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*Estimates of Mean Consequences and Confidence  
Bounds on the Mean Associated With  
Low-Probability Seismic Events in Total System  
Performance Assessments*

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# Outline

- Introduction
- Objectives
- Assumptions
- Mathematical Approach
- Results
- Conclusions

## *Introduction*

- U.S. regulations for high-level radioactive waste disposal require that a mean dose to members of the public does not exceed a prescribed value
- A possible mechanism for early breaching of engineered barrier system components is drift degradation and seismic events of high magnitude (i.e., low recurrence rate)

## *Introduction (Continued)*

- Consequence estimates can be obtained using a performance assessment (PA) model
  - A large number of variables affecting the potential repository performance are considered
  - Propagation of input uncertainty is accomplished using Monte Carlo sampling
  - Only few hundreds to few thousands of Monte Carlo realizations are typically performed
- Special methodologies are needed to derive confidence bounds on mean consequences of low probability events

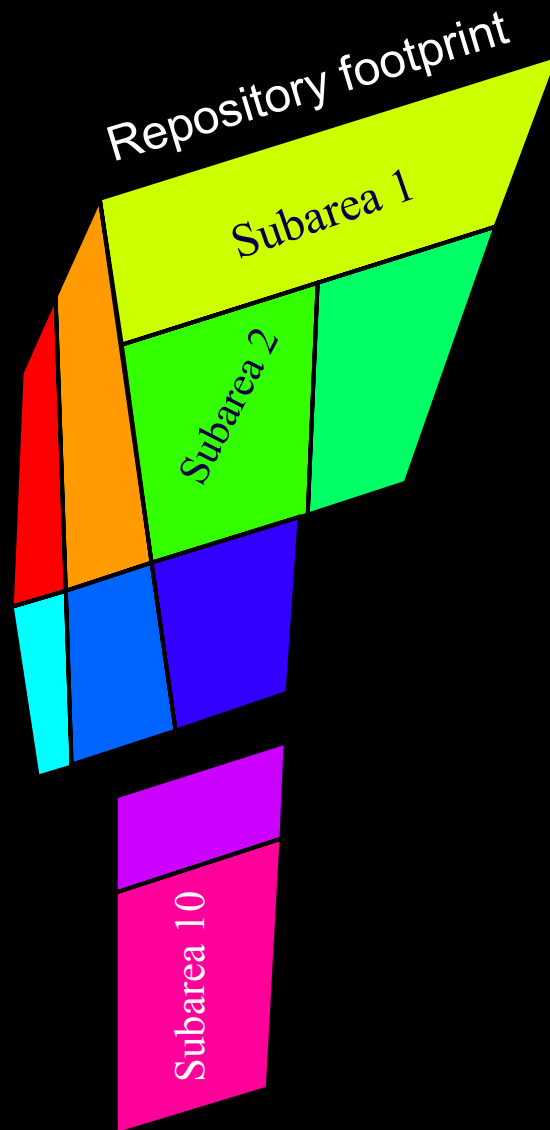
## Objectives

- Present an approach to estimate consequences of low recurrence rate seismic events with a limited number of Monte Carlo realizations for a particular type of PA model
  - PA model of interest: consequences per waste package (WP) are independent of the process causing waste package failure (e.g., the consequence per waste package is the same for high and low intensity seismic events)
- Develop formulas for confidence bounds on mean consequences

## Assumptions

- Only events of recurrence rates,  $\lambda$ , less than a threshold (e.g.,  $\lambda < 10^{-4} \text{ yr}^{-1}$ ) damage the waste package
  - Facilities/structures are assumed to have been designed and built to withstand events of  $\lambda \geq 10^{-4} \text{ yr}^{-1}$
- The probability for an event,  $p_e$ , to cause waste package failure is time independent
- A waste package can be in two states: breached or not

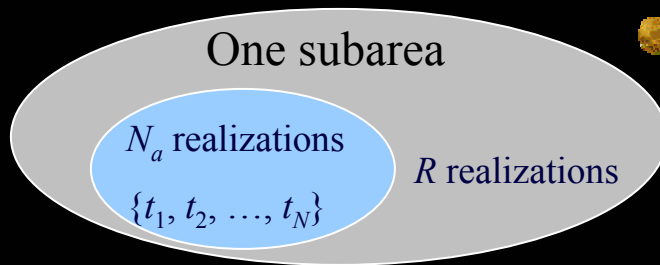
## Assumptions (Continued)



