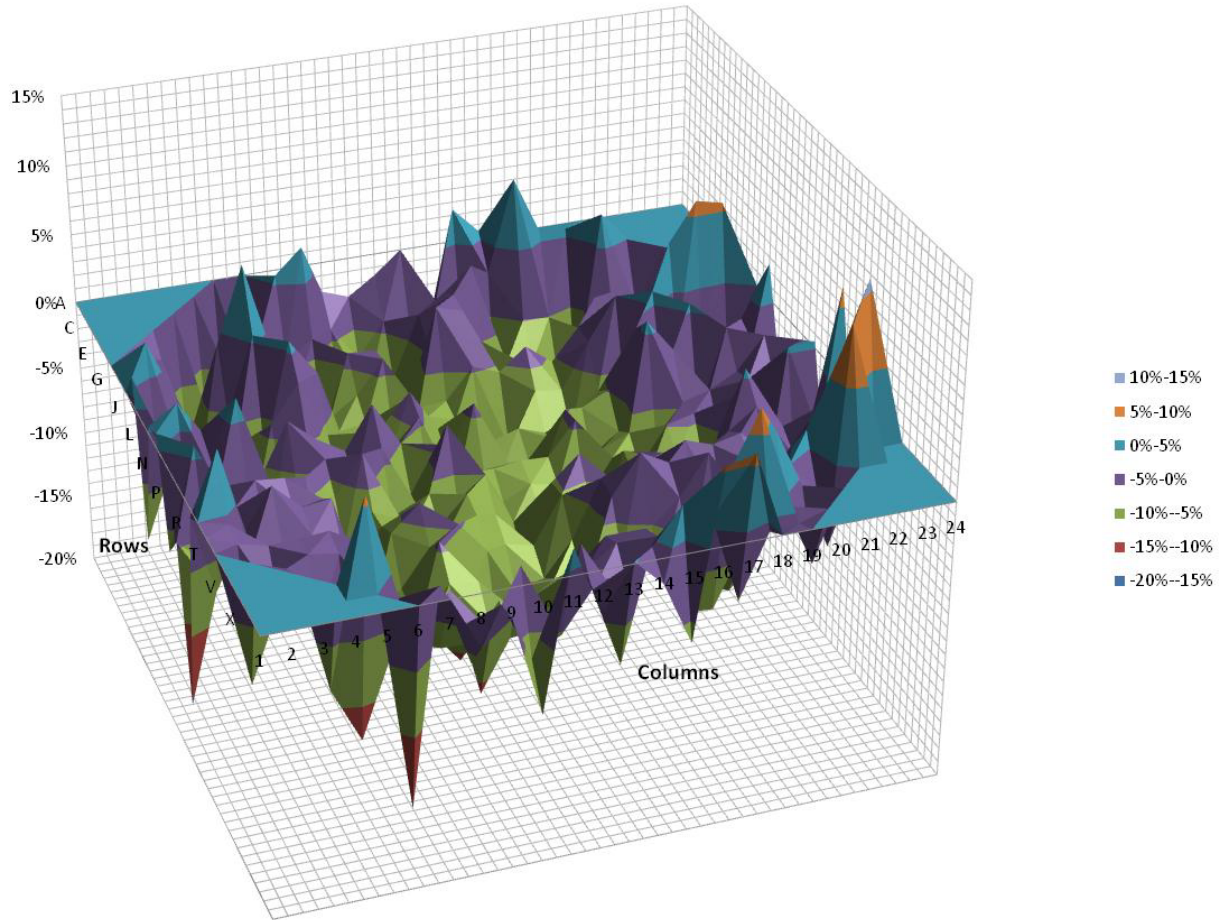




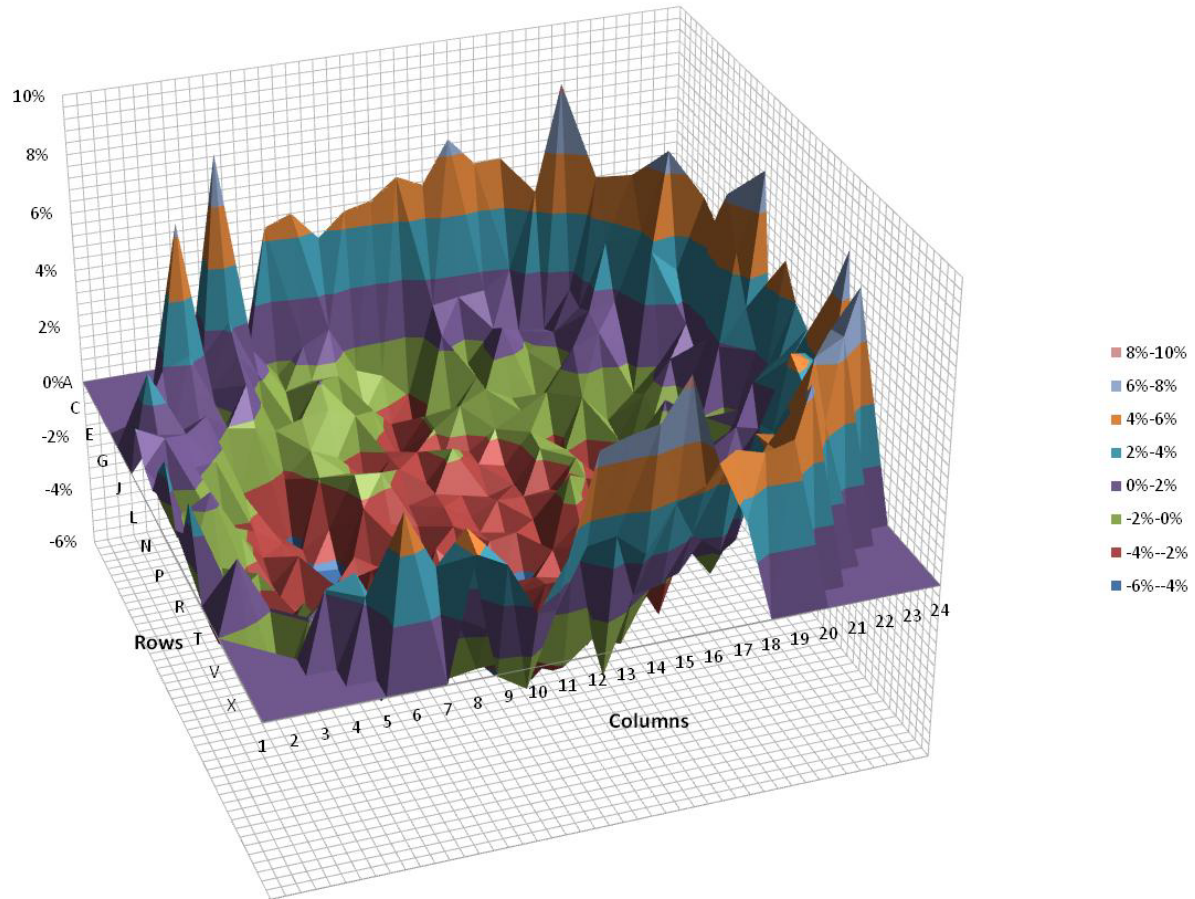
**Figure 24 Differences in Bundle Power Calculated Between PARCS (FDM, 1-group Boundary Condition) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP – Plane Number 4**



**Figure 25 Differences in Bundle Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and MCNP for the Reference Case (PARCS-MCNP)X100%/MCNP – Plane Number 1**



**Figure 26 Differences in Bundle Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP – Plane Number 1**



**Figure 27 Differences in Bundle Power Calculated Between PARCS (FDM, 2-group Boundary Conditions) and MCNP for the LZCs at 100% (PARCS-MCNP)X100%/MCNP – Plane Number 4**

## APPENDIX C PARCS USER'S MANUAL UPDATE ASSOCIATED WITH THE BOUNDARY CONDITIONS

Card Type	Field	Default	Description
ALBEDO_N	Bcsetnum	None	The number of albedos to be input is specified by bcsetnum. The albedo is specified, for each bcsetnum, for each energy group for the (north, south, east, or