

**From:** "Gauntt, Randall O" <rogaunt@sandia.gov>  
**To:** "Jason Schaperow" <JHS1@nrc.gov>, "Gauntt, Randa...  
**Date:** Thu, Jul 13, 2000 2:19 PM  
**Subject:** RE: Plume Energy

OK,  
This version seems to be right.  
Sorry about the false start.  
Randy

-----Original Message-----

**From:** Jason Schaperow [mailto:JHS1@nrc.gov]  
**Sent:** July 11, 2000 1:12 PM  
**To:** rogaunt@sandia.gov  
**Cc:** AXB@nrc.gov; AXN@nrc.gov; CGT@nrc.gov  
**Subject:** Plume Energy

Please see the attached file (WordPerfect8 format). Also, I just FAXed you a copy of the attached file (FAX number (505)-844-8719), in case you do not have a program handy to read it. Thank you very much.

Sincerely,  
Jason

**CC:** TWFN\_DO.twf5\_po(AXB,AXN,CGT)

I-35

# Analysis of Plume Energy Associated with Spent Fuel Pool Storage Accident R.O. Gauntt 7/13/2000

## Fuel and Canister Dimensions \*\*\*\*\*

$$\begin{aligned} r_{o\_clad} &:= 6.135 \text{ mm} & r_{fuel} &:= \frac{0.410}{2} \cdot \text{in} \\ r_{i\_clad} &:= 5.322 \text{ mm} & \text{can\_perimeter} &:= 4.5215 \cdot \text{in} \\ \text{assembly\_length} &:= 4.1 \text{ m} & \Delta t_{\text{canister}} &:= 0.12 \cdot \text{in} \end{aligned}$$

## Fuel Properties \*\*\*\*\*

$$\begin{aligned} \rho_{Zr} &:= 6500 \frac{\text{kg}}{\text{m}^3} & C_{p_{\text{UO}_2}} &:= 370 \cdot \frac{\text{joule}}{\text{kg} \cdot \text{K}} \\ \rho_{\text{UO}_2} &:= 0.95 \cdot 10.96 \cdot \frac{\text{gm}}{\text{cm}^3} \\ \rho_{\text{ZrO}_2} &:= 5.6 \cdot \frac{\text{gm}}{\text{cm}^3} \\ \text{MW}_{\text{Zr}} &:= 91.2 \frac{\text{gm}}{\text{mol}} & \text{MW}_{\text{N}_2} &:= 28 \cdot \frac{\text{gm}}{\text{mol}} \\ \text{MW}_{\text{ZrO}_2} &:= 123.2 \cdot \frac{\text{gm}}{\text{mol}} \\ \text{MW}_{\text{O}_2} &:= 32 \cdot \frac{\text{gm}}{\text{mol}} \end{aligned}$$

## Fuel Assembly Properties \*\*\*\*\*

$$\begin{aligned} \text{mass}_{\text{clad}} &:= 64\pi \cdot (r_{o\_clad}^2 - r_{i\_clad}^2) \cdot \text{assembly\_length} \cdot \rho_{Zr} \\ \text{mass}_{\text{canister}} &:= \text{assembly\_length} \cdot \text{can\_perimeter} \cdot \Delta t_{\text{canister}} \cdot \rho_{Zr} \\ \text{mass}_{\text{fuel}} &:= 62 \cdot \pi \cdot r_{fuel}^2 \cdot \text{assembly\_length} \cdot \rho_{\text{UO}_2} \\ \text{mass}_{\text{canister}} &= 43.039 \text{ kg} \\ \text{mass}_{\text{clad}} &= 49.91 \text{ kg} \\ \text{mass}_{\text{fuel}} &= 225.442 \text{ kg} \end{aligned}$$

**Enthalpy (Internal Energy) of Zircaloy, UO<sub>2</sub> and ZrO<sub>2</sub> \*\*\*\*\*  
Properties from MATPRO**

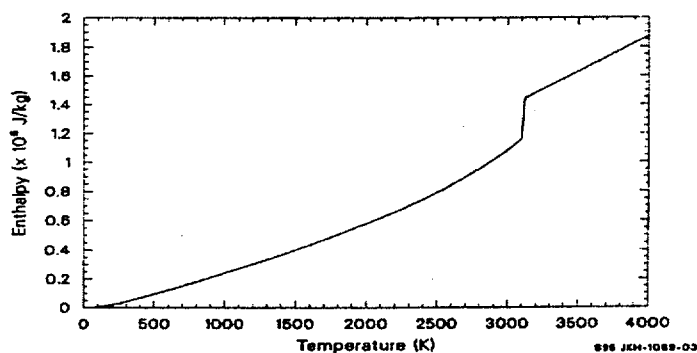
**UO<sub>2</sub> Internal Energy \*\*\*\*\***

$$\begin{aligned} K_1 &:= 296.7 \cdot K^{-1} & \theta &:= 535.285 \cdot K & \Delta H_{f\_UO2} &:= 2.74 \cdot 10^5 \cdot \frac{\text{joule}}{\text{kg}} \\ K_2 &:= 2.43 \cdot 10^{-2} \cdot K^{-2} & E_D &:= 1.577 \cdot 10^5 \cdot \frac{\text{joule}}{\text{mol}} & C_{p1\_UO2} &:= 503 \cdot \frac{\text{joule}}{\text{kg} \cdot K} \\ K_3 &:= 8.745 \cdot 10^7 & R &:= 8.3143 \cdot \frac{\text{joule}}{\text{mol} \cdot K} \end{aligned}$$

$$H_{\text{solid\_UO2}}(T) := \left[ \frac{K_1 \cdot \theta}{\left( \frac{\theta}{T} - 1 \right)} + \frac{K_2 \cdot T^2}{2} + K_3 \cdot e^{\left( \frac{-E_D}{R \cdot T} \right)} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

