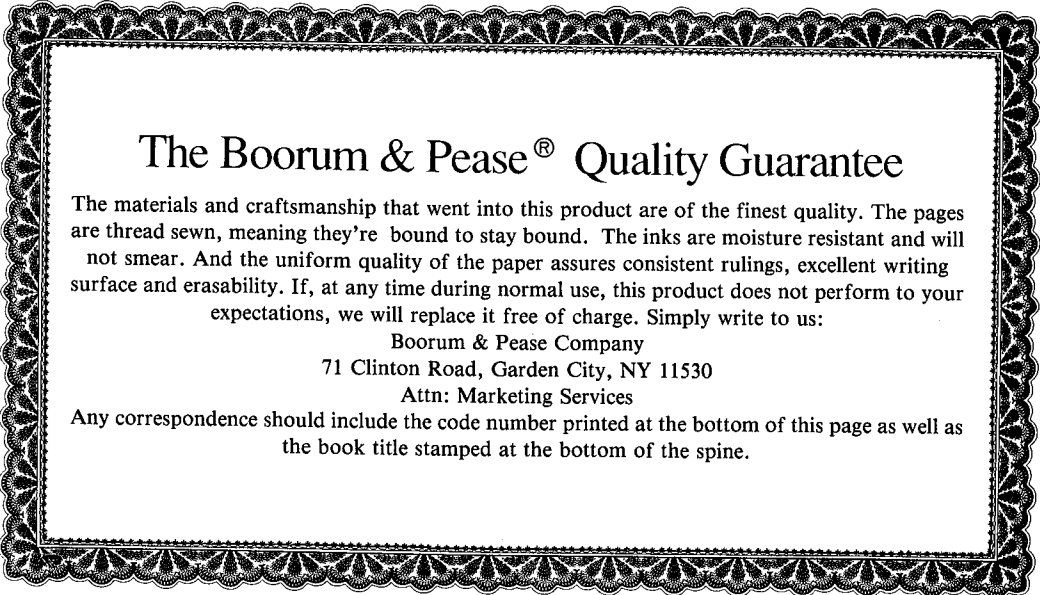


21
150

R

Issued To: Gordon Wittmeyer
CNWRA
210-522-5082 Jan 12/28/95



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COPY 126

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Contents

Page

Record of selected technical work conducted
by Gordon Wittmeyer on the Regional
Hydrogeology Research project (20-5704-150).

Subject: SCIENTIFIC NOTEBOOK No. 126 / 127

Date: Fri, 25 Aug 2000 12:24:42 -0500

From: Bruce Mabrito <bmabrito@gargol.cnwra.swri.edu>

Organization: CNWRA

To: Maria Padilla <mypadilla@gargol.cnwra.swri.edu>,
 "Bruce Mabrito (bmabrito)" <bmabrito@gargol.cnwra.swri.edu>,
 "English Percy (epercy)" <epercy@gargol.cnwra.swri.edu>,
 "David Pickett (dpickett)" <dpickett@gargol.cnwra.swri.edu>,
 "James Prikryl (jprikryl)" <jprikryl@gargol.cnwra.swri.edu>

The purpose of this e-mail message is to document the location of scientific notebook number 127.

First, scientific notebook 126 was issued to Gordon Wittmeyer on 12/8/1994. That notebook was utilized and then returned to QA Records 2/22/1996.

During the August 2000 call for scientific notebooks, another scientific notebook, also numbered 126, was returned. It has been determined that QA "double issued" the number 126. Apparently, I issued No. 126 to Gordon Wittmeyer in 1994 and Alice Cortinas (Records Custodian) issued a second scientific notebook with the same number 126 on 12/21/1994 to Jim Prikryl. In the call for notebooks, we discovered this fact. We had assumed that scientific notebook No. 127 was lost and a memorandum was issued from Dr. English Percy on June 15, 2000 so stating. It is very clear that this notebook should have been identified number 127 because all other identifying information (issuer, receiver of notebook, dates, and project numbers) otherwise match well.

The following actions are being taken. A B. Mabrito signed copy of this e-mail message will be attached to the E. Percy memo of 6/15/2000 and also to the scientific notebook issued to Jim Prikryl. Second, the number 126 on the front of Jim Prikryl's notebook (which is now being used by Dr. David Pickett) will be changed to number 127 and initialed and dated by B. Mabrito. The Scientific Log Notebook will be corrected to reflect that scientific notebook No. 127 was not lost and is now in use by Dr. David Pickett.

Bruce Mabrito 8/25/2000
 Bruce Mabrito

December 8, 1994.

Goal: Produce a kriged map of mean annual precipitation for the Death Valley region.

Procedure: Ordinary kriging with an extended or exterior variable drift model. Drift model is first order, and based on elevation.

Elevation \rightarrow precip model; drift model

$$1000 \ln(AAP) = a + b(\text{elevation})$$

AAP = average annual precip

Elevation data comes from USGS 1 degree DEM

1. Each $1^\circ \times 1^\circ$ area is divided into a 1201×1201 grid of elevations (in meters) spaced 3 arc-sec apart.

2. Read each DEM file into EarthVision (EV).

3. Convert each to a 1201×1201 EV 2D grid.

4. Reduce grid density

5. Create union of $1^\circ \times 1^\circ$ reduced grids

6. Export union grid to ASCII file

7. Convert ASCII geographic coords to UTM

10X10 DEM'S (1usr4/gwith/Ischyaetal)*.2grds

- caliente west: caliente-w: cal-w.2grd
- goldfield east: goldfield-e: gold-e.2grd
- goldfield west: goldfield-w: gold-w.2grd
- lasvegas west: lasvegas-w: lv-w.2grd
- deathvalley east: death-valley-e: dv-e.2grd
- deathvalley west: death-valley-w: dv-w.2grd

use EV's "utilities" (on performer)

└ Import DEM

└ convert to
*.2grd

Next step is to reduce the grid density of each of the above from 1201x1201 to 101x101 using the "formula processor" utility under "utilities" (function "refgrd")

cal-w-small.2grd = refgrd(cal-w.2grd, 101, 101, -417600, -414000, 133200, 136800)

gold-e-small.2grd = refgrd(gold-e.2grd, 101, 101, -421200, -417600, 133200, 136800)

gold-w-small.2grd = refgrd(gold-w.2grd, 101, 101, -424800, -421200, 133200, 136800)

lv-w-small.2grd = refgrd(lv-w.2grd, 101, 101, -417600, -414000, 129600, 133200)

dv-e-small.2grd = refgrd(dv-e.2grd, 101, 101, -421200, -417600, 129600, 133200)

dv-w-small.2grd = refgrd(dv-w.2grd, 101, 101, -424800, -421200, 129600, 133200)

Next step is to combine the six *.small.2grd grids into one grid using the formula processor. We use the function "union"

small1.2grd = union(cal-w-small.2grd, gold-e-small.2grd)

small2.2grd = union(small1.2grd, gold-w-small.2grd)

small3.2grd = union(lv-e-small.2grd, dv-e-small.2grd)

small4.2grd = union(small3.2grd, dv-w-small.2grd)

small.2grd = union(small2.2grd, small4.2grd)

└ this is the coarse elevation grid file for
-115° to -118° W & 36° N to 38° N

Next step is to convert small.2grd to an ASCII X,Y,Z file using the "ev-export" utility

% ev-export -o small.dat small.2grd

small.dat is ~ 2.8 Mb on 1usr4/gwith/Ischyaetal

Next we need to convert small.dat so that its X,Y coordinates are in UTM rather than Latitude - Longitude. (small.dat is 301 X 201)

1. Copy small.dat to ~~small-z.dat~~ ^{small-map} ~~small-map~~

Format of small.map is

X (Arc Sec) , Y (Arc Sec) , Z (elev. meters),
column , row

2. Because small.map is in arc-sec, a small program was developed to convert the Lat-Lon to decimal degrees. This file is called

"small.out" → X (dec. deg.), Y (dec. deg.),
Z (elevation in m)

3. Evenden's Cartographic projection procedure for UTM machines was to convert the X,Y coordinates in "small.out" to UTM. The resulting file is "small.utm"

X (meters (utm)), Y (meters (utm)), Z (elev, m)

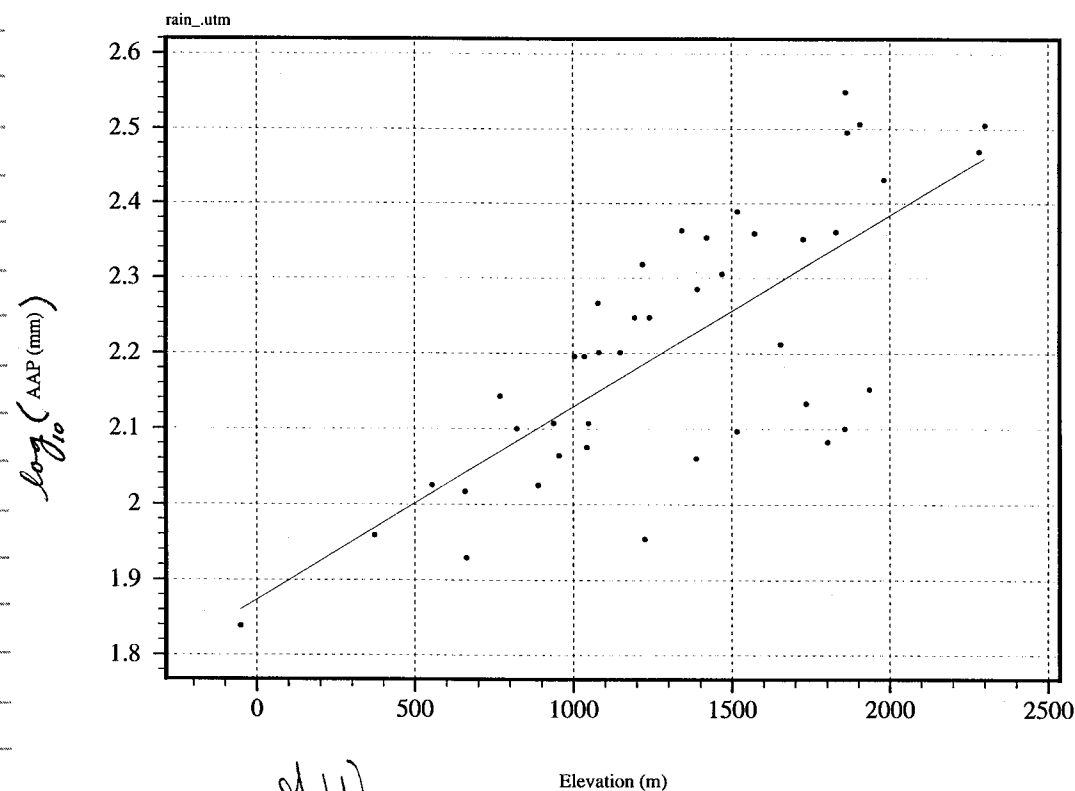
Script used is shown below ^{GW} 12/8/94

Jordan Wiltschko

12/12/94

Precipitation data for the Death Valley region were obtained from Hanesi et al. (1992) and entered into the computer. The coordinates of the precip stations in Hanesi et al. were given in Nevada state plane coordinates. However, the coordinates for these same stations were given in French (1983) in Longitude - Latitude. These Long-Lat were then converted to UTM coordinates using Evenden's cartographic projection program.

The logarithm of ^{GW} ~~Ann~~ ^{Annual} Average Annual Precipitation was regressed on elevation in meters to obtain an external drift model.



GW

The drift model is:

$$\ln(AAP) = 4.3146 + .0005872 E$$

AAP: Average Annual Precip (mm)

E: Elevation above MSL in meters.

ln: log base e.

Jordan Wilhite

12/13/94

Nauprogram for $\ln(AAP)$ and for
 $\ln(AAP) - (4.3146 + .0005872 E)$ (the
 residual AAP are shown attached.