west) face of the problem domain. The last line of the input is a linear “map” of albedo set numbers specifying which albedo set will be used for that axial position.
	albn(bcsetnum,ng)		
	irbemap(nz)		
ALBEDO_S	bcsetnum	None	
	albs(bcsetnum,ng)		
	irbemap(nz)		
ALBEDO_E	Bcsetnum	None	In the example, three sets are input, one albedo for each of the two energy groups. In plane 1, set 1 is used, in plane 2 set 2, 3 set 3, 4 set 2, and 5 set 1.
	albe(bcsetnum,ng)		
	irbemap(nz)		
ALBEDO_W	bcsetnum	None	
	albw(bcsetnum,ng)		
	irbemap(nz)		
	ALBEDO_* 3 0.0 0.0 0.33 0.4 0.5 0.5 1 2 3 2 1		
ALBEDO_T	bcsetnum	None	The number of albedos to be input is specified by bcsetnum. The albedo is specified, for each bcsetnum, for each energy group for the (top or bottom) face of the problem domain.
	albt(bcsetnum,ng)		
ALBEDO_B	bcsetnum	None	
	albb(bcsetnum,ng)		
	ALBEDO_T 2 0.0 0.0 100000.0 1000000.0		
	BC_ZT_MAP	izbemap(nfa)	nfa*1
BC_ZB_MAP	izbemap(nfa)	nfa*1	
BC_ZT_MAP 1 2 1 2 2 2 1 2 1			