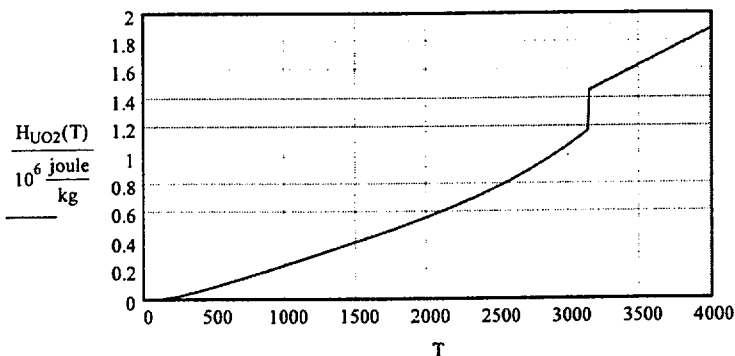
$$H_{UO2}(T) := \Phi(3138K - T) \cdot H_{\text{solid\_UO2}}(T) + \Phi(T - 3138K) \cdot [H_{\text{solid\_UO2}}(3138K) + \Delta H_{f\_UO2} + (T - 3138K) \cdot C_{p1\_UO2}]$$

$$T := 0K, 10K..4000K$$



**MATPRO Data**

**Figure 2-3. Enthalpy of UO<sub>2</sub> as a function of temperature to 4,000 K.**



**Curve Fit to MATPRO**

# Zircaloy Oxide Internal Energy \*\*\*\*\*

$$H_{300} := 1.194 \cdot 10^4$$

$$H_1(T) := \left[ 565 \cdot \frac{T}{K} + 3.055 \cdot 10^{-2} \cdot \left( \frac{T}{K} \right)^2 + 1.14 \cdot 10^7 \cdot \left( \frac{K}{T} \right) - 2.102495 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_2(T) := \left[ 604.5 \cdot \left( \frac{T}{K} \right) - 1.46 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_3(T) := \left[ 171.7 \cdot \left( \frac{T}{K} \right) + 0.1082 \cdot \left( \frac{T}{K} \right)^2 + 2.868 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_4(T) := \left[ 171.7 \cdot \left( \frac{T}{K} \right) + 0.1082 \cdot \left( \frac{T}{K} \right)^2 + 3.888 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_5(T) := \left[ 815.0 \cdot \left( \frac{T}{K} \right) + 1.39 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_{\text{ZrO}_2}(T) := \begin{cases} H_1(T) & \text{if } [(T > 273.0\text{K}) \wedge (T < 1478.0\text{K})] \\ H_2(T) & \text{if } [(T > 1478.01\text{K}) \wedge (T < 2000.0\text{K})] \\ H_3(T) & \text{if } [(T \geq 2000.0\text{K}) \wedge (T < 2558.0\text{K})] \\ H_4(T) & \text{if } [(T \geq 2558.0\text{K}) \wedge (T < 2973.0\text{K})] \\ H_5(T) & \text{if } [(T \geq 2973.01\text{K}) \wedge (T < 4100.0\text{K})] \\ 0.0 \frac{\text{joule}}{\text{kg}} & \text{otherwise} \end{cases}$$

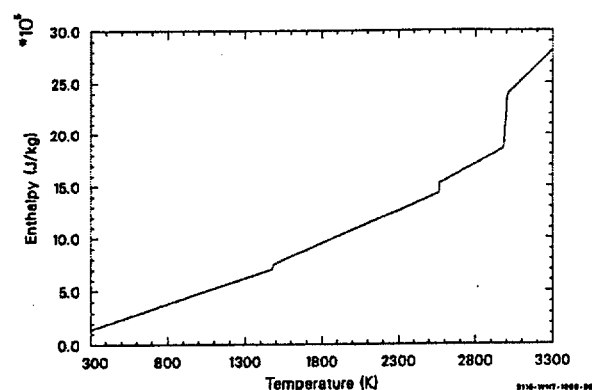
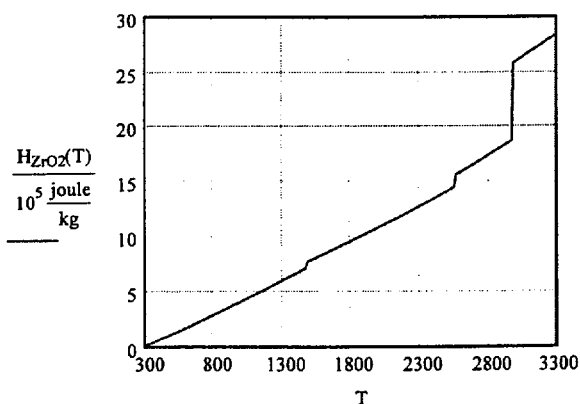


figure 5-3. Zircaloy oxide enthalpy as a function of temperature.