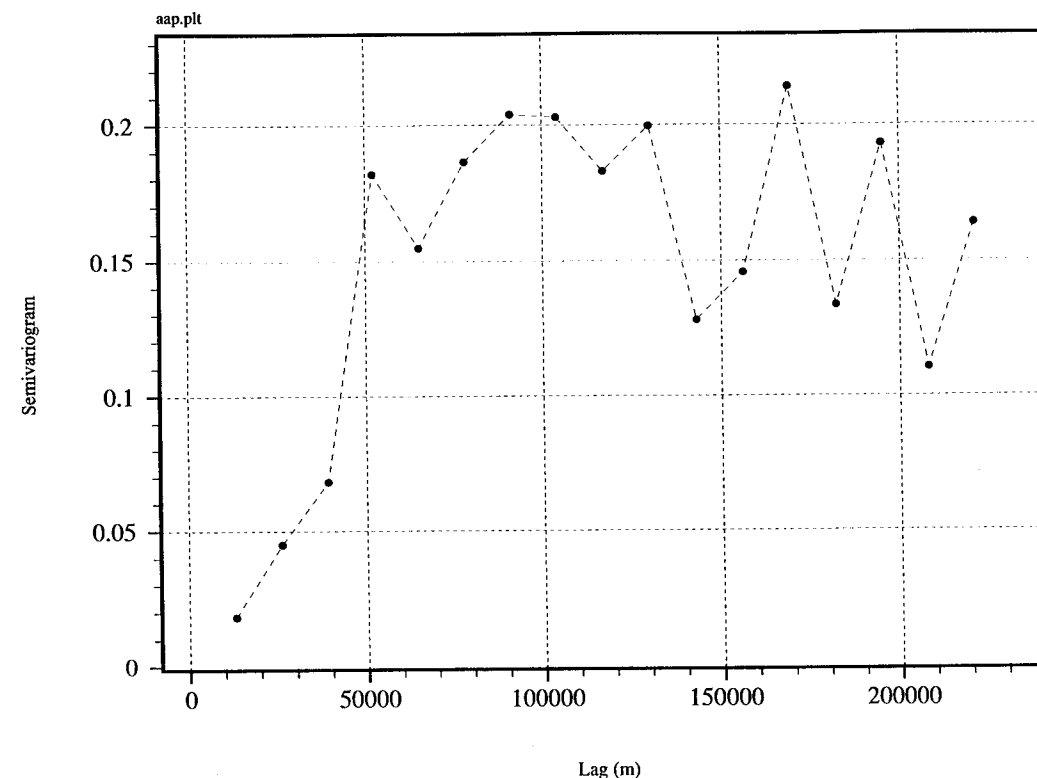
① γ for $\ln(AAP)$ appears to be stationary which is confusing since AAP is presumed to be a function of elevation and the nauprogram of elevation developed by Hensel et al. (1992) showed a definite lack of stationarity.

② γ for residual $\ln(AAP)$. Omni-directional γ is apparently non-stationary.

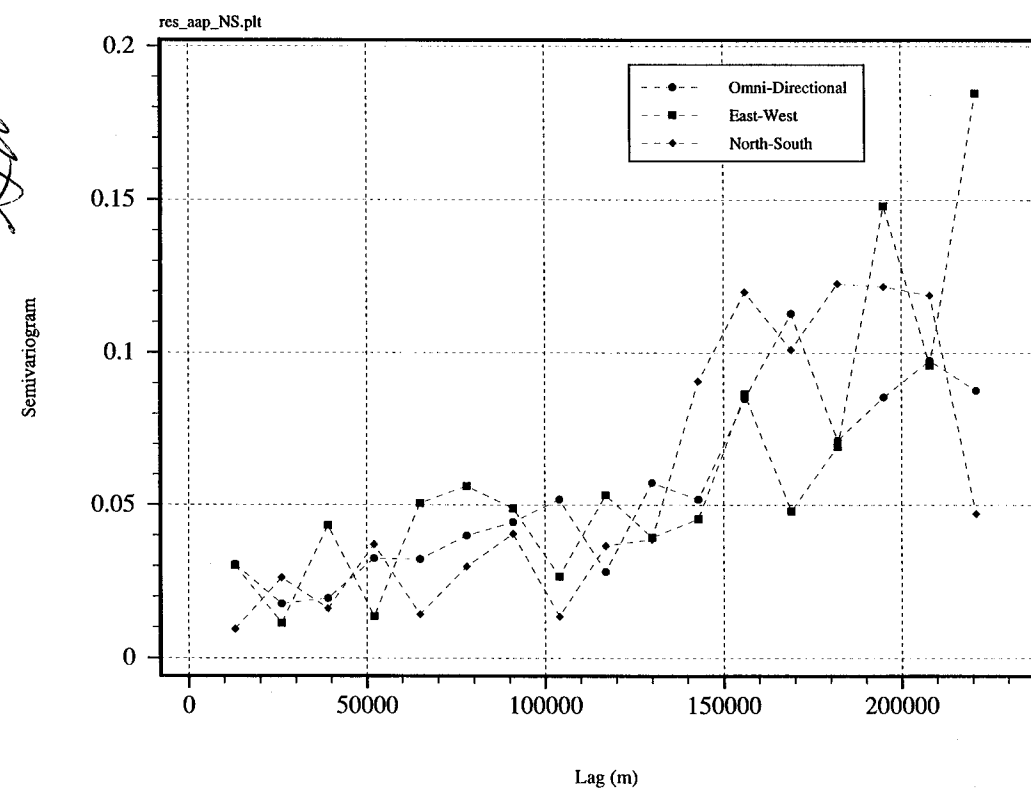
③ Other directional γ 's for residual $\ln(AAP)$

④ Directional γ 's for residual $\ln(AAP)$.
 NE-SW & NW-SE direction appear to be principal directions. However, $\gamma(NE-SW)$ is clearly not stationary... or if it is, its correlation length is very large (~200,000 m).

Sample Semivariogram for $\ln(AAP)$

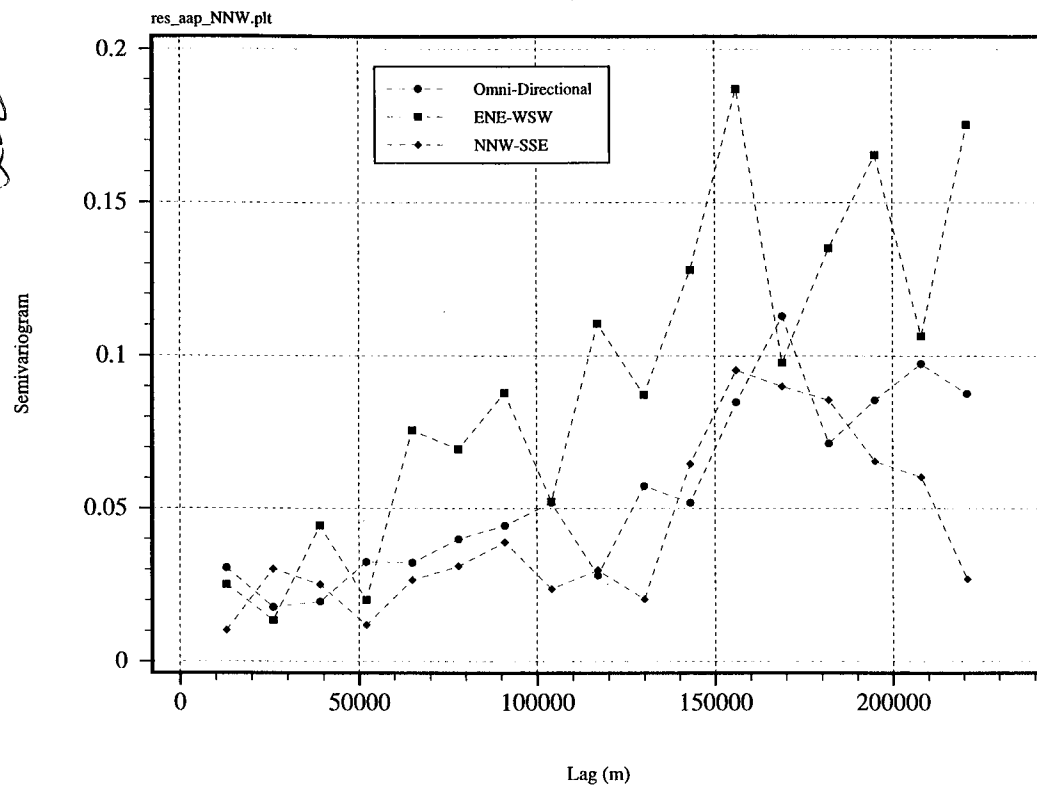


Sample Semivariogram for Residual $\ln(AAP)$

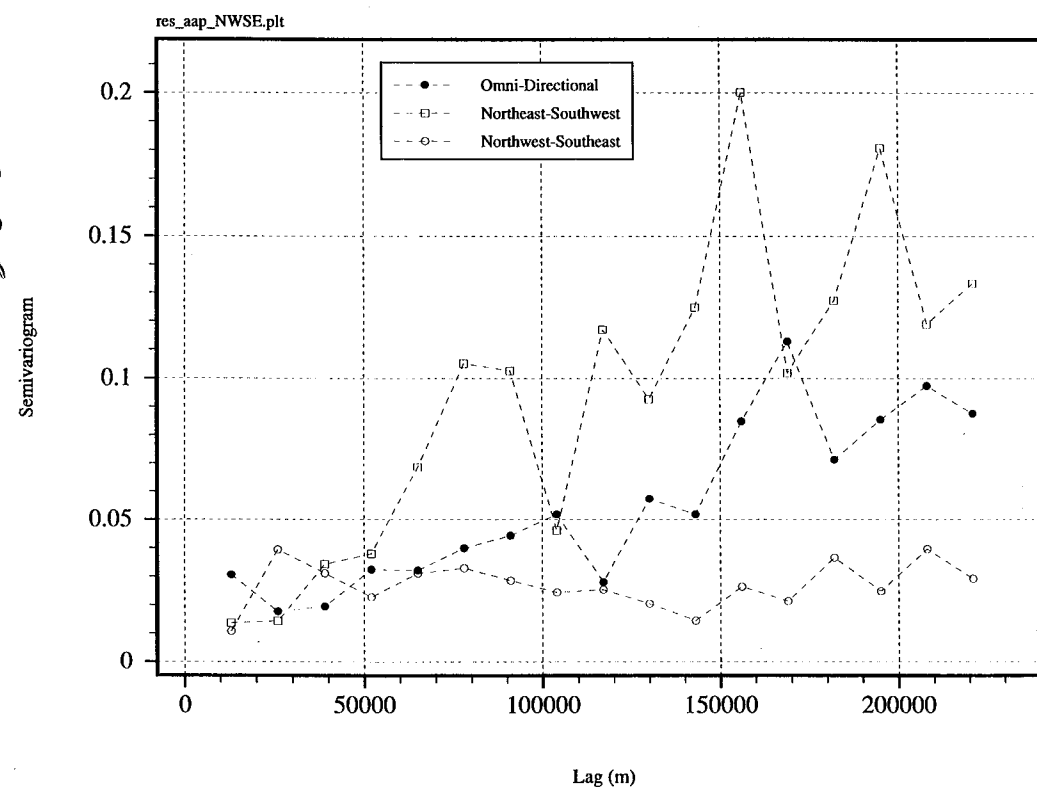


Sample Semivariogram for Residual $\ln(\text{AAP})$

(3)

Sample Semivariogram for Residual $\ln(\text{AAP})$

(4)



The behavior of γ for residual $\ln(\text{AAP})$ is very confusing at first glance. The semivariogram is definitely not stationary whereas γ for the raw variable ($\ln(\text{AAP})$) is stationary. This is exactly opposite what one normally expects; one usually subtracts the trend from the raw variable in order to construct a residual variable that is stationary.

Grid of estimated AAP based on elevation
 \Rightarrow rain_map.zgrid.

Grid of residual precip.

rain_diff.zgrid.

Gordon Wilhemyer

December 20, 1994

It is readily apparent from plot 4 on page 8 that the residual variogram is not stationary. Recall that the residual is given by

$$Res = AAP - \exp(4.3146 + .0005872 E)$$

where AAP is the measured average annual precipitation at the 42 stations, and E is the elevation in meters. This residual reflects AAP minus the orographic effect. However, the lack of stationarity of the RES is probably due to yet another effect, namely the rainshadow effect of the Sierra Nevada.

I developed a simple program to fit a polynomial trend surface to the RES.