EXTRAP_D_R	bcsetnum	None	<p>The number of extrapolation distances to be input is specified by bcsetnum. The extrap. dist. is specified, for each bcsetnum, for each energy group. The last line of the input is a linear “map” of the set numbers specifying which set will be used for that axial position.</p> <p>The example has 2 sets of extrapolation distances, specifying distances for each energy group and a geometric radius to use for each set. Plane 1 uses set 1, 2-3 use 2, and 4 uses 1.</p>
	extrapdistr (bcsetnum,ng)		
	extraprad(bcsetnum)		
	Irbcmap(nz)		
	EXTRAP_D_R 2 2.0 2.0 28.0 2.5 2.7 29.0 1 2 2 1		
EXTRAP_D_Z	bcsetnum	None	<p>The number of extrapolation distances to be input is specified by bcsetnum. The set is specified, for each bcsetnum, for each energy group of the problem domain. Should be used in conjunction with the BC_Z*_MAP card(s).</p> <p>In the example, two sets are input, one extrap. dist. for each of the two energy groups.</p>
	extrapdistz (bcsetnum,ng)		
	EXTRAP_D_Z 2 3.5 3.7 2.6 2.43		

## APPENDIX D<sup>1</sup> CODING ADDED INTO THE ANM DRIVER IN PARCS TO ACCOMMODATE THE NEW BOUNDARY CONDITIONS

For NEM, we start with the transverse integrated 1D diffusion equation,

$$-D \frac{d^2 \phi_g(x)}{dx^2} + \Sigma_{tg} \phi_g(x) - \frac{\chi_g}{k} \sum_{g'=1}^G \nu \Sigma_{tg'} \phi_{g'}(x) - \sum_{g'=1}^G \Sigma_{g,g'} \phi_{g'}(x) = S_g(x) = S_g^{tf}(x) - L_g(x) \quad (1)$$

Define the vectors and matrices,

$$\begin{aligned} \bar{\phi} &= \begin{bmatrix} \phi_1 \\ \phi_2 \\ \vdots \\ \phi_G \end{bmatrix}, \bar{J} = \begin{bmatrix} J_1 \\ J_2 \\ \vdots \\ J_G \end{bmatrix}, \bar{S} = \begin{bmatrix} S_1 \\ S_2 \\ \vdots \\ S_G \end{bmatrix}, \bar{A} = \bar{K} - \bar{S} - \frac{1}{k} \bar{\chi} \bar{F}^T, \bar{\chi} = \begin{bmatrix} \chi_1 \\ \chi_2 \\ \vdots \\ \chi_G \end{bmatrix} \\ \bar{F} &= \begin{bmatrix} \nu \Sigma_{f1} \\ \nu \Sigma_{f2} \\ \vdots \\ \nu \Sigma_{fG} \end{bmatrix}, \bar{S} = \begin{bmatrix} \Sigma_{1,1} & \Sigma_{1,2} & \cdots & \Sigma_{1,G} \\ \Sigma_{2,1} & \Sigma_{2,2} & \cdots & \Sigma_{2,G} \\ \vdots & \vdots & \ddots & \vdots \\ \Sigma_{G,1} & \Sigma_{G,2} & \cdots & \Sigma_{G,G} \end{bmatrix}, \bar{K} = \begin{bmatrix} \Sigma_{t1} & 0 & \cdots & 0 \\ 0 & \Sigma_{t2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \Sigma_{tG} \end{bmatrix}, \text{ and} \\ \bar{D} &= \begin{bmatrix} D_1 & 0 & \cdots & 0 \\ 0 & D_2 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & D_G \end{bmatrix}, \end{aligned}$$