One representative waste package is used to simulate a set

- All waste packages in a subarea are assumed simultaneously breached
- Conditions controlling radionuclide releases (temperature, water flow rates, in-package chemistry) are assumed identical for all waste packages in a subarea

## Problem Description



Probability for a realization to include a waste package breaching event:

$$p = 1 - e^{-p_e \lambda T} \approx \frac{N_a}{R}$$

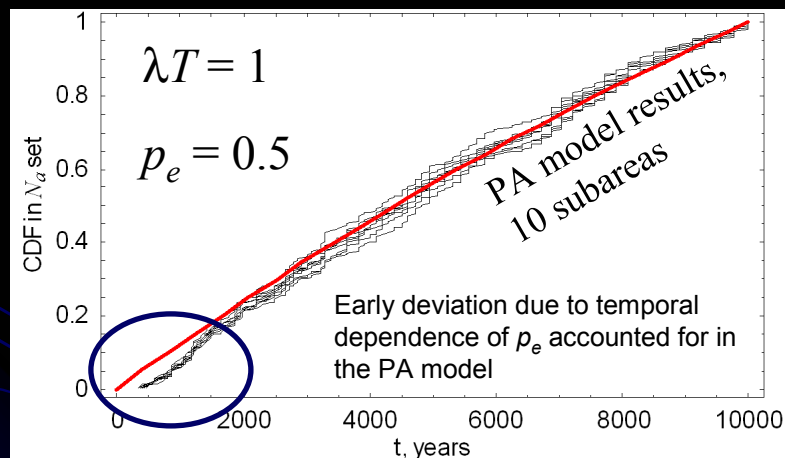
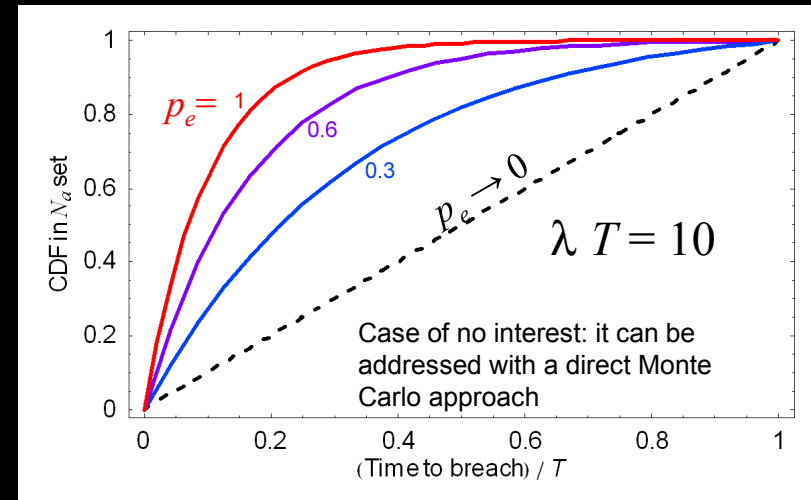
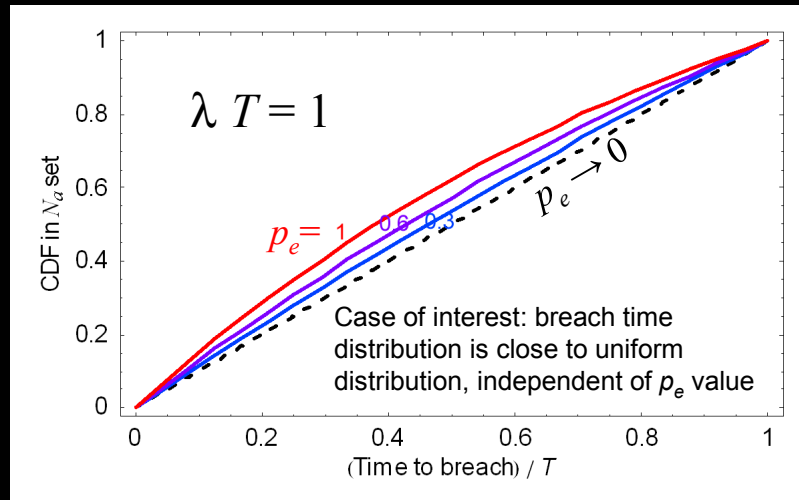
$T$ : simulation time