The first order trend surface is given by

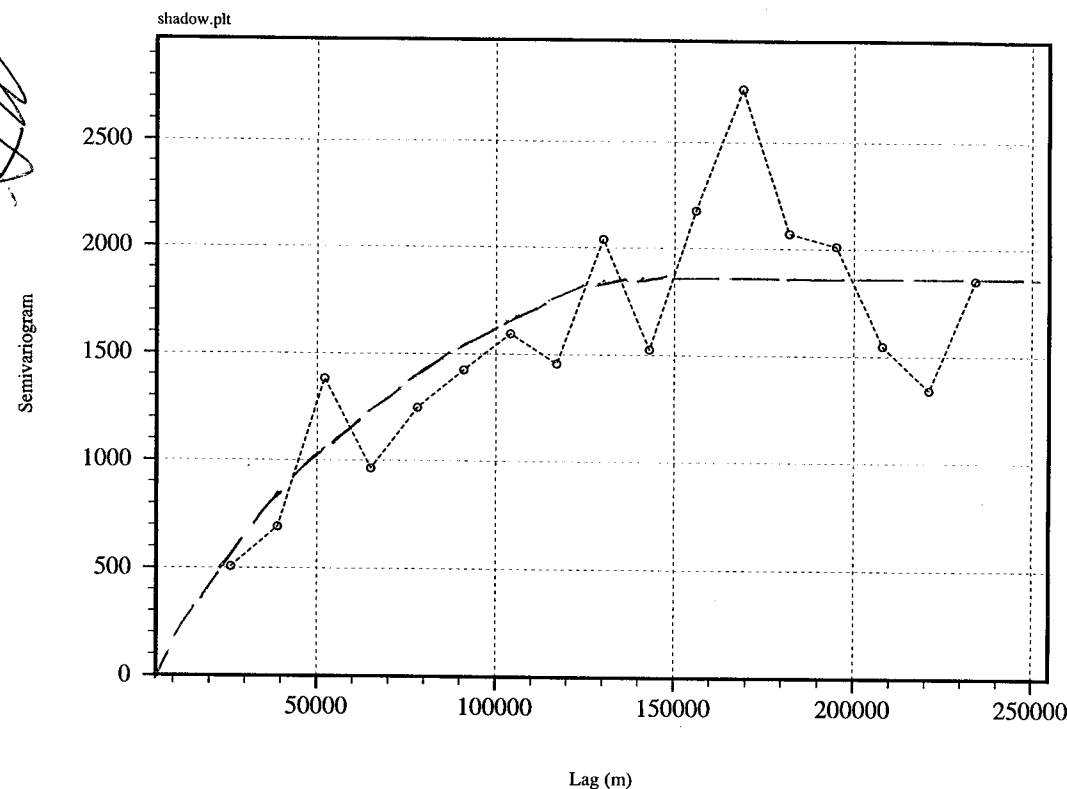
$$\hat{RES}(mm) = 67.36 + 3.34 \times 10^{-4} X - 6.26 \times 10^{-5} Y$$

where X and Y are the UTM coordinates in meters. The new rainshadow residual is given by

$$SHAORES = RES - 67.36 - 3.34 \times 10^{-4} X + 6.26 \times 10^{-5} Y$$

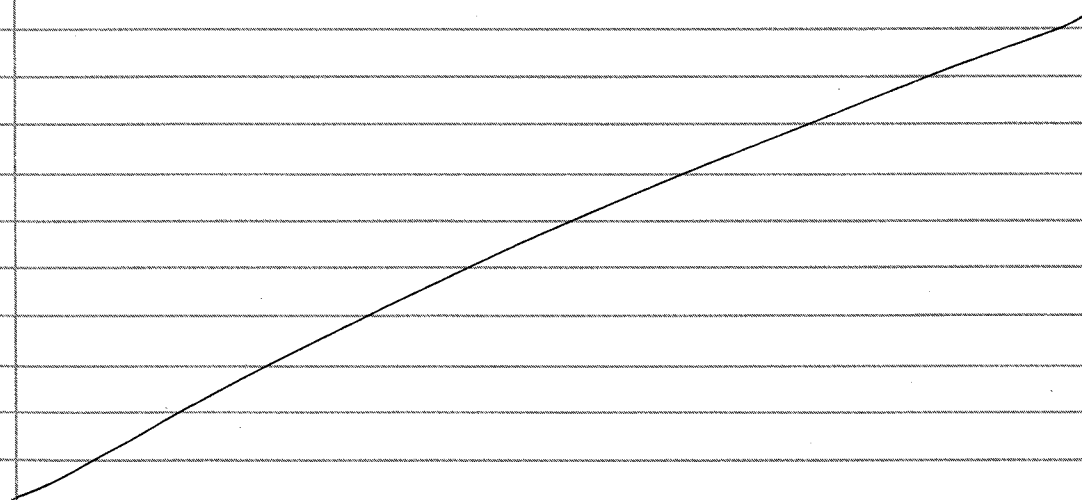
The semivariogram for SHAORES is given in plot 1 following. SHAORES with a 1st degree trend surface appear to be stationary and may be represented a spherical semi-variogram

Semivariogram for AAP Residuals without Rain Shadow Effect

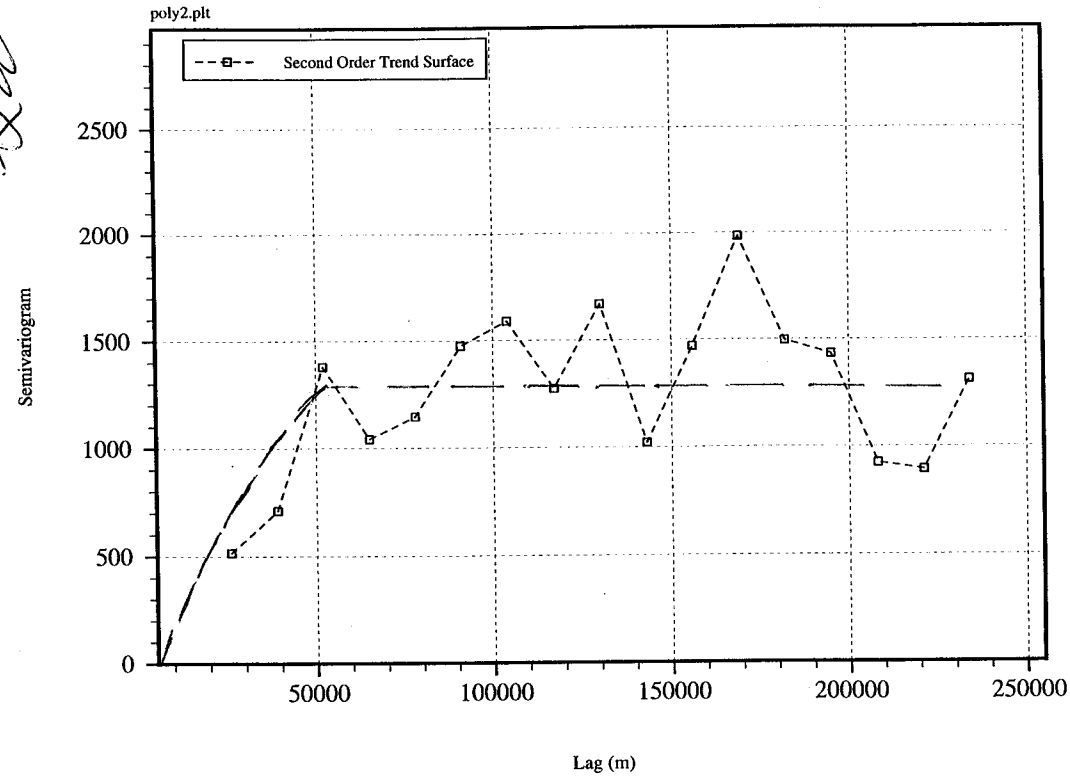


$$\gamma(h) = \begin{cases} \sigma^2 \left(1.5 \frac{h}{a} - .5 \left(\frac{h}{a} \right)^3 \right); & h \leq a \\ \sigma^2 (1) & \text{otherwise} \end{cases}$$

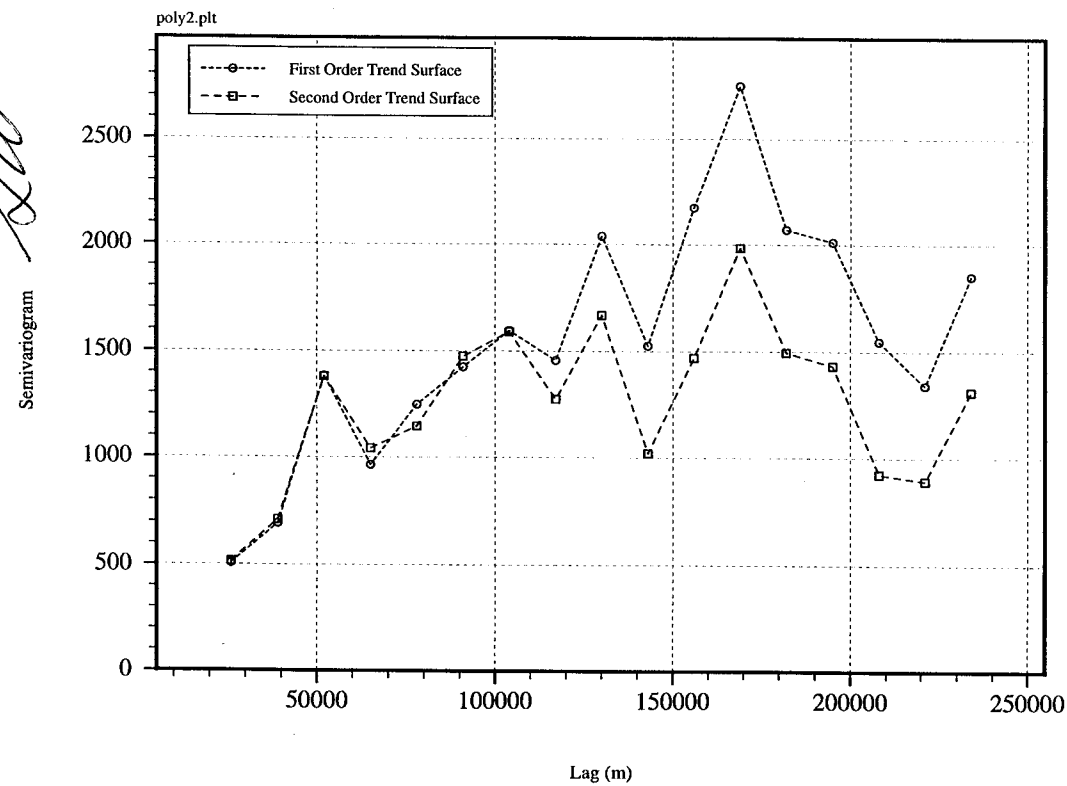
where $a = 150000$ meters, $\sigma^2 = \text{sill} = 1830$



Semivariogram for AAP Residuals without Rain Shadow Effect ⁽²⁾



Semivariogram for AAP Residuals without Rain Shadow Effect ⁽³⁾



The second order trend surface is given by

$$RES(mm) = 14942.43 - 1.16 \times 10^{-2} X - 5.52 \times 10^{-3} Y + 2.17 \times 10^{-10} X^2 + 2.81 \times 10^{-9} XY + 4.55 \times 10^{-10} Y^2$$

Then $SHADRES = RES - RES$

The semivariogram for SHADRES is shown in plot 2 on page 12 for the case where a 2nd order trend surface was fitted to RES. The range is clearly less than that for $\gamma(h)$ for the 1st order trend surface. A suitable semivariogram model may be given by:

$$\gamma(h) = \begin{cases} 1300 \left(1.5 \left(\frac{h}{50000} \right) - .5 \left(\frac{h}{50000} \right)^3 \right); & h \leq 50000 \\ 1300 & ; \text{otherwise} \end{cases}$$

Jordan Willemeyer

12/21/94

I believe that the spatial distribution of AAP in southern Nevada can be geostatistically estimated using a combination of kriging with an external drift and nonstationary or universal kriging.

In the southern Nevada area rainfall varies spatially as a result of 3 primary factors:

1. Orographic effects,
2. Rainshadow effect of the Sierra Nevada,
3. Winter frontal precip in the ~~west~~ ^{12/21/94} western portion predominates, summer monsoonal precip is more important in the eastern portions.

Because the orographic effect can be modelled by a simple linear relationship between AAP and elevation, and because elevation measurements (or estimates) are dense in DEM coverage, it makes sense to treat it as the external drift model. Once the orographic effect is removed from the AAP data the rainshadow effect is more obvious, showing a pronounced northwest-southeast trend. If the proper polynomial trend surface is fitted to the residual AAP data, the resulting (AAP - Orographic Effect) - Rainshadow Effect = RESRAIN resembles a stationary RF which may be spatially estimated using kriging.

AAP^* : measured average annual precipitation in mm.

1. Orographic model

$$\hat{AAP} = \exp(a + b \text{ELEV})$$

where ELEV is elevation in meters.

2. Orographic Residual

$$RESAAP = AAP^* - \hat{AAP}(ELEV^*)$$

$ELEV^*$ = elevation at measurement location.

3. Orographic Residual model (polynomial trend surface) (aka rainshadow effect model.)

$$\hat{RESAAP}_1 = \alpha + \beta X + \delta Y \quad ; \text{ 1st order model.}$$

X : X-coordinate in UTM (m)

Y : Y-coordinate in UTM (m)

$$\hat{RESAAP}_2 = \alpha + \beta X + \delta Y + uX^2 + vXY + oY^2 \quad ; \text{ 2nd order model.}$$

4. Rainshadow residual

$$RESRAIN = RESAAP - \hat{RESAAP}_i \quad ; \quad i=1 \text{ or } 2$$

(aka SHADRES on pages 10-13)

RESRAIN is intrinsic and may be spatially estimated by ordinary kriging.