Then, diffusion equation (1) can be rewritten in matrix form,

$$-\bar{D} \frac{d^2}{dx^2} \bar{\phi}(x) + \bar{A} \bar{\phi}(x) = \bar{S}(x) \quad (2)$$

Define non-dimensional variable  $\xi = \frac{x}{h} - \frac{x_r + x_l}{2h}, h = \frac{x_r - x_l}{2}$

The Diffusion equation becomes

$$-\frac{\bar{D}}{h^2} \frac{d^2}{d\xi^2} \bar{\phi}(\xi) + \bar{A} \bar{\phi}(\xi) = \bar{S}(\xi) \quad (3)$$

Approximate the transverse leakage and transient fix source with 2<sup>nd</sup> order polynomial

$$S_g(\xi) = \sum_{i=0}^2 s_{g,i} P_i(\xi)$$

$$P_0(\xi) = 1, P_1(\xi) = \xi, P_2(\xi) = \frac{1}{2}(3\xi^2 - 1), P_3(\xi) = \frac{1}{2}(5\xi^3 - 3\xi), P_4(\xi) = \frac{1}{8}(35\xi^4 - 30\xi^2 + 3)$$

<sup>1</sup> Equations listed in the Appendix that constitute the coding implemented in PARCS was provided by University of Michigan

$$P_0'(\xi) = 0, P_1'(\xi) = 1, P_2'(\xi) = 3\xi, P_3'(\xi) = 5P_2(\xi) + 1, P_4'(\xi) = 7P_3(\xi) + 3\xi$$

$$P_0''(\xi) = 0, P_1''(\xi) = 0, P_2''(\xi) = 3P_0(\xi), P_3''(\xi) = 15\xi, P_4''(\xi) = 35P_2(\xi) + 10$$

$$s_0 = s^c$$

$$s_1 = G^{-1}h^c \left[ (s^r - s^c)(h^c + 2h^l)(h^c + h^l) - (s^l - s^c)(h^c + 2h^r)(h^c + h^r) \right]$$

$$s_2 = G^{-1}(h^c)^2 \left[ (s^r - s^c)(h^c + h^l) + (s^l - s^c)(h^c + h^r) \right]$$

$$G = 2(h^c + h^l)(h^c + h^r)(h^c + h^l + h^r)$$

The Diffusion equation can be rewritten as,

$$-\frac{D}{h^2} \frac{d^2}{d\xi^2} \bar{\phi}(\xi) + \bar{A} \bar{\phi}(\xi) = \sum_{i=0}^2 \bar{s}_i P_i(\xi) \quad (4)$$

Approximate the solution with 4<sup>th</sup> order Legendre polynomials

$$\bar{\phi}(\xi) = \sum_{i=0}^4 \bar{a}_i P_i(\xi) \quad (5)$$

The 5G coefficients of Legendre polynomials will be determined by 5G constraints.

For the boundary node, these constraints are average flux, 0<sup>th</sup> (nodal neutron balance), 1<sup>st</sup> and 2<sup>nd</sup> order WRE and the boundary condition.

$$\bar{a}_0 = \bar{\phi}$$

Define:  $\bar{D} = \left( \frac{D}{h} \right)$ ,  $\bar{K} = \left( \frac{D}{h^2} \right)^{-1}$  are diagonal matrices.

$$\text{2<sup>nd</sup> order WRE: } \bar{a}_4 = \frac{1}{35} \bar{K} (\bar{A} \bar{a}_2 - \bar{s}_2)$$

$$\text{0<sup>th</sup> order WRE: } 3\bar{a}_2 + 10\bar{a}_4 = \bar{K} (\bar{A} \bar{a}_0 - \bar{s}_0)$$

$$\bar{a}_2 = \left( 21I + 2\bar{K} \bar{A} \right)^{-1} \bar{K} (7\bar{A} \bar{a}_0 - 7\bar{s}_0 + 2\bar{s}_2)$$

$$\text{1<sup>st</sup> order WRE: } -15\bar{a}_3 + \bar{K} \bar{A} \bar{a}_1 = \bar{K} \bar{s}_1$$

For right boundary,

$$\bar{J}^r = \bar{\alpha}^r \bar{f}_a^r \bar{\phi}^r$$

Where,  $\bar{\alpha}^r, \bar{f}_a^r$  are diagonal matrices for albedo and discontinuity factors respectively.