$\lambda$ : recurrence rate

- In most realizations, there is no waste package breaching (because  $\lambda$  and  $p_e$  are small for the case of interest)
- $\{t_1, t_2, \dots, t_N\}$  is the collection of breach times in the set  $N_a$  (one subarea)
  - Breach times follow a truncated exponential distribution with recurrence rate equal to  $p_e \lambda$
- If product  $p_e \lambda$  is small, there are not enough realizations (set  $N_a$  is too small) to compute converging statistics on consequences



# Breach Time Distribution

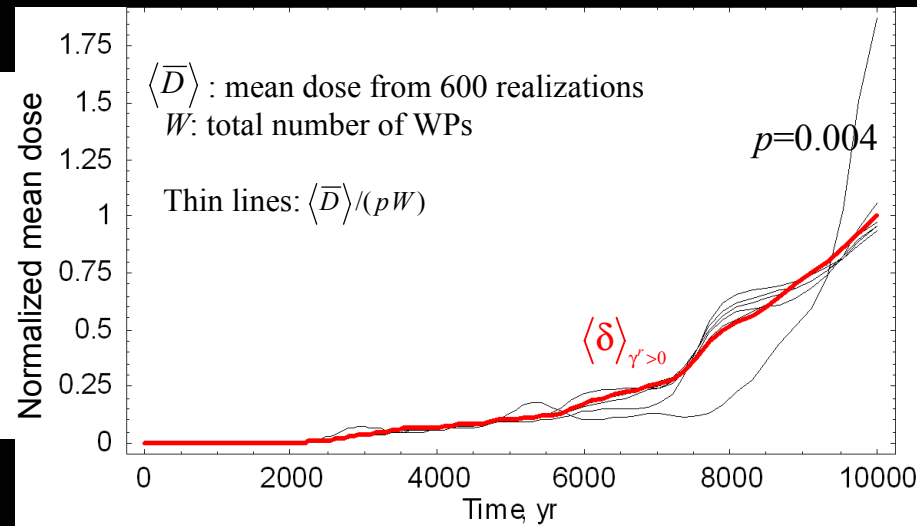


In the  $N_a$  set (one subarea) for the case of interest ( $\lambda T \leq 1$ ), the cumulative distribution of breach times is quasi-independent of the value of  $p_e$

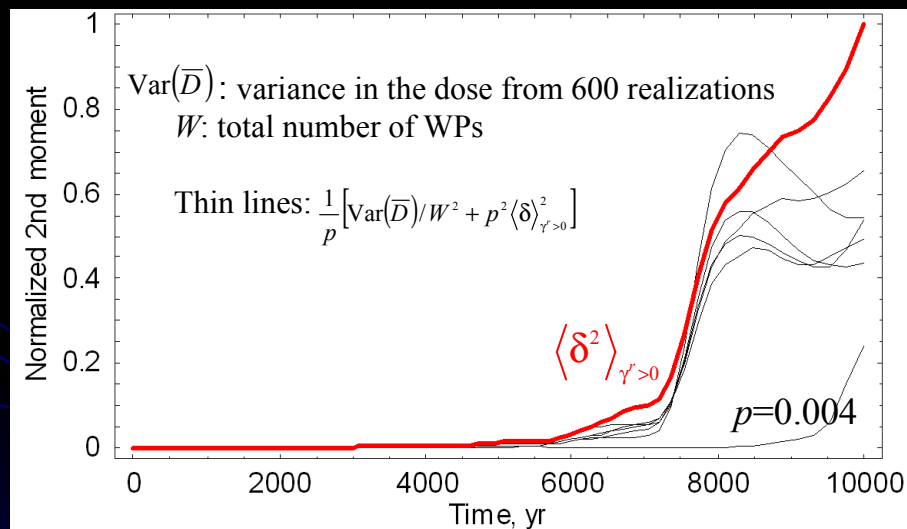
## Mathematical Approach

- Run the PA model with a high value of  $p_e$  (or  $p$ )
- Derive statistics in the  $N_a$  subset (one subarea only)
  - Moments of the dose per waste package:  $\langle \delta^m \rangle_{\gamma' > 0}$ ,  $m=1, 2, 3, \dots$
  - Statistics are independent of the value of  $p$
- Derive statistics for the complete  $R$  set (case of interest: low value of  $p$ ) from the  $N_a$  subset statistics
  - Total mean dose (aggregated from all subareas)
  - Analytical upper bound in the standard deviation
    - Derived by assuming perfectly correlated subareas
    - Used to assist in the understanding of the significance of the seismic scenario