The final spatial estimate of AAP is obtained by:

1. Fitting RESRAIN on the domain of interest
 RESRAIN_j ; $j = 1, \dots, \text{nodes on grid}$

2. Estimating RESAAP on the same grid

$$\text{RESAAP}_{1j} = \alpha + \beta X_j + \delta Y_j$$

or

$$\text{RESAAP}_{2j} = \alpha + \beta X_j + \delta Y_j + \mu X_j^2 + \nu X_j Y_j + \sigma Y_j^2$$

3. Estimating AAP due to orographic effect

$$\text{AAP}_j = \exp(\alpha + b \text{ELEV}_j)$$

4. Add up the effects

$$\text{AAP}_j = \text{AAP}_j + \text{RESAAP}_j + \text{RESRAIN}_j$$

Example of how we will do this.

1. Estimation of RESAAP at each node of the decimalized DEM ($36^\circ \rightarrow 38^\circ \text{N}$, $-115^\circ \rightarrow -18^\circ \text{W}$) are in the file ...

/home/gwitt/Ischyaetal/rain.utm

X-UTM (m)	Y-UTM (m)	AAP (mm)	Elev (m)
571477.625	4059803.250	157.000	1036.320
587903.562	4052634.000	157.000	1005.230
589385.688	4056310.250	159.000	1149.086
563978.688	4070837.500	119.000	1043.026
580272.875	4074747.000	208.000	1219.200
592156.125	4072981.000	128.000	938.784
566792.750	4087499.500	225.000	1725.168
574151.625	4091332.750	226.000	1420.368
584585.750	4089544.250	177.000	1194.816
563758.062	4100456.000	202.000	1469.136
572648.250	4100527.750	245.000	1517.904
584456.188	4102523.750	177.000	1241.146
569503.250	4115256.750	295.000	2282.952
585797.938	4119179.500	193.000	1391.412
562189.625	4107877.500	229.000	1572.768
624217.062	4219539.000	321.000	1905.000
662317.312	4136958.250	128.000	1048.512
716377.625	3984526.000	139.000	769.620
719152.750	4166016.500	231.000	1343.254
613593.000	4030745.500	230.000	1828.800
660934.938	4055467.500	320.000	2301.240
665043.250	3994509.000	104.000	658.978
672351.250	4007634.000	106.000	554.738
731299.312	4044195.500	91.000	371.856
724110.562	4201242.500	313.000	1865.376
632002.438	3999496.000	270.000	1981.200
627448.062	4003200.750	354.000	1859.280
689009.125	3926628.750	185.000	1078.992
388755.781	4208366.500	142.000	1935.480
522268.719	4085491.250	159.000	1082.040
511918.781	4033668.500	69.000	-51.206
646379.062	4033013.500	106.000	890.016
410244.312	4163603.250	125.000	1516.380
479459.625	4172350.750	136.000	1734.312
619255.625	4049239.750	116.000	955.853
553630.938	4056012.250	85.000	663.245
403923.594	4248677.000	115.000	1387.145
589883.625	4008279.750	126.000	822.960
572688.438	4255887.000	121.000	1802.282
500000.000	4128063.250	90.000	1225.296
492719.281	4213046.500	163.000	1654.150
479561.312	4213068.500	126.000	1857.146

/home/gwitt/Ischyaetal/drift.f

```

*****
*** Program reads in the rainfall data and uses an ***
*** external regression or drift model to produce ***
*** the residuals, which are then used to compute ***
*** the semivariogram. Gordon Wittmeyer, CNWRA ***
*** 12/9/94. ***
*****

c
c      program drift
c
c      implicit none
c
c      real*4 long , lat , aap , elev , a1 , a2 , resaap
c      real*4 reslog
c
c      open(7,file='rain_utm',status='old')
c      open(8,file='rain_res.dat',status='unknown')
c      open(9,file='rain_log.dat',status='unknown')
c
c      a1 = 4.3146
c      a2 = .0005872
c
c
c      1 read(7,*,end=2) long , lat , aap , elev
c      reslog = alog(aap) - (a1 + a2 * elev)
c      resaap = aap - exp(a1 + a2 * elev)
c      write(8,*) long , lat , resaap
c      write(9,*) long , lat , alog(aap)
c      goto 1
c
c      2 stop
c      end

```

Measured AAP at 42 stations in Southern Nevada

/home/gwitt/Ischyaetal/rain-res.dat

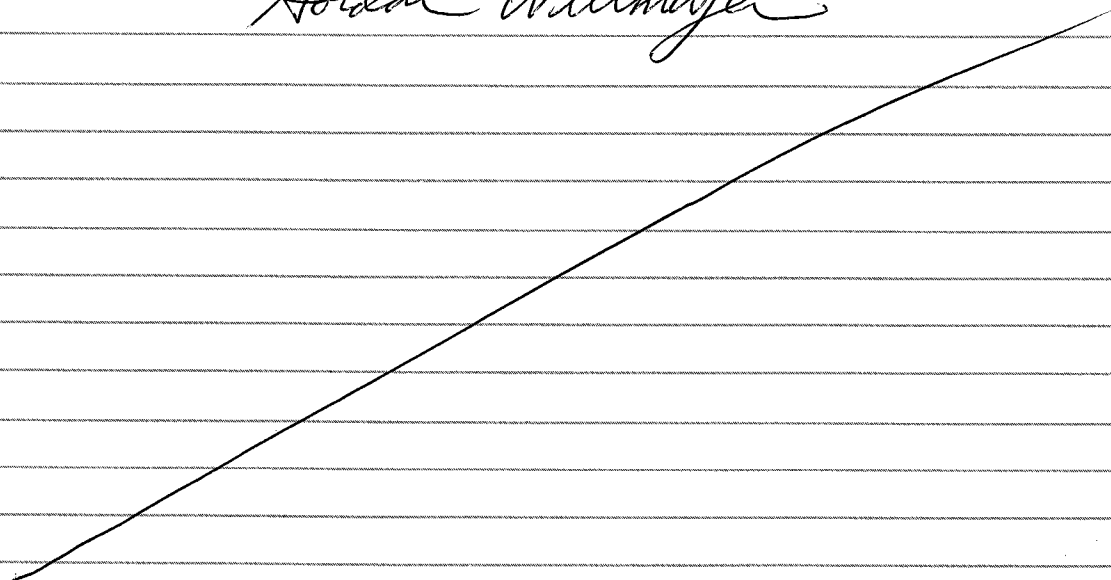
X-UTM (m)	Y-UTM (m)	RESAAP (mm)
571478.	4.05980E+06	19.5683
587904.	4.05263E+06	22.0545
589386.	4.05631E+06	12.1591
563979.	4.07084E+06	-18.9740
580273.	4.07475E+06	54.9883
592156.	4.07298E+06	-1.78169
566793.	4.08750E+06	19.0531
574152.	4.09133E+06	53.8028
584586.	4.08954E+06	26.1636
563756.	4.10048E+06	24.8004
572648.	4.10053E+06	62.6527
584456.	4.10252E+06	22.0038
569503.	4.11528E+06	9.24081
585798.	4.11918E+06	23.7060
562190.	4.10788E+06	40.6825
624217.	4.21954E+06	92.1158
662317.	4.13696E+06	-10.41914
716378.	3.98453E+06	21.4903
719153.	4.16602E+06	66.4263
613593.	4.03075E+06	11.1314
660935.	4.05547E+06	31.1557
665043.	3.99451E+06	-6.11794
672351.	4.00763E+06	2.42036
731299.	4.04420E+06	-2.03295
724111.	4.20124E+06	89.3799
632002.	3.99950E+06	30.6419
627448.	4.00320E+06	131.179
689009.	3.92663E+06	44.0812
388758.	4.20837E+06	-91.0175
522289.	4.08549E+06	17.8287
511919.	4.0367E+06	-3.56855
646379.	4.03301E+06	-20.1179
410244.	4.16360E+06	-57.1842
479460.	4.17235E+06	-71.0557
619256.	4.04924E+06	-15.0891
553631.	4.05601E+06	-25.3942
403924.	4.24868E+06	-53.8704
589884.	4.00828E+06	4.75152
572688.	4.25587E+06	-94.4869
500000.	4.12606E+06	-63.5604
492719.	4.21305E+06	-34.5352
479581.	4.21307E+06	-96.5421

← Measured AAP at
42 Stations in southern
Canada minus the geographic
effect given by the model

$$RESAAP = AAP - \exp(4.3146 + .0005872ELEV)$$

[Handwritten signature]

Gordon Wittmayer



12/22/94

Because the raw data on AAP contain an
estimate of variance, and because the variance
is not the same at all sample locations, it
is apparent that generalized least squares procedures
are needed to determine the coefficients a & b of

$$\log(AAP) = (a + b ELEV).$$

I used the Numerical Recipes subroutine FIT to
estimate a & b . The coefficients on the equation
in

$$AAP = \exp(4.2893 + .00065348 ELEV) \text{ Model 2}$$

GLS

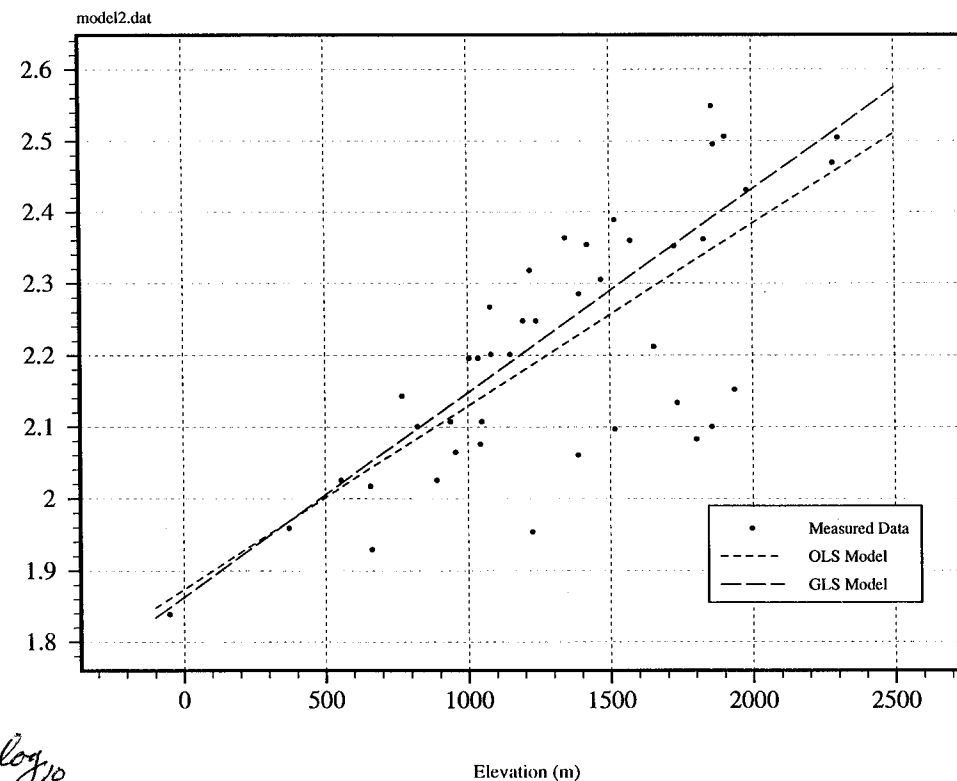
compared to

$$AAP = \exp(4.3145 + .0005873 ELEV) \text{ Model 1}$$

OLS

obtained using OLS!

[Handwritten signature]
★ $\log_{10}(AAP)$ (mm)



★ \log_{10}

EPS version of the chone file is given:

1 home/gwitt/Ischjetal/orograph.eps

2 Separate files of RESAAP = AAP - exp(a + b ELEV)

For OLS model: 1 home/gwitt/Ischjetal/rain-res-ols.dat

For GLS model: 1 home/gwitt/Ischjetal/rain-res-gls.dat

Polynomial drift models:

A. For OLS model based residuals

i.) 1st order drift

$$\hat{RESAAP} = 67.6095 + 3.337 \times 10^{-4} X + 6.262 \times 10^{-5} Y$$

RESRAIN = $\hat{RESAAP} - RESAAP$ in in

1 home/gwitt/Ischjetal/ols-poly1.dat

Model coefficients are in Variogram
 ↳ "loc"/ols-poly1.coef ↳ "loc"/ols-poly1.plt

ii) 2nd order drift

RESRAIN : "loc"/ols-poly2.dat
 Coefficients : "loc"/ols-poly2.coef
 Variogram : "loc"/ols-poly2.plt

iii) 3rd order drift

RESRAIN : "loc"/ols-poly3.dat
 Coefficients : "loc"/ols-poly3.coef
 Variogram : "loc"/ols-poly3.plt

B For GLS model based residuals

i) 1st order drift model

RESRAIN : ^{glw} "loc"/glw-poly1.dat
 Coeff : "loc"/glw-poly1.coef
 Variogram : "loc"/glw-poly1.plt

ii) 2nd order drift model

RESRAIN : "loc"/glw-poly2.dat
 Coeff : "loc"/glw-poly2.coef
 Variogram : "loc"/glw-poly2.plt

iii) 3rd order drift

RESRAIN : "loc"/glw-poly3.dat
 Coeff : "loc"/glw-poly3.coef
 Variogram : "loc"/glw-poly3.plt

Example of building the AAP distribution using an ~~external~~ drift model and residual kriging.