$$\bar{\gamma}^r = \bar{\alpha}^r \bar{f}_a^r$$

$$\bar{J}^r = -\frac{D}{h} \sum_{i=1}^4 \bar{a}_i P_i'(1) = -\bar{\gamma}^r (\bar{a}_1 + 3\bar{a}_2 + 6\bar{a}_3 + 10\bar{a}_4)$$



$$\begin{aligned}
\bar{\phi}^r &= \sum_{i=0}^4 \bar{a}_i P_i(1) = \sum_{i=0}^4 \bar{a}_i = \bar{a}_0 + \bar{a}_1 + \bar{a}_2 + \bar{a}_3 + \bar{a}_4 \\
-\beta (\bar{a}_1 + 3\bar{a}_2 + 6\bar{a}_3 + 10\bar{a}_4) &= \alpha \beta_a^r (\bar{a}_0 + \bar{a}_1 + \bar{a}_2 + \bar{a}_3 + \bar{a}_4) \\
\bar{a}_3 &= -C_0 \bar{a}_0 - C_1 \bar{a}_1 - C_2 \bar{a}_2 - C_4 \bar{a}_4 \\
C_0 &= \frac{\gamma^r}{6\beta + \gamma^r}, C_1 = \frac{\beta + \gamma^r}{6\beta + \gamma^r}, C_2 = \frac{3\beta + \gamma^r}{6\beta + \gamma^r}, C_4 = \frac{10\beta + \gamma^r}{6\beta + \gamma^r} \\
\bar{a}_1 &= -\left(15C_1 + \bar{A}\right)^{-1} \left[15(C_0 \bar{a}_0 + C_2 \bar{a}_2 + C_4 \bar{a}_4) - \bar{s}_1\right]
\end{aligned}$$

where  $C_0, C_1, C_2$  and  $C_4$  are diagonal matrices

All the coefficients are then known to calculate the current. The current is then used to update the diffusion coefficient. All of this was coded into a separate option for the one-node NEM solver in PARCS.



# APPENDIX E RESULTS OF THE TEST CASES USED TO VERIFY THE CODING IMPLEMENTED IN PARCS FOR THE BOUNDARY CONDITIONS

	k-eff											
	1-D				2-D				3-D			
	NEM		FDM		NEM		FDM		NEM		FDM	
Boundary Cond.	Albedo	PARCS BC	Albedo	PARCS BC	Albedo	PARCS BC	Albedo	PARCS BC	Albedo	PARCS BC	Albedo	PARCS BC
Reflective	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065	1.121065
Zero Incoming J	0.304938	0.304938	0.386610	0.386610	0.186000	0.186026	0.204721	0.204721	0.091930	0.091946	0.130416	0.130416
Zero Flux	0.359818	0.359818	0.304938	0.304938	0.149503	0.149509	0.165962	0.165962	0.117134	0.117188	0.103049	0.103049

	Two by Two Case							
	Albedo		Extrapolation Distance					
K-eff	0.044034		0.044034		Two by Two Case Boundary Conditions			
Group 1	6.622E+16	6.622E+16	6.622E+16	6.622E+16	Albedo		Extrapolation Distance	
Flux	6.622E+16	6.622E+16	6.622E+16	6.622E+16			Distance	Radius
Group 2	1.991E+16	1.991E+16	1.991E+16	1.991E+16	Group 1	0.681223	3.0	10.0
Flux	1.991E+16	1.991E+16	1.991E+16	1.991E+16	Group 2	0.4418445	3.0	10.0

Five by Five Case Calculated From Input											
x albedos G1	1	2	3	4	5	x albedos G2	1	2	3	4	5
1	1.090996	-	-	-	1.090996	1	0.707585	-	-	-	0.707585
2	0.211285	-	-	-	0.211285	2	0.137033	-	-	-	0.137033
3	0.170306	-	-	-	0.170306	3	0.110455	-	-	-	0.110455
4	0.211285	-	-	-	0.211285	4	0.137033	-	-	-	0.137033
5	1.090996	-	-	-	1.090996	5	0.707585	-	-	-	0.707585
y albedos G1	1	2	3	4	5	y albedos G2	1	2	3	4	5
1	1.090996	0.211285	0.170306	0.211285	1.090996	1	0.707585	0.137033	0.110455	0.137033	0.707585
2	-	-	-	-	-	2	-	-	-	-	-
3	-	-	-	-	-	3	-	-	-	-	-
4	-	-	-	-	-	4	-	-	-	-	-
5	1.090996	0.211285	0.170306	0.211285	1.090996	5	0.707585	0.137033	0.110455	0.137033	0.707585