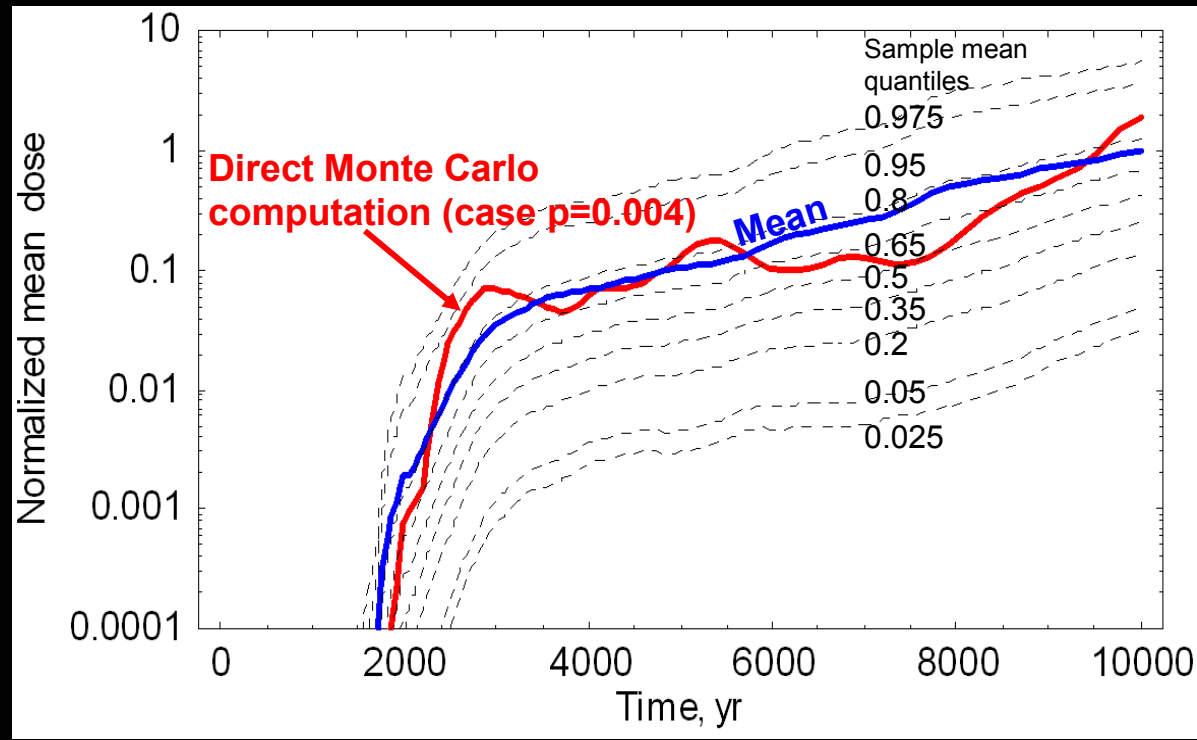
## Results



- Similar results of the mean dose per waste package in the  $N_a$  set were derived independently of the value of  $p$
- The reference **red line** was computed with the case  $p=0.4$



## Results



Confidence interval computed by assuming that, for every time step, the mean and standard deviation in the sample mean are computed as (case  $p=0.004$ )

$$\langle \bar{D} \rangle = p \langle \delta \rangle_{\gamma' > 0} \sum_{a=1}^A w_a = p \langle \delta \rangle_{\gamma' > 0} W$$

$$\text{SDev}(\langle \bar{D} \rangle) \leq \frac{W}{\sqrt{R}} \sqrt{p \langle \delta^2 \rangle_{\gamma' > 0} - p^2 \langle \delta \rangle_{\gamma' > 0}^2}$$