1. Kriged RESRAIN based on GKS and the 3rd order trend.

a) Kriging location in small-coord. utm

b) Scattered data in gls-poly3.dat

c) Assume spherical variogram model with
range = 80000 (m)
sill = 1000

d) Kriging output glS-poly3.krig

2 Next:

a) Estimate RESAPP using the 3rd order drift model based on GKS

b) Estimate AAP by the GKS model and add

$$\hat{RESRAIN} + \hat{RESAPP} + \hat{AAP} = \hat{AAP}$$

Gordon Willmeyer

12/27/94

The program "builder.f" was written to add together the kriged rainshadow residuals, the mean rainshadow effect, and the orographic effect.

Files: (all on "/home/gwillm/Isoshyetal")

1. Kriged rainshadow residuals: "glS-poly3.krig"

2. Elevation data file: "small-coord.utm"
"small.utm"

3. File containing coefficients of polynomial trend surface describing the mean rainshadow effect
"glS-poly3.coef"

4. Output file containing the average annual precipitation estimated for Southern Nevada Using:

i. GKS to fit the orographic model,

ii. A 3rd degree polynomial trend surface to model the mean rainshadow effect,

iii. Rainshadow residuals kriged with a spherical variogram model $r = 80000$ m, $sill = 1000$,

is "glS-poly3.aap."

5. Output file containing the orographic and mean rainshadow effect only is "glS-poly3.mean"

Use EarthVision to grid and contour both the aap and mean aap estimates.

1. On SGI Output of poly3 ^{mean} ~~aap~~ is called
HW 12/27/94

gls-poly3-mean.dat \Rightarrow

gls-poly3-mean.zgrd

2. On SGI Output gls poly3 ^{HW} ~~in aap~~ is

gls-poly3-aap.dat \rightarrow

gls-poly3-aap.zgrd

Gordon Willmeyer

1/3/95

I discovered a mistake in fitting the precipitation model using GKS. Apparently I had typed in the length of record instead of the standard deviation and thus the GKS estimates are incorrect.

	UTM Coord		SG DU AAP(mm)	1/3/95 Elev(m)	# years of record
	X	Y			
rain-std. utm	571477.625	4059803.250	157.000	1036.320	8 23
in	587903.562	4052634.000	157.000	1005.230	15 17
/home/gwillm/	589385.688	4056310.250	159.000	1149.096	13 18
Isohyetal	563978.688	4070837.500	119.000	1043.026	16 15
	580272.875	4074747.000	208.000	1219.200	21 21
	592156.125	4072981.000	128.000	938.784	19 12
	566792.750	4087499.500	225.000	1725.168	12 25
	574151.625	4091332.750	226.000	1420.368	13 23
	584585.750	4089544.250	177.000	1194.816	25 17
	563756.062	4100456.000	202.000	1469.136	18 18
	572648.250	4100527.750	245.000	1517.904	20 23
	584456.188	4102523.750	177.000	1241.146	22 17
	569503.250	4115256.750	295.000	2282.952	17 31
	585797.938	4119179.500	193.000	1391.412	8 22
	562189.625	4107877.500	229.000	1572.768	8 36
	624217.062	4219539.000	321.000	1905.000	47 16
	662317.312	4136958.250	128.000	1048.512	26 10
	716377.625	3984526.000	139.000	769.620	50 9
	719152.750	4166016.500	231.000	1343.254	51 11
	613593.000	4030745.500	230.000	1828.800	8 33
	660934.938	4055467.500	320.000	2301.240	9 27
	665043.250	3994509.000	104.000	658.978	33 8
	672351.250	4007634.000	106.000	554.736	32 8
	731299.312	4044195.500	91.000	371.856	26 13
	724110.562	4201242.500	313.000	1865.376	44 16
	632002.438	3999496.000	270.000	1981.200	8 36
	627448.062	4003200.750	354.000	1859.280	8 47
	689009.125	3926628.750	185.000	1078.992	50 14
	388755.781	4206366.500	142.000	1935.480	15 17
	522268.719	4085491.250	159.000	1082.040	47 12
	511918.781	4033668.500	69.000	-51.206	18 7
	646379.062	4033013.500	106.000	890.016	42 8
	410244.312	4163603.250	125.000	1516.380	31 9
	479459.625	4172350.750	136.000	1734.312	39 12
	619255.625	4049239.750	116.000	955.853	25 16
	553630.938	4056012.250	85.000	663.245	21 11
	403923.594	4248677.000	115.000	1387.145	53 7
	589883.625	4008279.750	126.000	822.960	20 16
	572688.438	4255867.000	121.000	1802.282	20 13
	500000.000	4126063.250	90.000	1225.296	14 13
	492719.281	4213046.500	163.000	1654.150	29 10
	479561.312	4213068.500	126.000	1857.146	22 11

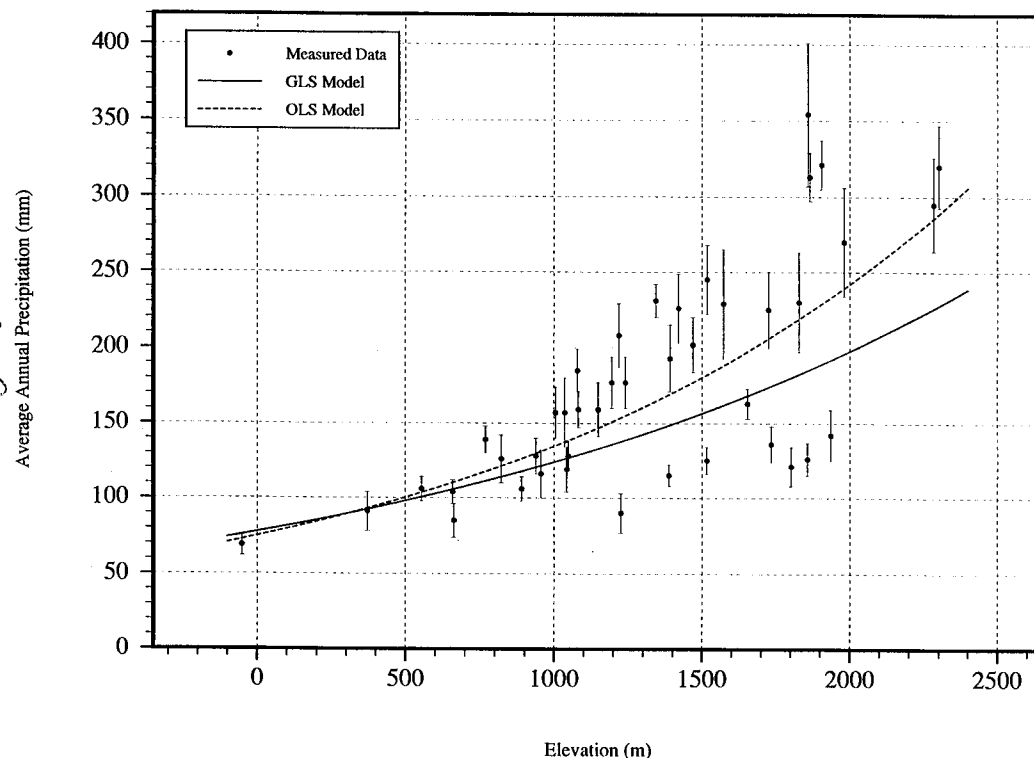
Program chi-fid.f must be modified and
rerun.

AW 11/14/95
Correct GLS model
GLS

$$AAP = \exp(4.35098 + 0.00468369 \text{ ELEV})$$

Compare to OLS model

$$AAP = \exp(4.3145 + 0.005873 \text{ ELEV})$$



↑
This file is /home/gawth/Isoplethal/orograph.eps

Now I must redo the steps outlined on pages
20-24 for the GLS orographic model.

1. Construct rain-ras-gls.dat using drift.f.

2. Fit new polynomial drift model to orographic residuals.
using rainshad.f

i) 1st order drift model

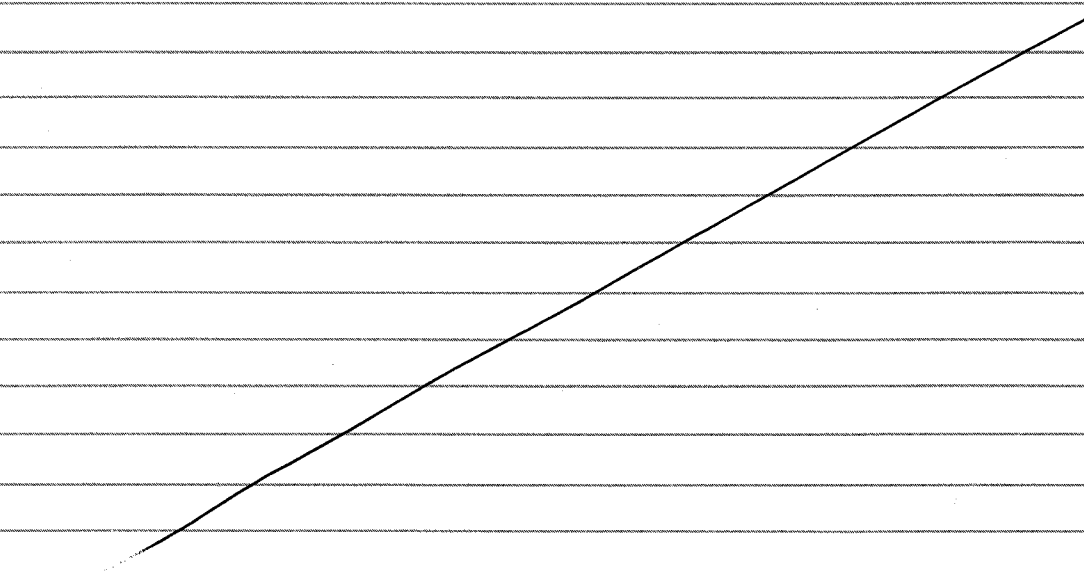
RESRAIN: "loc"/gls-poly1.dat
Coef: "loc"/gls-poly1.coef
Variogram: "loc"/gls-poly1.plt

ii) 2nd order drift model

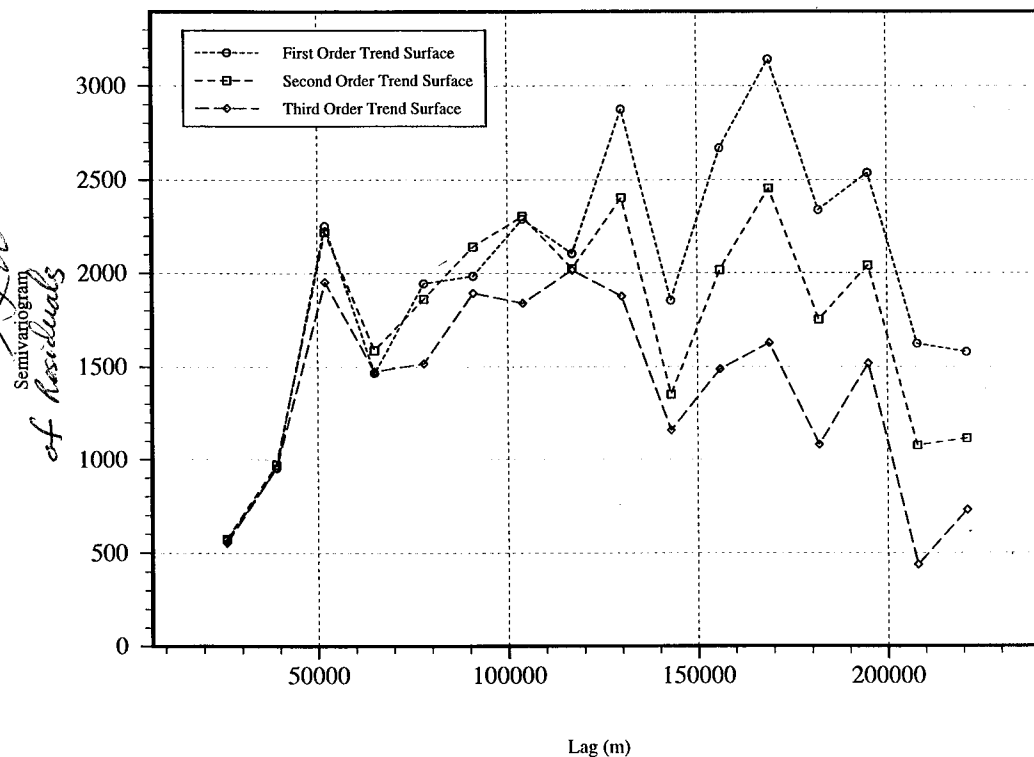
RESRAIN: "loc"/gls-poly2.dat
Coef: "loc"/gls-poly2.coef
Variogram: "loc"/gls-poly2.plt
AW 1/31/95

iii) 3rd order drift model

RESRAIN: "loc"/gls-poly3.dat
Coef: "loc"/gls-poly3.coef
Variogram: "loc"/gls-poly3.plt