Five by Five Case From PARCS Debug Run											
x albedos G1	1	2	3	4	5	x albedos G2	1	2	3	4	5
1	1.090996	-	-	-	1.090996	1	0.707585	-	-	-	0.707585
2	0.211285	-	-	-	0.211285	2	0.137033	-	-	-	0.137033
3	0.170306	-	-	-	0.170306	3	0.110455	-	-	-	0.110455
4	0.211285	-	-	-	0.211285	4	0.137033	-	-	-	0.137033
5	1.090996	-	-	-	1.090996	5	0.707585	-	-	-	0.707585
y albedos G1	1	2	3	4	5	y albedos G2	1	2	3	4	5
1	1.090996	0.211285	0.170306	0.211285	1.090996	1	0.707585	0.137033	0.110455	0.137033	0.707585
2	-	-	-	-	-	2	-	-	-	-	-
3	-	-	-	-	-	3	-	-	-	-	-
4	-	-	-	-	-	4	-	-	-	-	-
5	1.090996	0.211285	0.170306	0.211285	1.090996	5	0.707585	0.137033	0.110455	0.137033	0.707585



NRC FORM 335 (12-2010) NRCMD 3.7		U.S. NUCLEAR REGULATORY COMMISSION		1. REPORT NUMBER (Assigned by NRC, Add Vol., Supp., Rev., and Addendum Numbers, if any.)	
BIBLIOGRAPHIC DATA SHEET <i>(See instructions on the reverse)</i>				NUREG/IA-0453	
2. TITLE AND SUBTITLE Benchmarking of a Generic CANDU Reactor with PARCS, MCNP and RFSP				3. DATE REPORT PUBLISHED	
				MONTH September	YEAR 2015
				4. FIN OR GRANT NUMBER	
5. AUTHOR(S) B. Arsenault, O. Shaikh , *T. Downar, *D. Jabaay, *A. Ward, *Y. Xu				6. TYPE OF REPORT  Technical	
				7. PERIOD COVERED (Inclusive Dates)	
8. PERFORMING ORGANIZATION - NAME AND ADDRESS (If NRC, provide Division, Office or Region, U. S. Nuclear Regulatory Commission, and mailing address; if contractor, provide name and mailing address.) AMEC-NSS                                      * Univ. of Michigan 4F, 700 University Ave.                      Nuclear Eng and Rad. Science Toronto, Ontario                                1934 Cooley M5G 1X6, Canada                                Ann Arbor, MI 48109-2104, USA					
9. SPONSORING ORGANIZATION - NAME AND ADDRESS (If NRC, type "Same as above", if contractor, provide NRC Division, Office or Region, U. S. Nuclear Regulatory Commission, and mailing address.) Division of Systems Analysis Office of Nuclear Regulatory Research U.S. Nuclear Regulatory Commission Washington, DC 20555-0001					
10. SUPPLEMENTARY NOTES K. Tien NRC Project Manager					
11. ABSTRACT (200 words or less) The purpose of this project is to benchmark a generic CANDU reactor with the computer codes PARCS, MCNP and RFSP. RFSP is a diffusion code used by the Canadian nuclear industry for fuel management and for safety analyses. A number of changes were made to PARCS and GenPMAXS, the utility used to generate the fuel tables for PARCS. The changes were required to allow the modeling of specific aspects related to CANDU reactors. More specifically, the benchmarking exercise involves an assessment of the Finite Difference Method and the hybrid NEM/ANM solvers available in PARCS against the results of Monte Carlo simulations performed with MCNP. The results of the simulations calculated with the Finite Difference Methods in PARCS and RFSP are compared to determine possible areas of improvement in RFSP.					
12. KEY WORDS/DESCRIPTORS (List words or phrases that will assist researchers in locating the report.) CANDU Reactor PARCS MCNP RFSP GenPMAXS Monte Carlo simulation				13 AVAILABILITY STATEMENT unlimited	
				14. SECURITY CLASSIFICATION (This Page) unclassified	
				(This Report) unclassified	
				15. NUMBER OF PAGES 78	
				16. PRICE	



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**Benchmarking of a Generic CANDU Reactor with PARCS, MCNP and RFSP**

**September 2015**