$w_a$ : WPs in a subarea

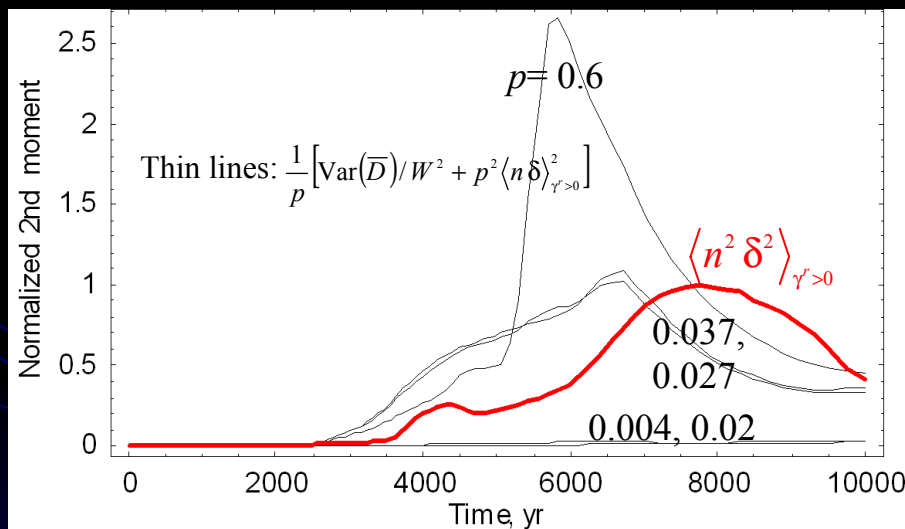
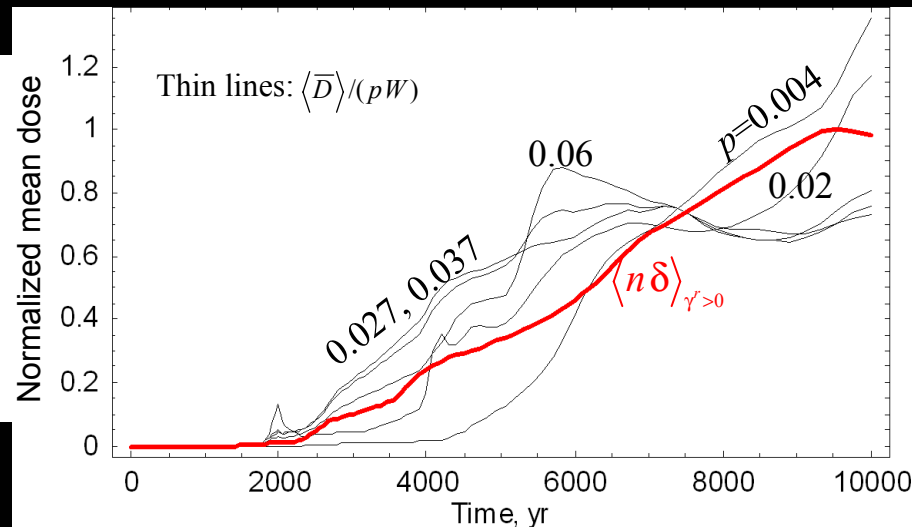
$W$ : Total WPs in repository

$\langle \delta^n \rangle_{\gamma' > 0}$  :  $n$  moment (dose per WP) in set  $N_a$   
(moment computed with case  $p=0.4$ )