For GKS Orographic Model



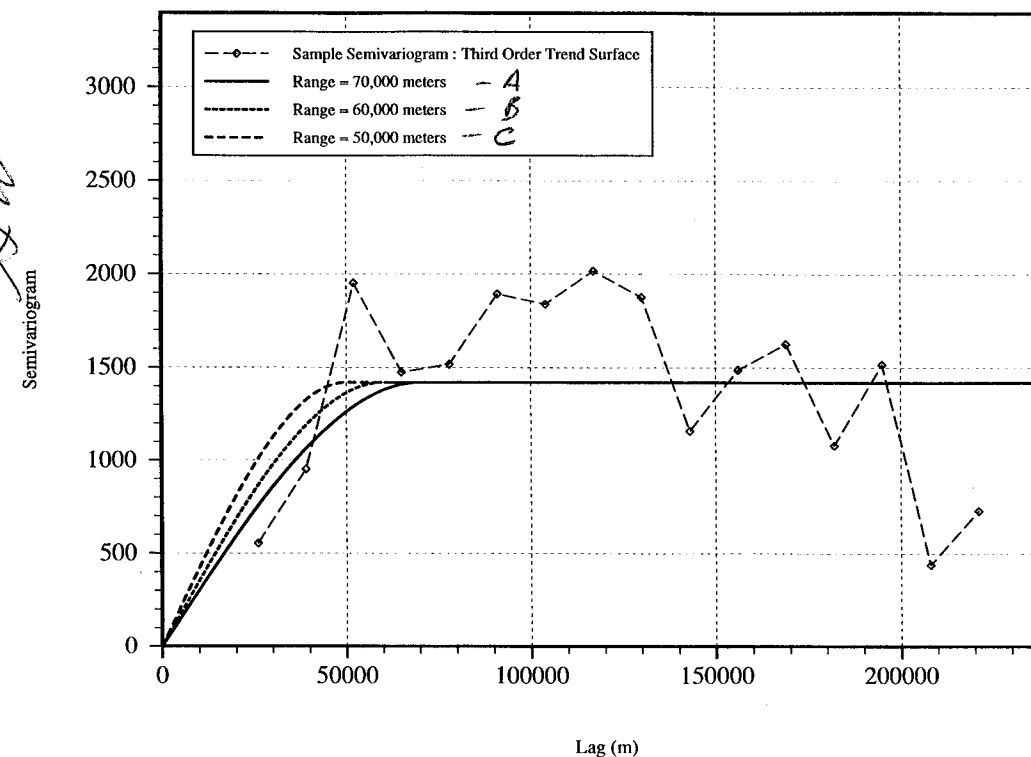
This plot is saved as /home/gwitt/Isoklyetal/variogram.eps

Exporting model semi-variogram to the ^{HW} ~~other~~ sample semi-variogram

For the semi-variogram corresponding to the 3rd order trend surface

A: Model 1: Spherical sill = $\sigma^2 = 1420$, range = 70,000
 B: Model 2: " " " , range = 60,000
 C: Model 3: " " " , range = 50,000

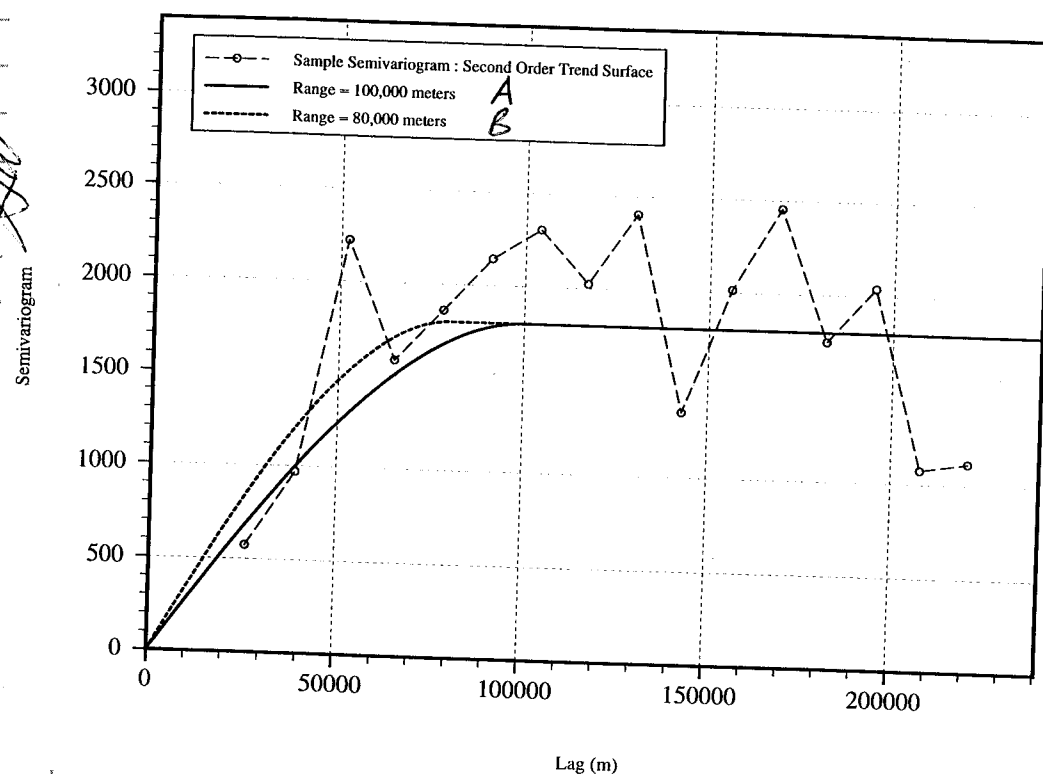
Sample Semi-variogram & Model σ^2 for residuals after 3rd order surface was fitted to AAP- orographic effect



For semi-variogram corresponding to the 2nd order trend surface

Model A: Spherical sill = $\sigma^2 = 1800$, range = 100,000

Model B: " " " " , range = 80,000



It feel that for the precip-elevation model fitted using GLS, the resulting residuals are best modelled using a 2nd order trend surface. This argument is based on the observation that the residuals RESRAIN produce a fairly stationary sample semivariogram. The selected semivariogram model is a spherical with sill ≈ 1800 & range = 80,000 m.

Now produce maps of the final AAP values

1. Kriged rainshadow residuals are in gls-poly2.krig
2. elevation data is in small.wtm
3. drift coefficients gls-poly2.coef
4. AAP is in gls-poly2.aap.

5. $\hat{RESAAP} + \hat{AAP}$ is in gls-poly2-oro.shad.

6. AAP is in gls-poly2-oro

Transfer files to ONYX and visualize.

1. gls-poly2.aap \rightarrow gls-poly2-aap.dat

2. gls-poly2-oro.shad \rightarrow gls-poly2-oro-shad.dat

3. gls-poly2.oro \rightarrow gls-poly2-oro.dat

Gordon Wiltschko

1/4/95

On the ONYX the following EarthVision grid files were created

$$\textcircled{1} \begin{array}{l} \text{gls-poly2-aap.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array} \left. \vphantom{\begin{array}{l} \text{gls-poly2-aap.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array}} \right\} \begin{array}{l} \hat{AAP} = \hat{RESRAIN} + \hat{RESAAP} \\ \quad \quad \quad + \hat{AAP} \end{array}$$

$$\textcircled{2} \begin{array}{l} \text{gls-poly2-oro-shadow.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array} \left. \vphantom{\begin{array}{l} \text{gls-poly2-oro-shadow.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array}} \right\} \begin{array}{l} \hat{RESAAP} + \hat{AAP} \end{array}$$

$$\textcircled{3} \begin{array}{l} \text{gls-poly2-oro.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array} \left. \vphantom{\begin{array}{l} \text{gls-poly2-oro.dat} \\ \star \quad \quad \quad \text{-2grd} \end{array}} \right\} \hat{AAP}$$

These files reflect the new GIS estimates of the precip-elevation relation and the 2nd order trend surface fitted to ^{SW} ~~residuals~~ orographic residuals. _{1/4/95}

Need to briefly test a few more semivariogram models for the residuals obtained after removing the orographic effect with elev-precip model, and the residual rain shadow effect using a 2nd order trend surface

Model A: Spherical sill = 1800, range = 100,000

$$\begin{array}{l} \text{"loc"} \quad \left. \begin{array}{l} RMSE = 1.2682 \\ SMSE = 3.6602 \end{array} \right\} \text{from cross-validation} \end{array}$$

1 loc / gwith / Isohyetal / gls-poly2-cross.mod1

Model B: Spherical sill = 1800, range = 80,000

$$RMSE = 1.1533$$

$$SMSE = 2.8781$$

1 loc / gls-poly2-cross.mod2

Model C: Spherical sill = 1800, range = 60,000

$$RMSE = 1.0188$$

$$SMSE = 2.0726$$

1 loc / gls-poly2-cross.mod3

Model D: Spherical sill = 1800, range = 40,000

$$RMSE = .86288$$

$$SMSE = 1.3632$$

1 loc / gls-poly2-cross.mod4

I would select this model!!

Model E: Spherical sill = 1800, range = 20,000

$$RMSE = .88256$$

$$SMSE = 1.0227$$

1 loc / gls-poly2-cross.mod5

Model F: Nugget = 400, Spherical sill = 1400, range = 40,000

$$RMSE = 1.1096$$

$$SMSE = 1.5375$$

1 loc / gls-poly2-cross.mod6

Model G: Spherical : sill = 2000, range = 40,000

$$RMSE = .7766$$

$$SMSE = 1.2269$$

1 loc / gls-poly2-cross.mod7

Model H: Spherical : sill = 2000, range = 40,000
neighborhood $r = 30,000$, num = 4 / quad

Optim not functioning for cross-validation.

Model D is selected as the best model among those tested by cross-validation

$$RMSE = \frac{1}{\sum_{i=1}^{n_i} n_i} \sum_{i=1}^{n_i} \left[z_i^*(x_k) - z_i(x_k) \right]^2$$

is a measure of accuracy, would like

$$RMSE = 0$$

$$SMSE = \frac{1}{\sum_{i=1}^{n_i} n_i} \sum_{i=1}^{n_i} \frac{\left[z_i^*(x_k) - z_i(x_k) \right]^2}{\sigma_k^2(x_k)}$$

is a measure of consistency of the estimation variance

$$1 - 2(2/n_i)^{.5} \leq SMSE \leq 1 + 2(2/n_i)^{.5}$$

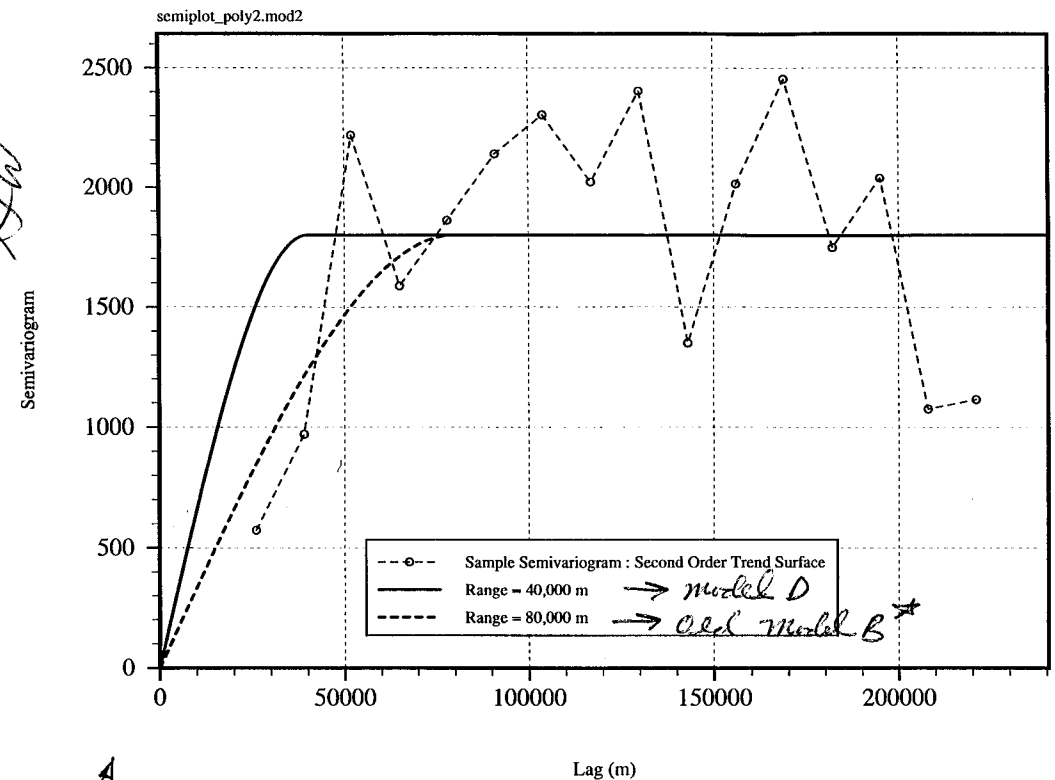
$$n_i = 41$$

$$.5583 \leq SMSE \leq 1.442$$

Although Model G appears to be better than D based on RMSE & SMSE I prefer to use a model with a sill equal to the sample variance.

Re-krige RESRAIN using model D

⇒ gls_poly2.krige in "loc"



* See page 29 for defn of "old" Model B.

EPS file in "loc" / modeld_semi.eps

Now produce maps of final AAP values

1. Krige rainshadow residuals are in gls_poly2.krige
2. Elevation data is in small.utm
3. drift coefficients are in gls_poly2.coef
4. AAP is in gls_poly2.aapz
5. RESAAP + AAP is in gls_poly2.oro.shad.z
6. AAP is in gls_poly2.oro.z

On the ONYX

- ① $\left. \begin{array}{l} \text{gls-poly2-aap2.dat} \\ \star \quad \quad \quad \text{.zgrd} \end{array} \right\} \hat{AAP}$
- ② $\left. \begin{array}{l} \text{gls-poly2-oro-shad2.dat} \\ \star \quad \quad \quad \text{.zgrd} \end{array} \right\} \hat{RESAAP} + \hat{AAP}$
- ③ $\left. \begin{array}{l} \text{gls-poly2-oro2.dat} \\ \star \quad \quad \quad \text{.zgrd} \end{array} \right\} \hat{AAP}$

Jordan Willemse

1/9/95

Need to redo all isohyals and recharge maps based on the OLS orographic precip. model so that the new cross-validation procedure can be used to select the model semivariogram for RESRAIN.

Recall:

1. Orographic model using OLS is

$$\hat{AAP} = \exp(4.3145 + .0005873 \text{ ELEV})$$

2. Fit polynomial trend surface to

$$\begin{aligned} \text{RESAAP}^{\star} &= \text{AAP}^{\star} - \hat{AAP} \\ &= (\text{measured AAP} - \text{predicted AAP}) \end{aligned}$$

3. Remove polynomial trend surface from RESAAP

$$\begin{aligned} \text{RESRAIN}^{\star} &= \text{RESAAP}^{\star} - \hat{RESAAP} \\ &= (\text{AAP}^{\star} - \hat{AAP} - \sum_{i=1}^{np} a_i f_i(X)) \end{aligned}$$

4. Fit model semivariogram to RESRAIN^{\star} using cross-validation.

5. Kriging estimator of $\hat{RESRAIN}$ at all grid points

6. Add up all effects.

$$\hat{AAP} = \hat{RESRAIN} + \hat{RESAAP} + \hat{AAP}$$

i) RESAAP^{*} is in /loc/rain-res-ols.dat
obtained using drift.f

ii) Fit polynomial surface to RESAAP^{*} using
rainshad.f

a) 1st order drift model

RESRAIN: "loc" / ols-poly1.dat
coef : " / ols-poly1.coef
r : " / ols-poly1.plt

b) 2nd order drift model

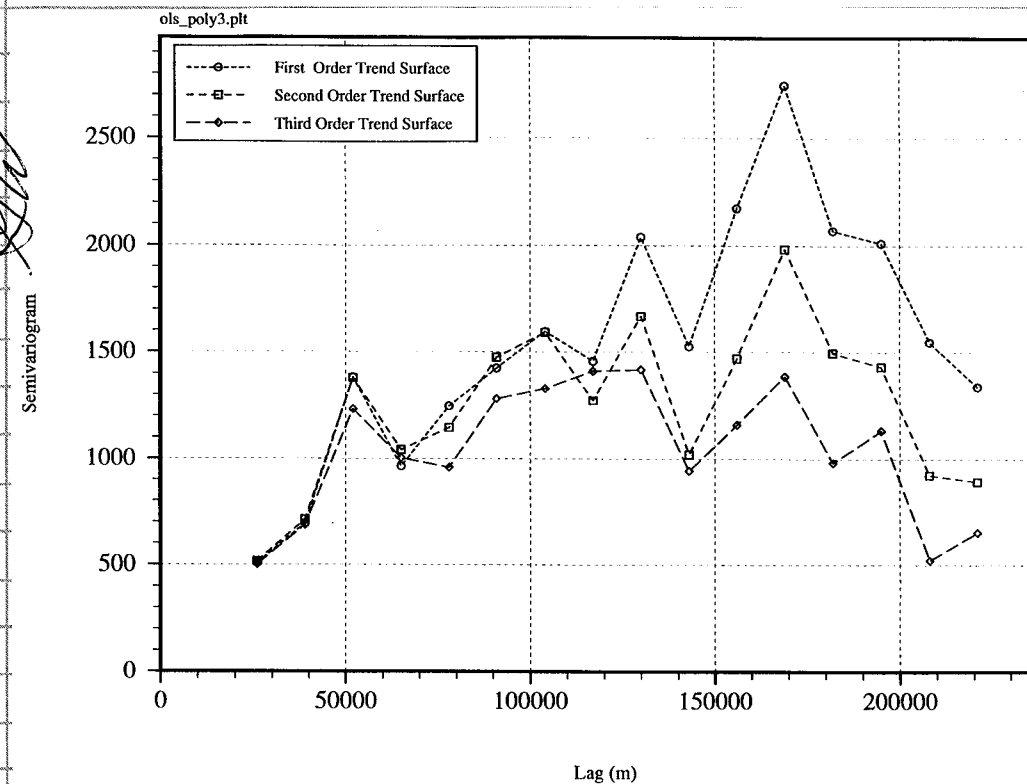
RESRAIN: loc / ols-poly2.dat
coef : " / ols-poly2.coef
r : " / ols-poly2.plt

c) 3rd order drift model

RESRAIN: loc / ols-poly3.dat
coef : " / ols-poly3.coef
r : " / ols-poly3.plt

iii) Plot semivariogram (sample semivariogram)

Plot file is als-vario.eps



It appears that a 3rd order trend needs to be removed from RESAAP before RESRAIN yields a stationary sample semivariogram.

iii) Use cross validation to select final semivariogram model

a) Model 1 Spherical sill = 1080, range = 60,000 m

RMSE = 1.3290

SMSE = 3.2540

b) Model 2 Spherical sill = 1080, range = 40,000

RMSE = 1.1565

SMSE = 2.0873

c) Model 3 Spherical sill = 1080, range = 20,000

$$RMSE = 1.0756$$

$$SMSE = 1.2953$$

d) Model 4 Spherical sill = 1080, range = 10,000

$$RMSE = 1.0561$$

$$SMSE = 1.0967$$

e) Model 5 Spherical sill = 1080, range = 15,000

$$RMSE = 1.0480$$

$$SMSE = 1.1571$$

f) Model 6 Pure nugget = 1080
test failed!

g) Model 7 Spherical sill = 1080 range = 17,500

$$RMSE = 1.0574$$

$$SMSE = 1.2172$$

h) Model 8 Spherical Sill = 1080 range = 10

$$RMSE = 1.0448$$

$$SMSE = 1.0709$$

↑
Nearly ϕ correlation

i) Model 9 Spherical sill = 1080, range = .001

$$RMSE = 1.0448$$

$$SMSE = 1.0708$$

The results of this cross-validation study, are, to put it mildly, somewhat confusing. Note that for models 5 & 7, both the RMSE & SMSE reach their smallest values, however, we know that the residuals must be correlated since they are derived from the polynomial drift model. Note that SMSE will approach one as the correlation length or range goes to zero and ~~the~~^{all} samples are used to ~~fit~~^{fit}. This is because the fitted estimate at every point is identically equal to the mean of the sample values! So SMSE is really not the best measure.

I think that eye-fitting the semivariogram may ^{make} more sense until problem with cross-validation can be resolved.

Gordon Wittmeyer

1/12/95

I. Check contour of polynomial drift function.

Based on visual inspection it appears that the 3rd order trend surface polynomial that I fit to rain-res-als.dat is very similar to that fitted by EarthVision.

Compare: rain-res-als.zgrd (3rd degree trend surface)
to als-poly3-map.zgrd

(201 X 249 (396348.9, 3972563) → (693791.1, 4218688))

→ This portion of rain-res-als.zgrd extracted and regrid to make trends.zgrd

The figures look very similar leading me to conclude that my polynomial fitting program works quite well.

II raw semivariogram for

$$AAP^* - AAP = RESAAP \text{ for als eqn.}$$

rain-als.eps

raw semivariogram for

$$AAP^* - AAP = RESAAP \text{ for gls eqn.}$$

rain-gls.eps

John Willmeyer

1/13/95

From earlier work I know that the variance of the rain shadow residuals after removing an n th order polynomial trend surface is given by:

1. For OLS model

- a. 1st order poly. $\sigma^2 = 1560$
- b. 2nd " " $\sigma^2 = 1310$
- c. 3rd " " $\sigma^2 = 1080$ ✓

2. For GLS model

- a. 1st order poly. $\sigma^2 = 2040$
- b. 2nd " " $\sigma^2 = 1800$ ✓
- c. 3rd " " $\sigma^2 = 1420$

Because selecting the model semivariogram using cross-validation statistics produced some very strange results I have built a simple non-linear least square program to fit model $\gamma(h)$ to sample $\gamma(h)$.

1. For OLS model / 3rd order poly.

$$\begin{aligned} \text{sill} &= \sigma^2 = 1080 \\ \text{nugget} &= 0 \\ \text{range} &= 69,600 \text{ m.} \end{aligned}$$

2. For GLS model / 2nd order poly.

$$\begin{aligned} \text{sill} &= \sigma^2 = 1800 \\ \text{nugget} &= 0 \\ \text{range} &= 76,900 \text{ m.} \end{aligned}$$

John Willmeyer

1/17/95

Need to rebuild the AAP & other maps using these new semivariogram models.

A. For the OLS model.

1. Perform Kriging range = 69,600 m, sill = 1080, nugget = ϕ
(resid-krig.f)

a. Get cross-validation stats. (ols-poly3.cross)
RMSE = 1.4129
SMSE = 3.8560

b. Krig on the 3° x 2° area

i) Data: ols-poly3.dat
ii) Kriging locations: ^{new 1/17/95}ols-small-coord.utm
iii) Kriging output: ols-poly3.krig

2. Add orographic, rain shadow and kriged residual rain shadow effects. (builder.f)

i) Kriged rain shadow residuals: ols-poly3.krig
ii) elevation data: small.utm
iii) Coefficients of mean rain shadow polynomial: ols-poly3.coef
iv) AAP: ols-poly3.aap
v) Orographic + mean rain shadow: ols-poly3-oro.shad
vi) Orographic effect: ols-poly3.oro
vii) Mean rain shadow: ols-poly3.shad

B. For the GHS model

1. Kriging range = 76,100 m, sill = 1800, nugget = ϕ

a) Cross-validation stats (ghs-poly2.cross)
RMSE = 1.8947
SMSE = 4.5597

b) Krig on the 3° x 2° area

i) Data: ghs-poly2.dat
ii) Kriging locations: small-coord.utm
iii) Kriging output: ghs-poly2.krig

c)

2. Add orographic, rain shadow & Kriged residual rain shadow effects.

i) Kriged rain shadow residuals: ghs-poly2.krig
ii) elevation data: small.utm
iii) Coefficients of mean rain shadow polynomial: ghs-poly2.coef
iv) AAP: ghs-poly2.aap
v) Orographic + mean rain shadow: ghs-poly2-oro.shad
vi) Orographic effect: ghs-poly2.oro
vii) Mean rain shadow: ghs-poly2.shad

Using EarthVision of the SGI ONYX I have created the following graphs.