## A More General Case

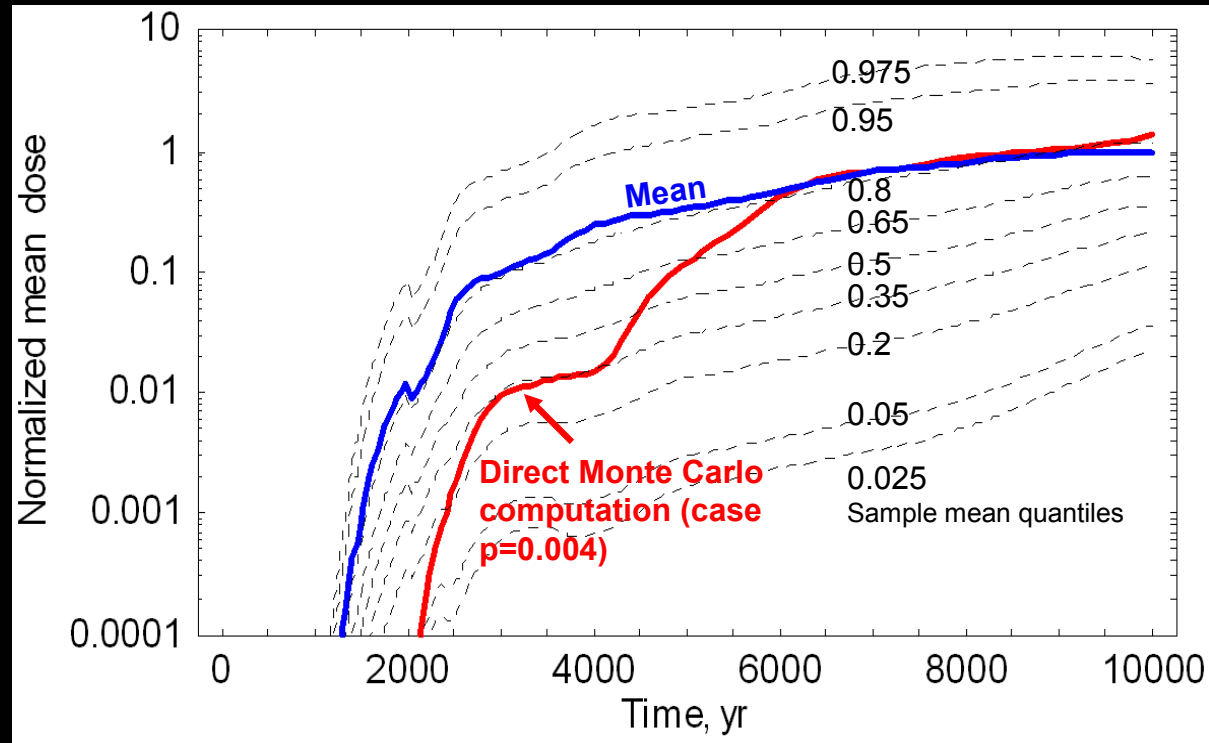
- The previous derivation assumed that all of the waste packages in a subarea were breached once an event of sufficient magnitude occurred
- If only a fraction,  $n$ , of the waste packages in a subarea is breached then the formulas are modified as
  - Sample mean:  $\langle \bar{D} \rangle = pW \langle n\delta \rangle_{\gamma^r > 0}$
  - Sample variance:  $\text{Var}(\bar{D}) = \langle \bar{D}^2 \rangle - \langle \bar{D} \rangle^2 \leq W^2 \left( p \langle n^2 \delta^2 \rangle_{\gamma^r > 0} - p^2 \langle n\delta \rangle_{\gamma^r > 0}^2 \right)$
  - SDev in the sample mean:  $\text{SDev}(\langle \bar{D} \rangle) \leq \frac{W}{\sqrt{R}} \sqrt{p \langle n^2 \delta^2 \rangle_{\gamma^r > 0} - p^2 \langle n\delta \rangle_{\gamma^r > 0}^2}$
  - The distribution for the fraction,  $n$ , is assumed independent of the subarea, but could be a function of other factors (e.g., event intensity)

## Results



- The fraction,  $n$ , randomly sampled in this example, is a source of extra variance in the mean dose
- The reference **red line** was computed with a stylized 500-realization run
  - Breach times uniformly distributed
  - One breaching event in each realization (i.e.,  $N_a=R$ )

## Results



Confidence interval computed by assuming that, for every time step, the mean and standard deviation in the sample mean are computed as (case  $p=0.004$ )

$$\langle \bar{D} \rangle = pW \langle n\delta \rangle_{\gamma^r > 0}$$

$$\text{SDev}(\langle \bar{D} \rangle) \leq \frac{W}{\sqrt{R}} \sqrt{p \langle n^2 \delta^2 \rangle_{\gamma^r > 0} - p^2 \langle n\delta \rangle_{\gamma^r > 0}^2}$$

## Conclusions

- An approach was developed to estimate mean consequences of seismic events in a performance assessment model
- The approach was extended to account for the case where only a fraction (defined by a distribution function) of the waste packages in a subarea may be breached
- Mean consequences can be derived with stylized runs
  - Breach times uniformly distributed
  - One waste package breaching event in each realization
- Derived equations can be used to estimate mean consequences without the need for a large number of PA model realizations



## *Disclaimer*

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