OLS:

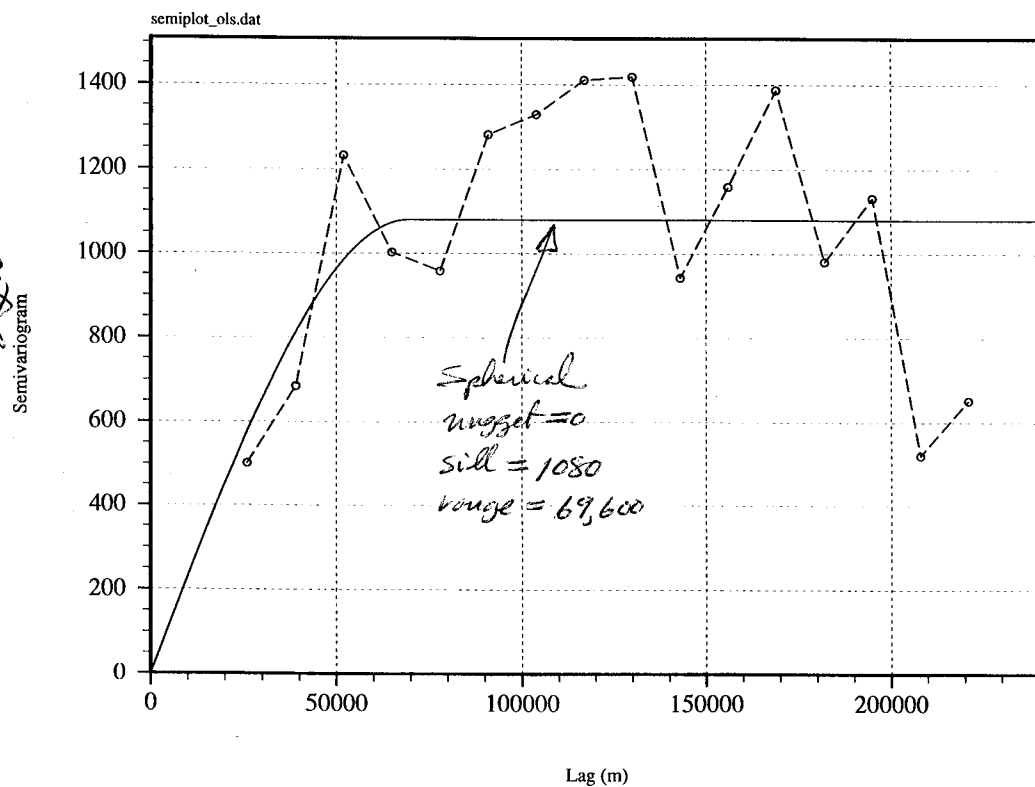
i) ~~ols poly3 aap.zgrd~~

ii) ~~ols poly3 oro.zgrd~~

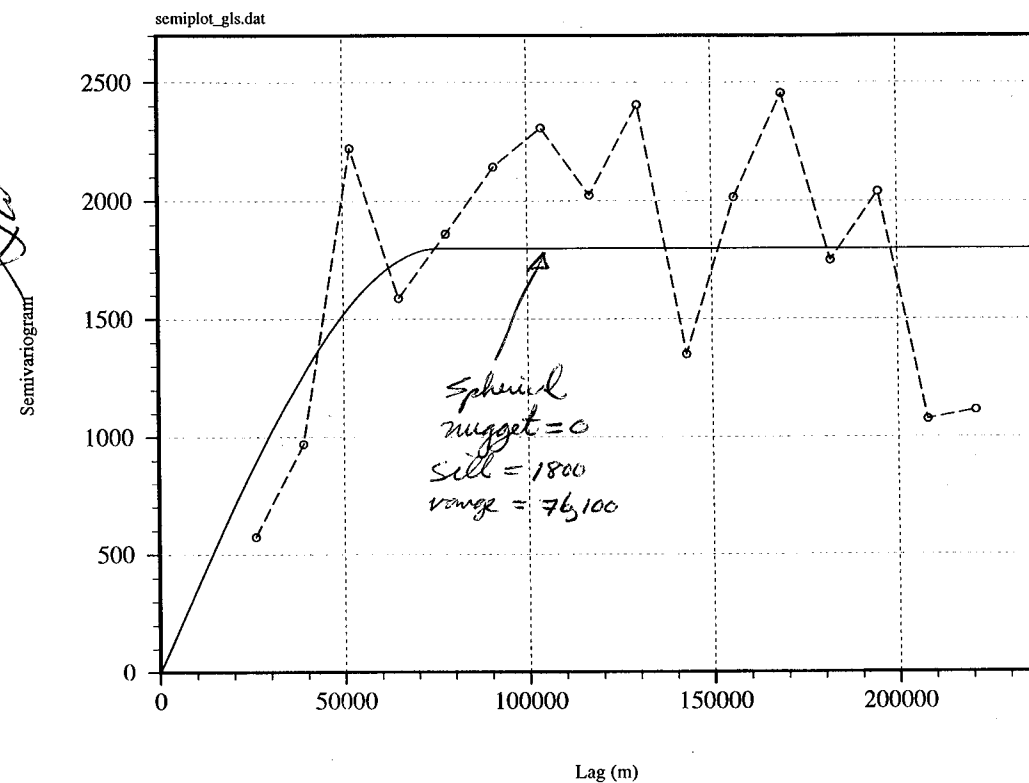
GKS:

i) ~~gks poly2 aap.zgrd~~

ii) ~~gks poly2 oro.zgrd~~



Semivariogram of rain shadow residuals from OLS or model

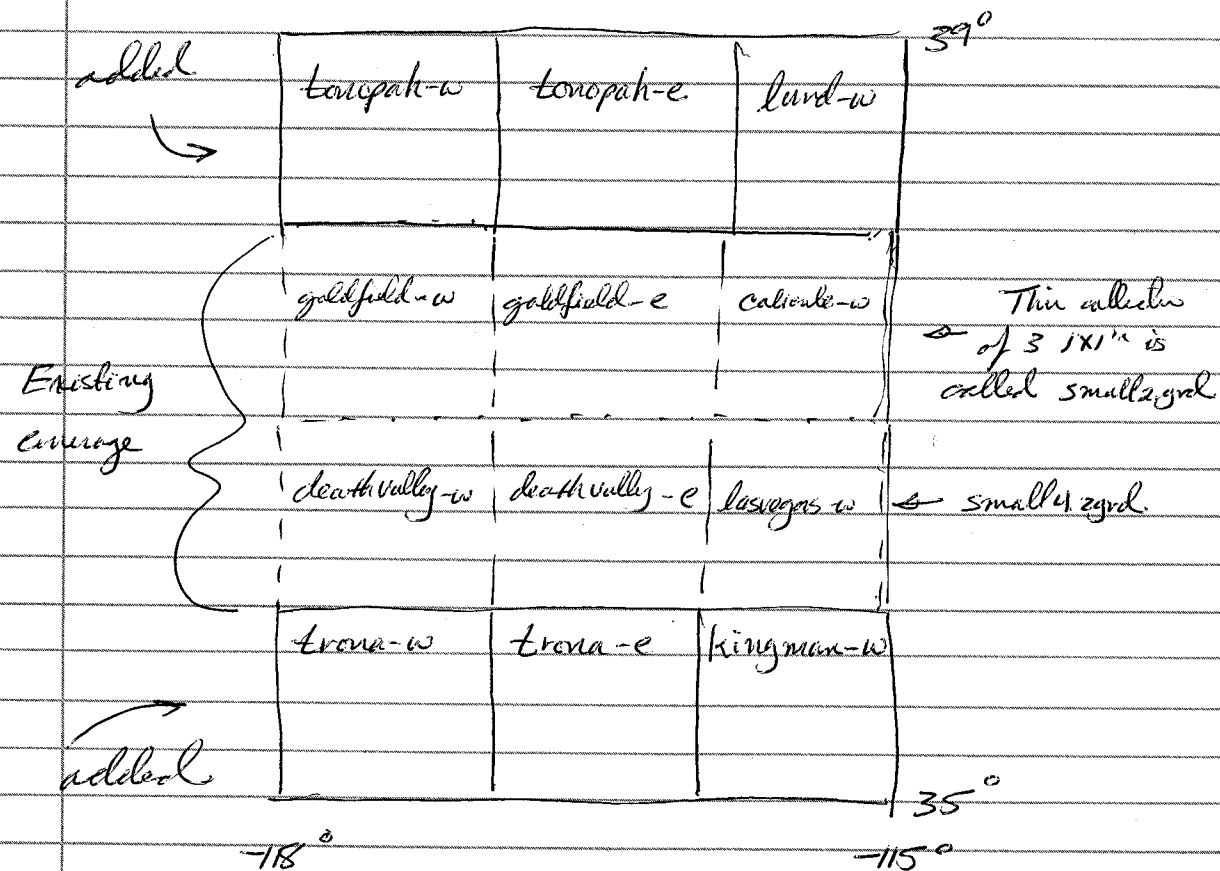


Semivariogram of rain shadow residuals from GKS or model

Gordon Willemer

April 2, 1995
(A Sunday!!)

Need to extend the region by adding the
1° x 1° degree data from:



1. Read each of the six into EV and create a
grid.

on 1px.grd

- a kingman-w → king-w.grd
- b trona-e → trona-e.grd
- c trona-w → trona-w.grd
- d land-w → land-w.grd
- e tonopah-e → tonopah-e.grd
- f tonopah-w → tonopah-w.grd

2. Now reduce the grid density of each "dem" .zgrd
from 1201 x 1201 to 101 x 101

a. king-w-small.zgrd = refgrd (king-w.grd, 101, 101,
-417600, -414000, 126000, 129600)

b. trona-e-small.zgrd = refgrd (trona-e.grd, 101, 101,
-421200, -417600, 126000, 129600)

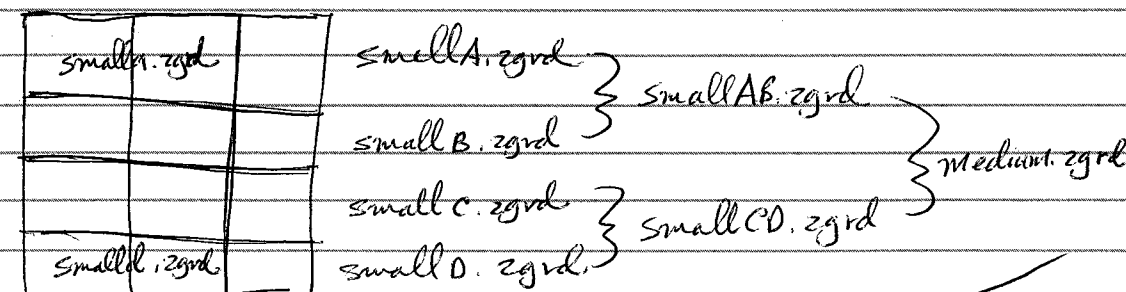
c. trona-w-small.zgrd = refgrd (trona-w.grd, 101, 101,
-424800, -421200, 126000, 129600)

d. land-w-small.zgrd = refgrd (land-w.grd, 101, 101,
-417600, -414000, 126000, 140400)

e. tonopah-e-small.zgrd = refgrd (tonopah-e.grd, 101, 101,
-421200, -417600, 126000, 140400)

f. tonopah-w-small.zgrd = refgrd (tonopah-w.grd, 101, 101,
-424800, -421200, 126000, 140400)

3. Combine all 12 1° x 1° "small" grids into one
grid using the function "uninc".



June 26, 1995

Development of a PORTFLOW grid to model free-surface flow in a 2D vertical cross-section transverse to the steep hydraulic gradient region near Syncline Ridge.

Using the program MeshMaker to construct the grid and assign the properties. Initial exported grid is "dmesh.exp" on performer. Development of a code to translate "dmesh.exp" into PORTFLOW compatible ^{AW} input file.

Gordon Wiltschko

This research project was formally closed on January 19, 1996. The work described in this scientific notebook is primarily related to the development of a procedure to estimate average annual precipitation and average annual recharge within the Death Valley region.

The spatial estimation procedure described herein combines universal kriging with kriging in the presence of an external drift function. The external drift function accounts for orographic effects, while universal or non-universal kriging is used to handle the Sierra Nevada rain shadow effect.

Gordon Wiltschko

Principal Investigator

2/5/96